



Two epochs VLBA Imaging of Sgr A* at 86 GHz

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At 30



In collaboration with

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Sgr A*

- as a gravitational source

- dark mass $\sim 3 \times 10^6 M_{\text{sun}}$ within a radius of 15 mas = 120 AU = 2000 R_{sch}
(motions of *s like **S0-2**)
- $M_{\text{SgrA}^*} > 4 \times 10^5 M_{\text{sun}}$
(motions of Sgr A* itself)

Sgr A*

- as a radiative source

- X-ray flaring of 200 – 900 sec rise/fall timescales
=> 7 - 30 R_{sch} or 0.05 - 0.2 mas
(Chandra and XMM-Newton)
- IR flares of 30 – 40 min
=> 5 AU (80 R_{sch}) or 0.6 mas
(VLT and Keck)
- Correlated radio/X-ray variation (Zhao et al 04')
=> $r_{\text{Radio}} > r_{\text{X-ray}} = 7 R_{\text{sch}}$ or 0.05 mas **At 30**

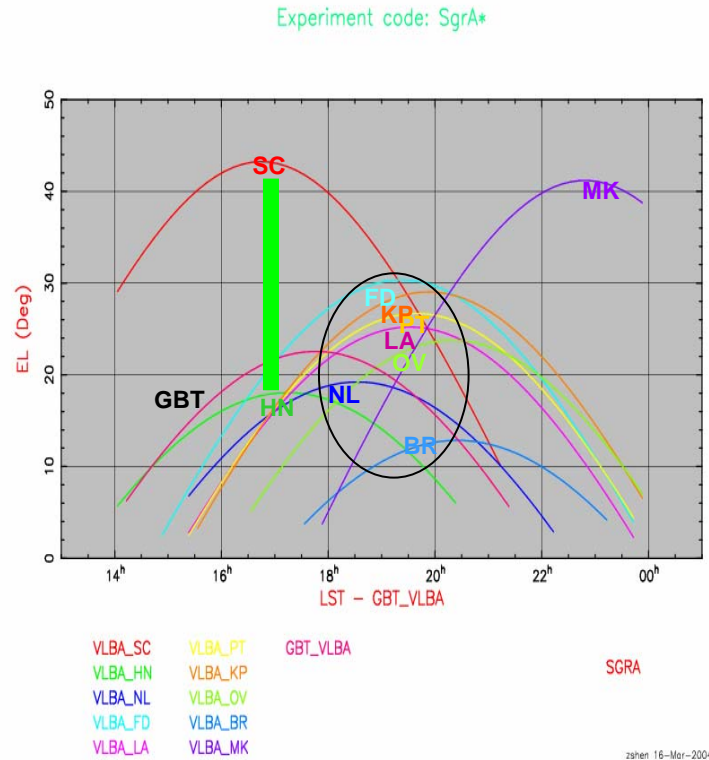
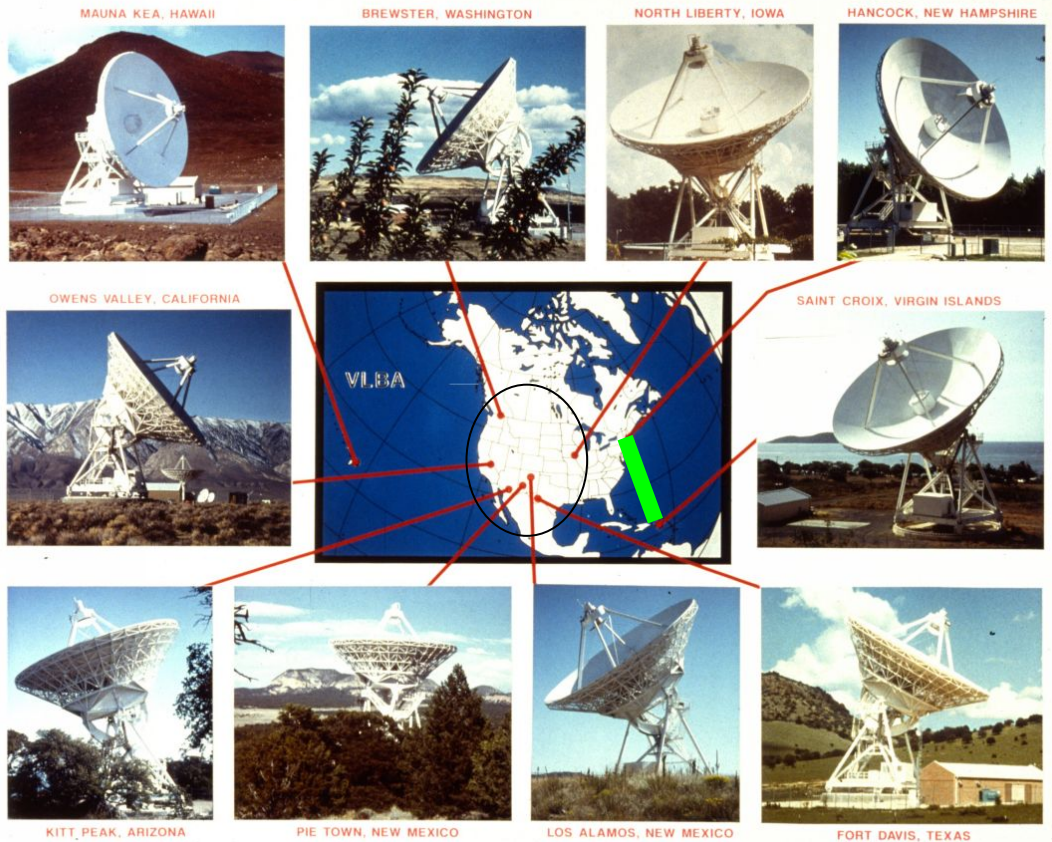
VLBI Observations of Sgr A*

- Interstellar scattering effect dominates the **cm-VLBI** images of SgrA* by λ^2 -law, with an *apparent* E-W elongated shape
- need for the mm-VLBI

Mm-VLBI Observations of Sgr A^{*}

- The mm-VLBI plagued by **2** facts
 - ☒ southerly Dec of SgrA^{*} ($\sim -30^\circ$)
 - ☒ northern lat. for most mm-VLBI antennas

