

# Using AW-Projection from CASA/ARDG branch

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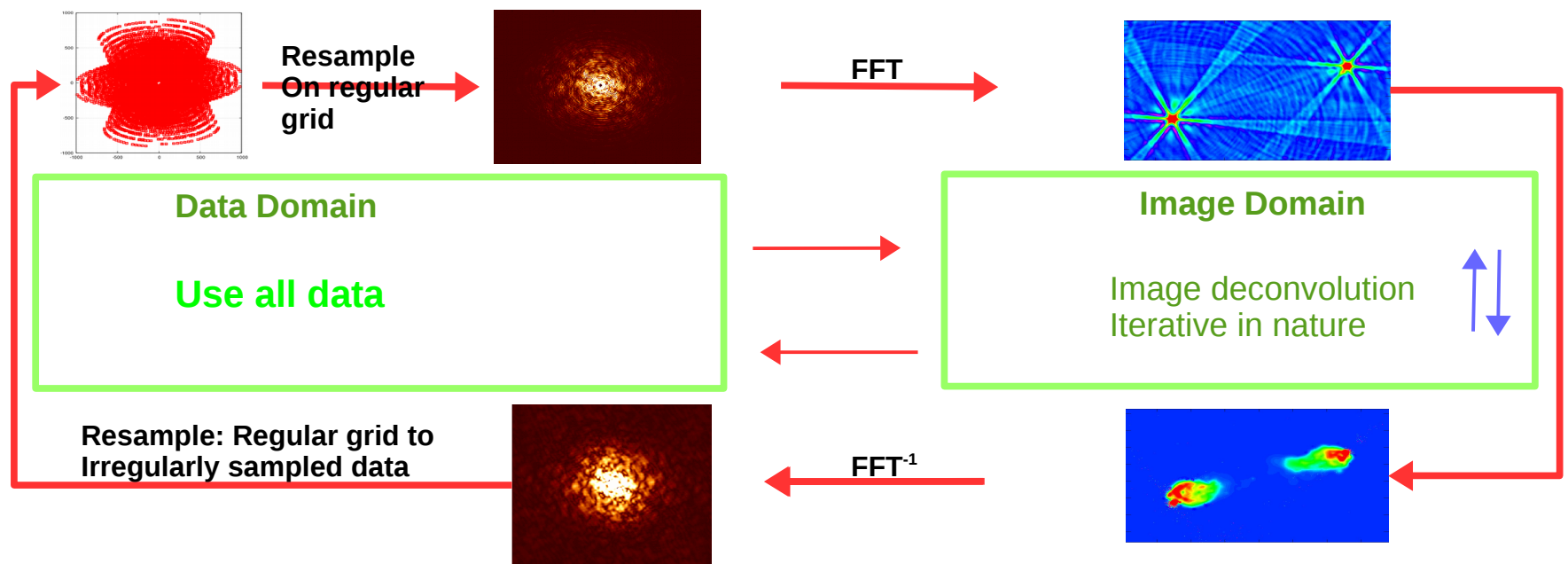
S. Bhatnagar

Sept. 7<sup>th</sup>, 2018



# Imaging & Deconvolution: A recap

- Compute residuals using the original data
  - Needs Gridding and de-Gridding during major-cycle iterations