Uptime plot of VLBA Observations of Sgr A*



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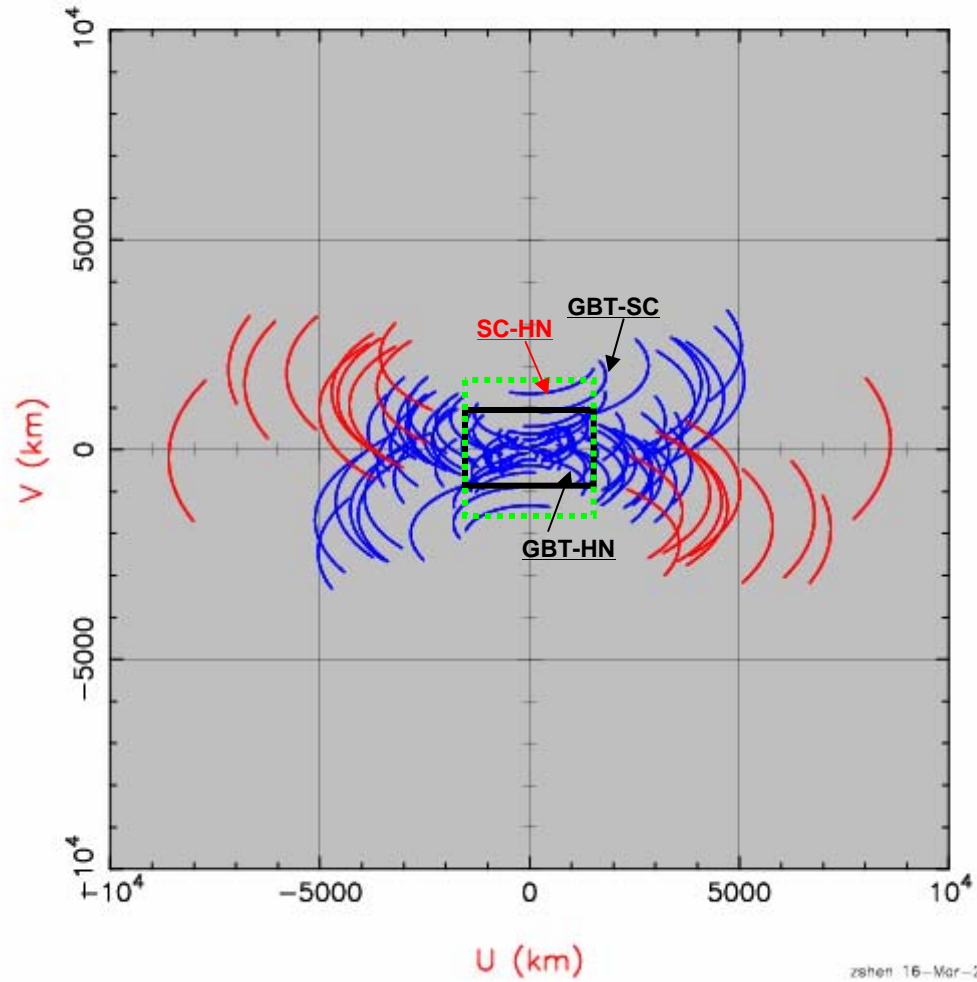
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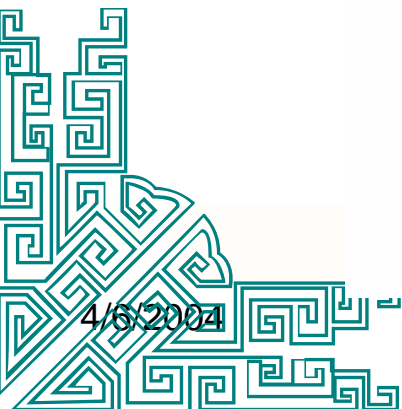
(u,v) coverage of VLBA Observations of Sgr A*

UV Coverage for SgrA*

- VLBA_SC
- VLBA_HN
- VLBA_NL
- VLBA_FD
- VLBA_LA
- VLBA_PT
- VLBA_KP
- VLBA_OV
- VLBA_BR
- VLBA_MK
- GBT_VLBA
- SGRA



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Mm-VLBI Observations of Sgr A*

- The mm-VLBI plagued by **2** facts
 - ☒ southerly Dec of SgrA* ($\sim -30^\circ$)
 - ☒ northern lat. for most mm-VLBI antennas
- ✗ lack of spatial resolution in N-S (= minor axis)
- ✗ severe atmospheric effects on data calibration
(large and variable opacity, short and variable T_{coh})
- + compromised sensitivity at mm-band
(high T_{sys} : >100 K at zenith; low antenna efficiency: $< 45\%$)

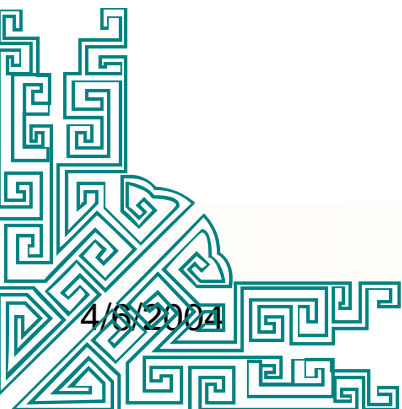
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How to improve



- During the observations
 - ✓ dynamic scheduling -> best weather condition
 - ✓ compact SiO masers for amp cal and pointing
- During the data analysis
 - ✓ closure amplitudes to constrain the model-fitting

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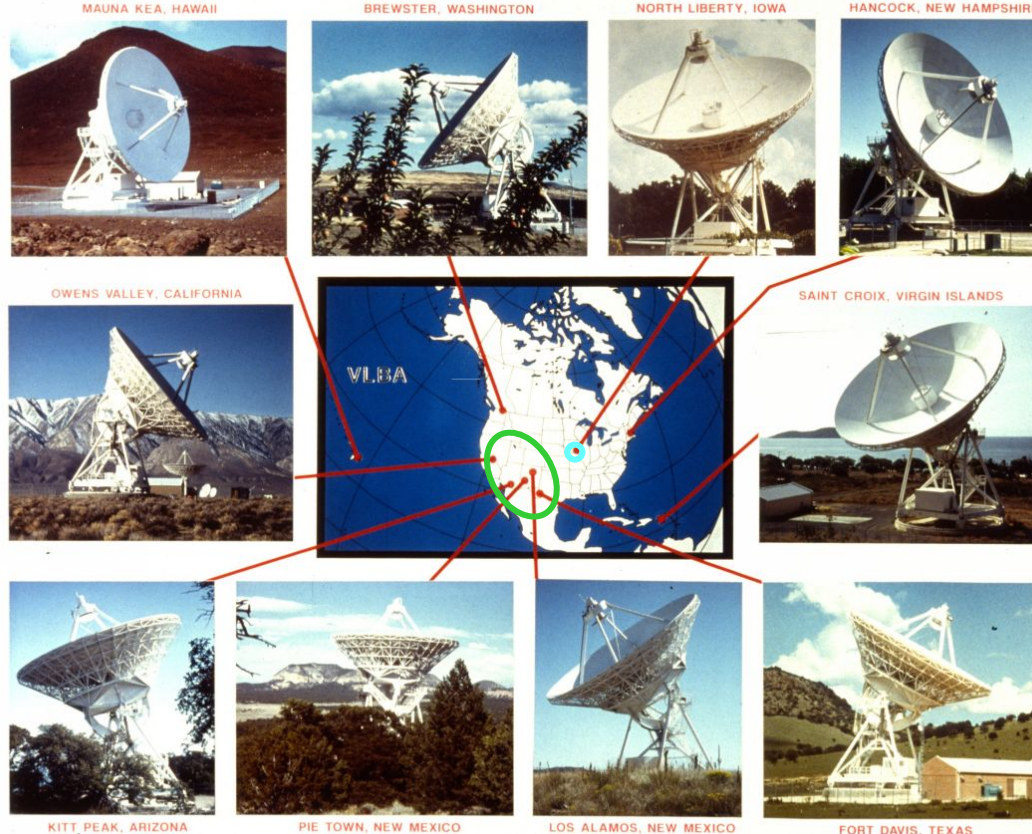
1st epoch 3mm VLBA Observation

- Nov 3, 2002 (dynamic since Feb 2001)
- 512 Mbps (highest recording rate)
- Frequent pointing check (every 15 min)
- Very good detections among 5 antennas (FD/KP/LA/OV/PT), plus some to NL
- First 3mm VLBI image of SgrA^{*}

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1st epoch 3mm VLBA Observation

- Very good detections among 5 antennas (FD/KP/LA/OV/PT), plus some to NL

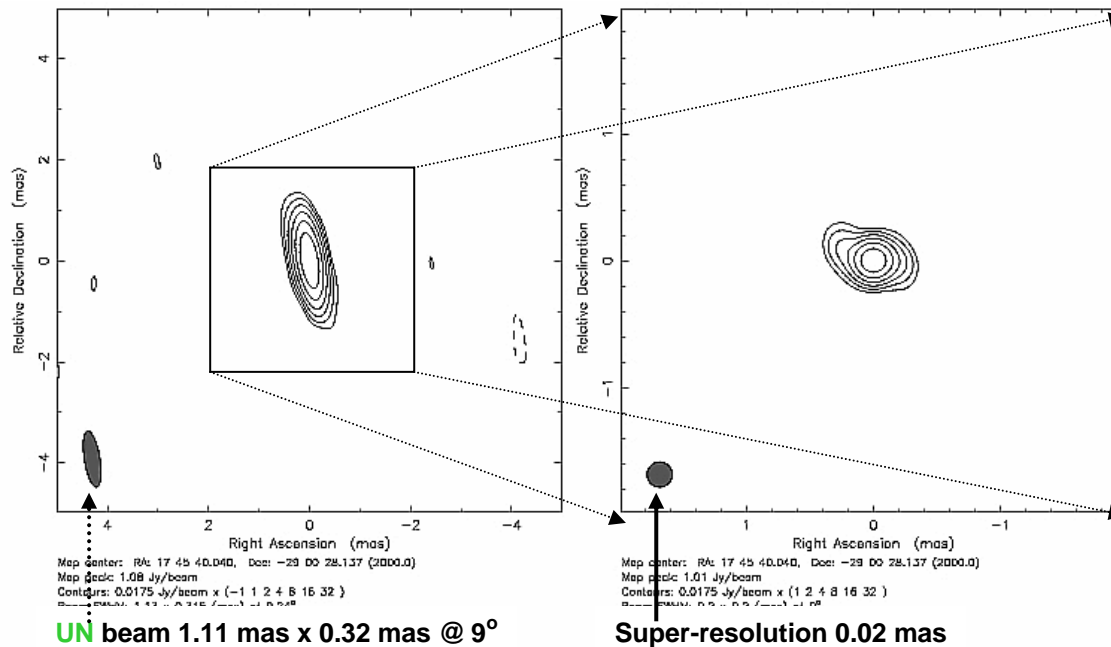


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1st epoch 3mm Observation

- First 3mm VLBI image of SgrA*



- ⊕ unresolved (no extended structure) → single component
- ⊕ zero closure phases
- ⊕ ~ E-W elongated emission → consistent with $\lambda \geq 7\text{mm}$ data

Model-fitting using the closure amplitude constraints

- χ^2 – *minimization* algorithm

$$\chi^2 = \sum_t \sum_{ij} w_{ij} |A_{ij}^{obs}(t) - G_i(t) G_j(t) A_{ij}^{mod}(t)|^2$$

here, the visibility amplitude A_{ij} is used,

“good observable” - the closure amplitude

$$C_{ijkl} = \frac{A_{ij} A_{kl}}{A_{ik} A_{jl}}$$

is conserved by assuming an antenna-dependent gain G_i only.

This is equivalent to the use of closure quantities!

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Bias Correction

- The measured visibility amplitude $\langle Z \rangle$ has a **positive bias** with respect to the true amplitude A

$$\langle Z \rangle \approx A \left(1 + \frac{\sigma^2}{2A^2} \right) \quad (\text{strong signal : } A \gg \sigma)$$

$$\langle Z \rangle \approx \sigma \sqrt{\frac{\pi}{2}} \left(1 + \frac{A^2}{4\sigma^2} \right) \quad (\text{weak signal : } A \ll \sigma)$$

here, σ is the rms deviation of a single component of the complex noise vector. This is **big at low SNR** ≤ 3 , but **can be corrected** (see Thompson, Moran, & Swenson 1986)

However, it is difficult to estimate the unbiased \mathbf{C}_{ijkl} and thus to treat its formal error properly if we fit the closure amplitude directly (see Trotter, Moran, & Rodriguez 1998).

At 30

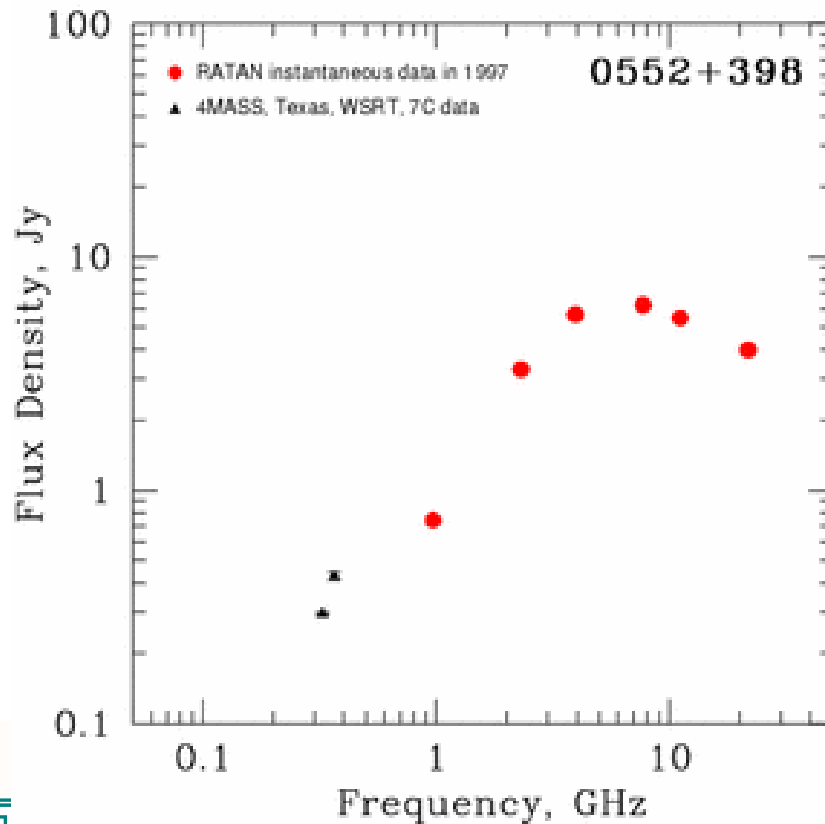
Model-fitting procedure

- χ^2 – *minimization* algorithm
- Bias correction to the measured visibility amplitude $A_{ij}(t)$
- Determination of the antenna-based gain G_i from the observed visibility amplitude A and the given model \tilde{A} at each time t
- Comparison of χ^2 for different model \tilde{A} to get the best fit model
- Error estimate from the χ^2 distribution
1 σ (68.3% confidence): $\chi^2(\text{min}) \rightarrow \chi^2(\text{min}) + \chi^2(\text{min}) / N_{\text{dof}}$



Application to DA193

- DA193 ($z=2.365$)



GPS source

VLBI calibrator

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Application to DA193

- **DA193: VLBI calibrator**

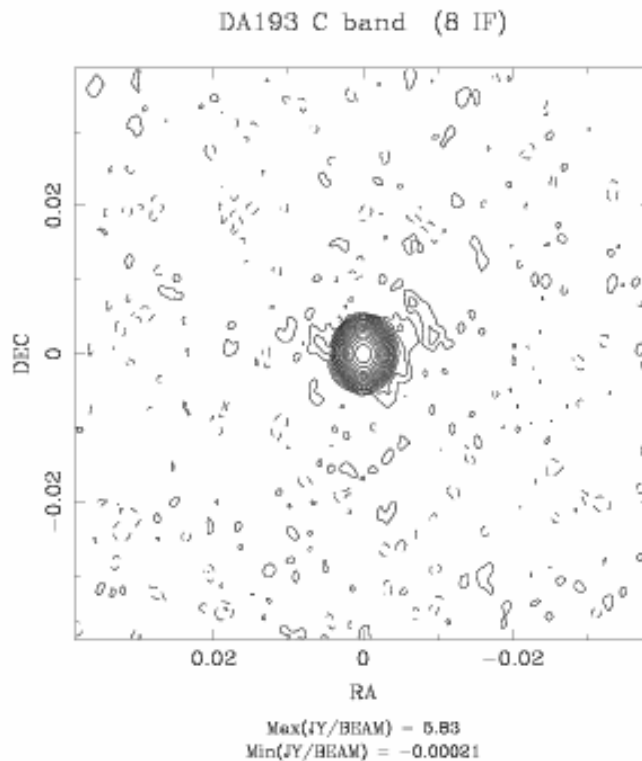


Figure 9.13: High dynamic range image of DA193. Peak to off-source RMS is 115,000:1

D. Briggs thesis (1995)

DR = 115,000:1

fit with a single Gaussian

0.904 x 0.514 mas @109.5°

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Application to DA193

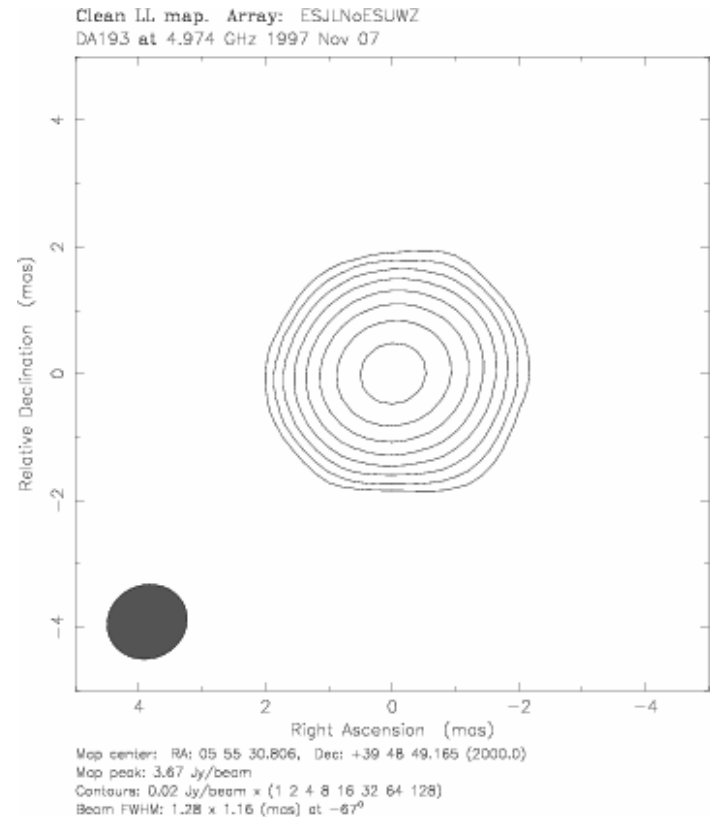
- DA193: EVN+Sh+Ur+Hart
(Nov 7, 1997)

- Standard VLBI self-calibration imaging and model-fitting

0.82 x 0.64 mas @ 111°

- Our procedure

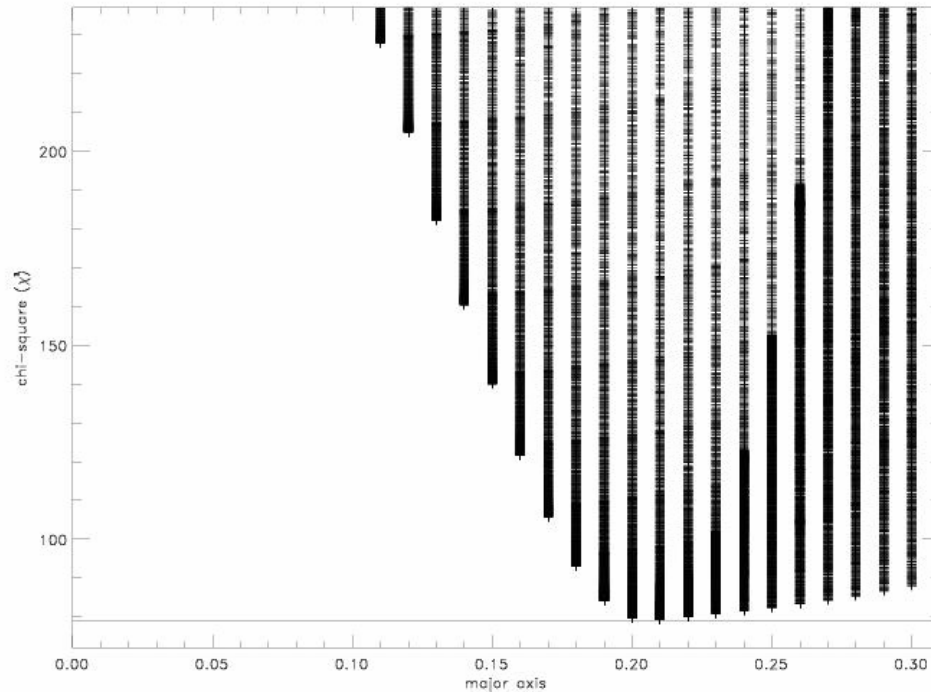
0.82 x 0.48 mas @ 108°



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1st epoch 3mm Observation

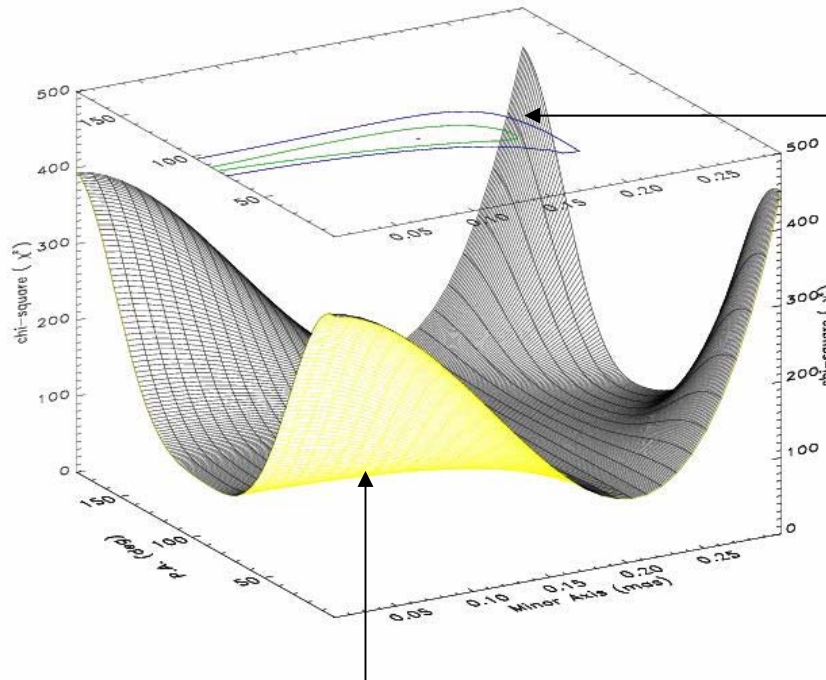
- **major axis: 0.21 (+0.02 / -0.01) mas**



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1st epoch 3mm Observation

- Minor axis: $0.13 (+0.05 / -0.13)$ mas
and PA: $79^\circ (+12^\circ / -33^\circ)$



Contour plot showing the Confidence intervals of 68.3% and 90.0%.

Surface plot of Chi^2 as a function of both minor axis and PA (major axis = 0.21 mas).

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1st epoch 3mm Observation

- **Model fitting:**

- ✓ **Single elliptical Gaussian**

major axis: 0.21 (+0.02 / -0.01) mas

minor axis: 0.13 (+0.05 / -0.13) mas

position angle: 79° (+12° / -33°)

- ✓ **Best Circular Gaussian**

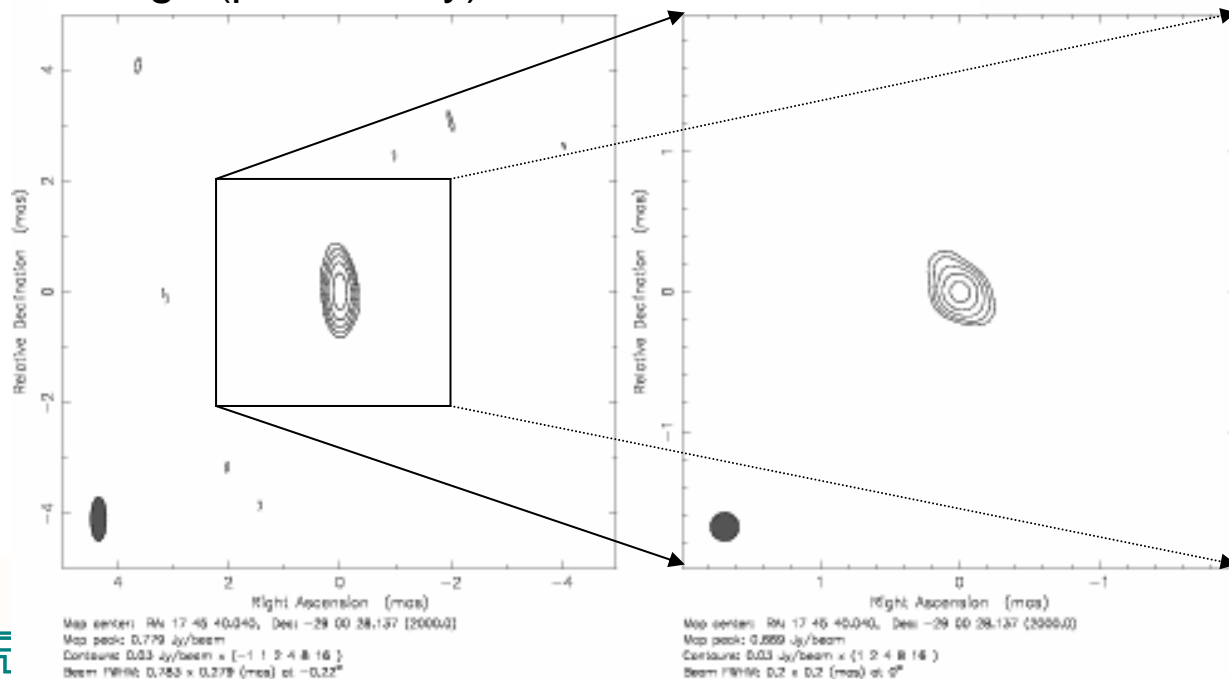
FWHM: 0.20-0.21 mas

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2nd epoch 3mm VLBA Observation

- Observations on Sept 28, 2003
- ✓ 512 Mbps; pointing check every 15 min
- ✗ gust @OV, tape (recording, playback) @KP, PT

Image (preliminary)



At 30

2nd epoch 3mm Observation

- **Model fitting:**

- ✓ **Single elliptical Gaussian**

major axis: 0.21 (+0.01 / -0.01) mas

minor axis: 0.00 - 0.13 mas

position angle: 87° (+12° / -9°)

- ✓ **Best Circular Gaussian**

FWHM: 0.20 mas

Discussion

- *Apparent* SgrA* structure at 3mm: elongated roughly along E-W with a major axis size of 0.21 mas

	Elliptical Gaussian Model (major,minor,pa)	circular
1999 Apr, CMVA (Doeleman et al 2001)	0.34(+/-0.14), 0.17(+/-0.02), 22(+/-20)	0.18(+/-0.02)
2002 Nov, VLBA	0.21(+0.02/-0.01), 0.13(+0.05/-0.13), 79(+13/-33)	0.20 - 0.21
2003 Sept, VLBA	0.21(+0.01/-0.01), 0.00-0.13, 87(+12/-9)	0.20

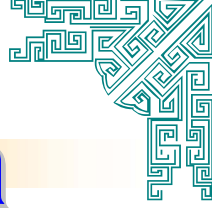
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Discussion

- *Intrinsic* structure of SgrA* emission

The best ever measurement in Nov 2002 shows a 3σ deviation from the extrapolated scattering angle of 0.175 ± 0.003 mas along the major axis. If confirmed, this indicates an intrinsic size of **0.116 mas, or ~ 1 AU @ 8 kpc, or ~ 17 Rsch ($3 \times 10^6 M_{\text{sun}}$).**

Intrinsic Tb $\sim 1.5 \times 10^{10}$ K (non-thermal origin)



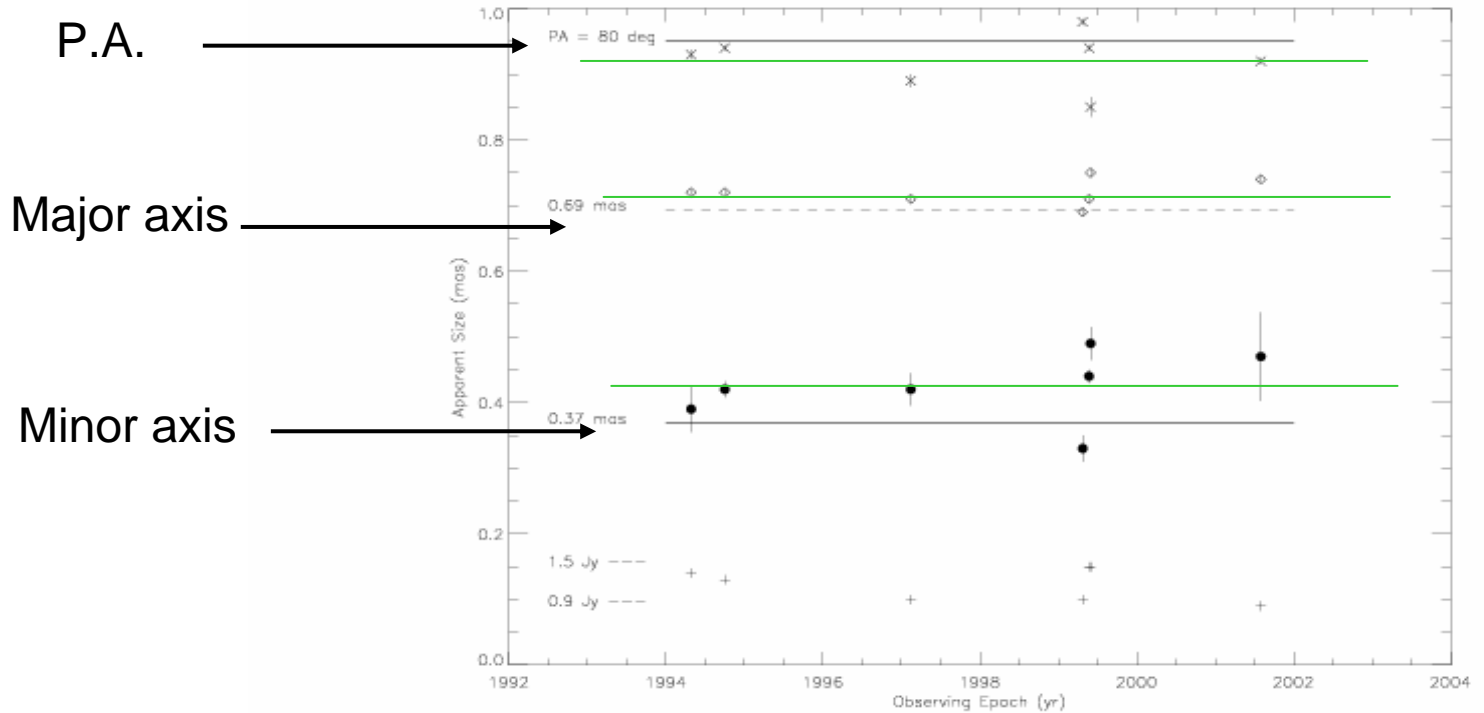
Discussion – 7mm data

Epoch	Ctr Freq(+BW) GHz (+ MHz)	S (Jy)	Major axis (mas)	Minor axis (mas)	P.A (degree)	Reduced chi ²	SC- HN	Notes
1994.32	43.151 (64)	1.4	0.72 +/- 0.01	0.39 +/- 0.07	78 +/- 2	1.11	yes	
1994.75	43.151 (64)	1.3	0.72 +/- 0.01	0.42 +/- 0.03	79 +/- 1	1.17	yes	Bower & Backer 1998
1997.12	43.213 (32)	1.0	0.71 +/- 0.01	0.42 +/- 0.05	74 +/- 2	2.89	no	Lo et al 1998; dual pol
1999.31	43.135 (32)	1.0	0.69 +/- 0.01	0.33 +/- 0.04	83 +/- 1	0.97	yes	1.26 x 0.44 @ 7°
1999.39	43.135 (32)	1.5	0.71 +/- 0.01	0.44 +/- 0.02	79 +/- 1	1.59	yes	1.35 x 0.48 @ 11°
1999.41	43.135 (32)	1.5	0.75 +/- 0.01	0.49 +/- 0.05	70 +/- 3	0.85		
	39.135 (32)	1.6	0.86 +/- 0.01	0.54 +/- 0.03	78 +/- 1	1.54		39 GHz
	45.135 (32)	1.5	0.66 +/- 0.01	0.42 +/- 0.04	75 +/- 3	1.31		45 GHz
2001.58	42.8-43.1 (32)	0.9	0.74 +/- 0.01	0.47 +/- 0.14	77 +/- 6	3.41	yes	

Average over 7 epochs: major 0.72 +/- 0.02 mas
 minor 0.42 +/- 0.04 mas
 P.A. 77 +/- 3 deg

At 30

Discussion – 7mm data



At 30

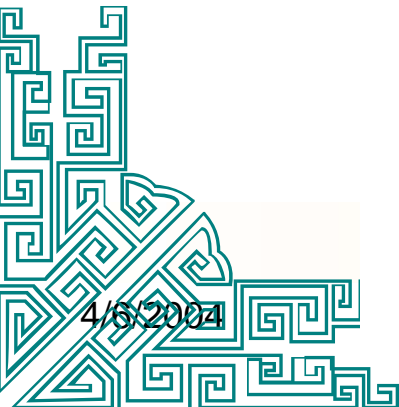


Discussion – past SgrA* size measurements

Table 1. Summary of published Sgr A* size measurements

Epoch (yrs)	SVLBI (Jy)	θ_{major} (mas)	θ_{minor} (mas)	Axial Ratio ($\theta_{\text{minor}}/\theta_{\text{major}}$)	P.A. ($^{\circ}$)	References
<u>$\lambda = 35.6 \text{ mm}$</u>						
1997.10	0.73±0.10	18.0±1.53	9.88±1.68	0.55±0.14	78±6	Lo <i>et al.</i> (1998)
1991.90		17.5±0.5	8.5±1.0	0.49±0.06	87±5	Lo <i>et al.</i> (1993)
1983.36		16.1±0.3	16.1	1.0		Marcaide <i>et al.</i> (1992)
1983.35		15.5±0.1		0.55±0.25	98±15	Lo <i>et al.</i> (1985)
1982.30		17.4±0.5		0.53±0.10	82±6	Jauncey <i>et al.</i> (1989)
1978.07	0.7	18±2	18	1.0		Lo <i>et al.</i> (1981)
1976.18	0.9±0.06	14±2	14	1.0		Lo <i>et al.</i> (1977)
1975.38	0.6±0.1	<20.0		1.0		Lo <i>et al.</i> (1975)
1974.50		17.0	17.0	1.0		
<u>$\lambda = 13.5 \text{ mm}$</u>						
1997.10	0.74±0.04	2.70±0.15	1.50±0.59	0.56±0.25	81±11	Lo <i>et al.</i> (1998)
1992.85	1.05±0.10	2.67±0.15	1.63±0.41	0.61±0.12	79±10	Marcaide <i>et al.</i> (1999)
1991.49	0.98±0.05	2.6±0.2	1.3	0.5	87	Lo <i>et al.</i> (1993)
1991.47	1.07±0.15	2.60±0.20	1.30±0.88	0.5±0.3	80±15	Alberdi <i>et al.</i> (1993)
1985.11	1.2±0.4	1.8±0.09	1.8	1.0		Marcaide <i>et al.</i> (1992)
1983.47	0.98±0.05	2.2±0.2	1.21±1.21	0.55±0.5	87±30	Lo <i>et al.</i> (1985)
<u>$\lambda = 6.9 \text{ mm}$</u>						
1997.10	1.03±0.01	0.70±0.01	0.58±0.07	0.83±0.11	87±8	Lo <i>et al.</i> (1998)
1994.75	1.28±0.10	0.76±0.04	0.55±0.11	0.73±0.10	77±7	Bower & Backer (1998)
1992.62	2.10±0.10	0.74±0.03	0.40±0.20	0.54±0.29	90±10	Backer <i>et al.</i> (1993)
1992.40	1.42±0.10	0.75±0.08	0.75	1.0		Krichbaum <i>et al.</i> (1993)
<u>$\lambda = 3.5 \text{ mm}$</u>						
1999.27	1.4	0.34±0.14	0.17±0.02	0.50±0.26	22±20	Doeleman <i>et al.</i> (2001)
	1.4	0.18±0.02	0.18	1.0		Doeleman <i>et al.</i> (2001)
1995.18	1.80±0.30	0.19±0.03	0.19	1.0		Krichbaum <i>et al.</i> (1998)
1994.25	1.40±0.20	0.15±0.05	0.15	1.0		Rogers <i>et al.</i> (1994)
1993.27	1.25±0.35	0.22±0.19	0.22	1.0		Krichbaum <i>et al.</i> (1999)

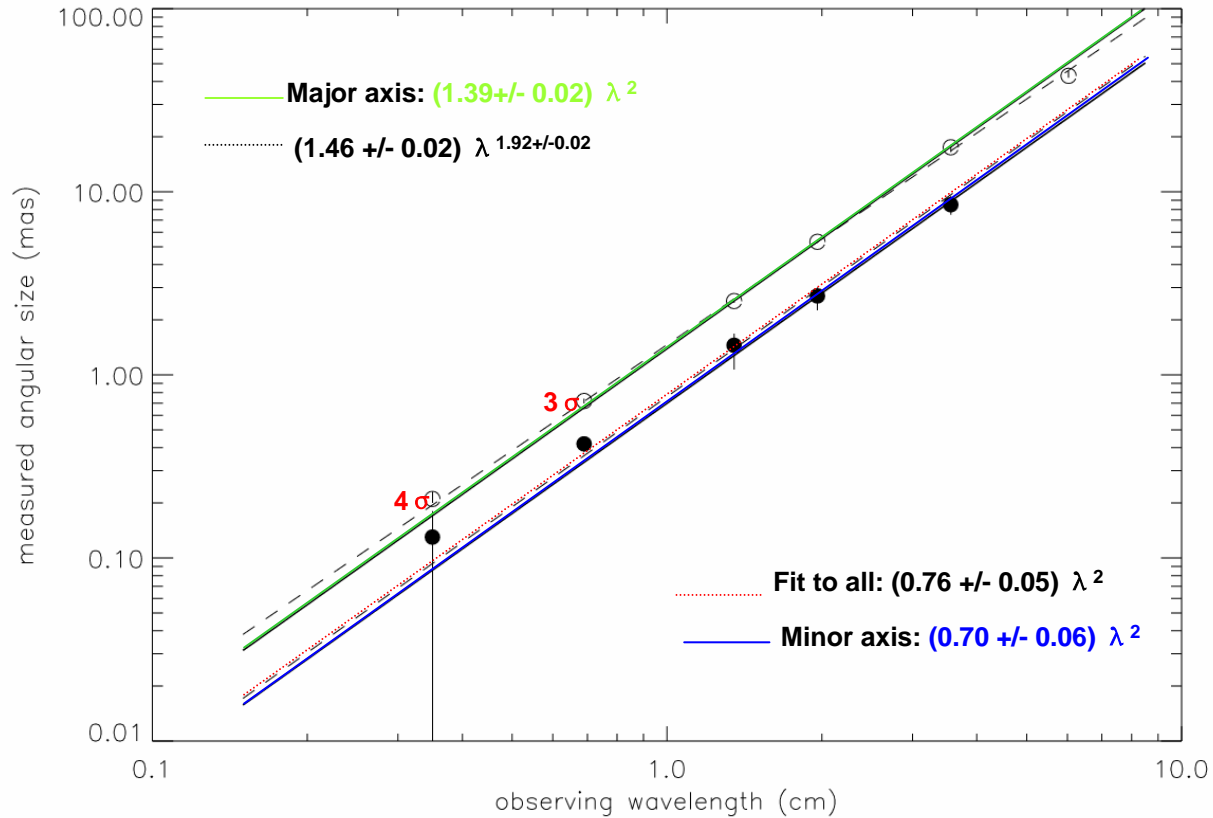
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Discussion – reanalysis of the archived VLBI data

λ (cm)	major (mas)	minor (mas)	p.a. (deg)	Resolution (mas x mas @ deg)	Notes
6.03	43.0 +2.5 /-1.0			21 x 12 @ 4	Only 1 epoch data!
3.56	17.5 +0.5/-1.0	8.50 +/- 1.0	87 +/- 3	12.5 x 6.5 @ 5	
1.96	5.33 +/- 0.07	2.70 +0.30/-0.44	83 +/- 3	9.5 x 3.9 @ 26	1 epoch only!
1.35	2.53 +0.06/-0.05	1.45 +0.23/-0.38	83 +4/-5	6.4 x 2.3 @ 24	
0.69	0.72 +/- 0.02	0.42 +/- 0.04	77 +/- 3	1.6 x 0.5 @ 10	Errors from the scatter of 7 epochs data
0.35	0.21 +0.02/-0.01		79 +12/-33	1.1 x 0.3 @ 9	Minor axis poor

Scattering law revisited



At 30

Summary



- First 3mm VLBA image of Sgr A* shows an E-W elongated structure, consistent with the morphology observed at other longer λ .
- A 3σ deviation from the extrapolated scattering angle of 0.175 mas at 3mm (from the current $1.43 \lambda^2$) may suggest an intrinsic size of 1 AU along E-W at 3mm.
- Investigation of the archived multi-wavelength data suggests a slightly smaller scattering effect of $1.39 \lambda^2$.
- The current scattering law needs to be re-examined with more measurements at both short (mm) and long (cm) wavelengths.

At 30