**W-Projection**

**AW-Projection**

**WB AW-Projection**

**Standard gridding**

**CS-Clean**

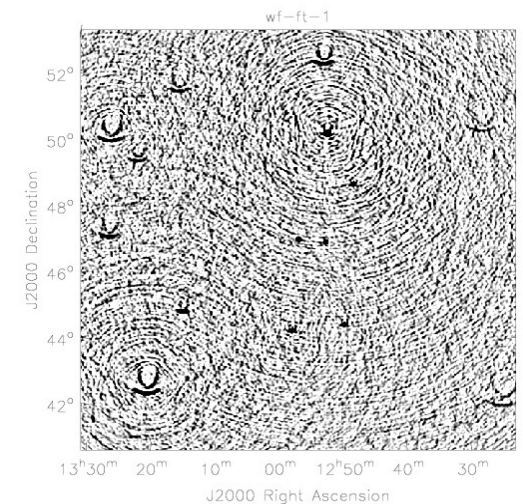
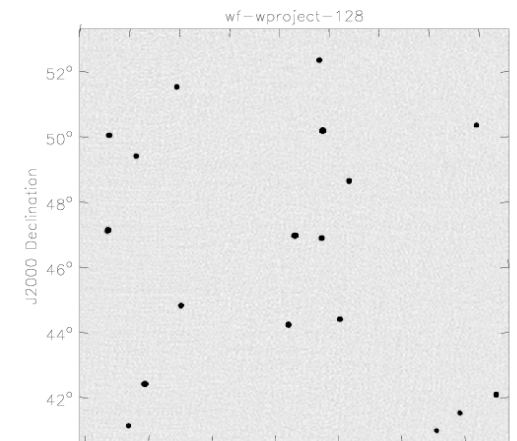
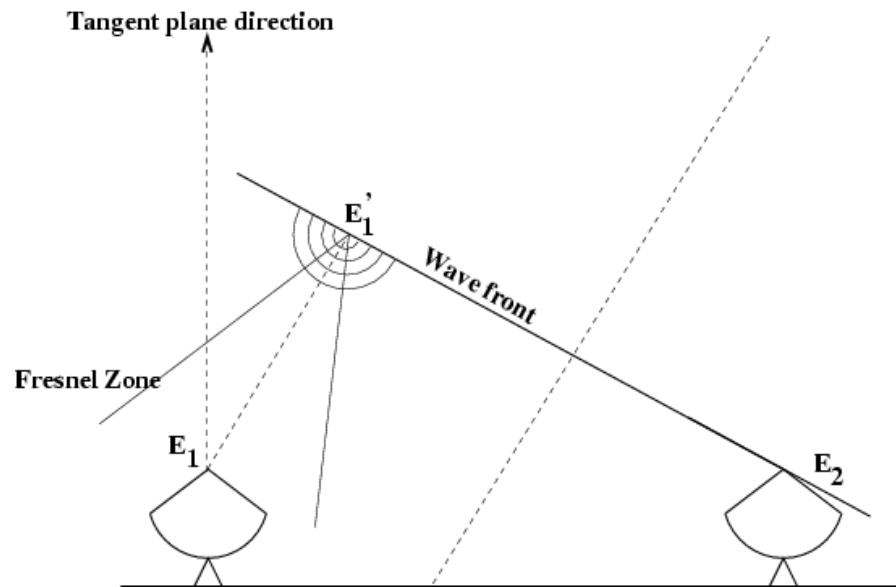
**MS-Clean**

**MT-MFS**

**Hogbom Clean**

# Non co-planar baseline: The W-term

- 2D FT approximation of the Measurement Equation breaks down

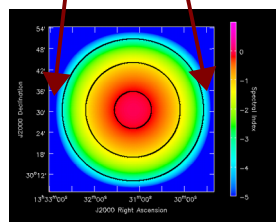
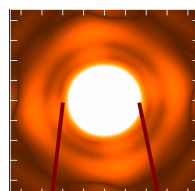
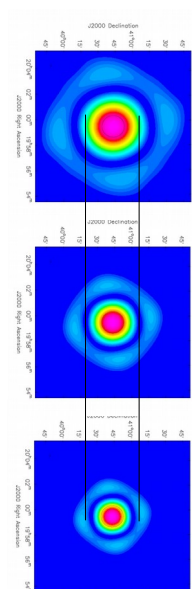


- We measure:  $V_{12} = \langle \mathbf{E}_1(u, v, w=0) \mathbf{E}_2^*(0,0,0) \rangle$
- We interpret it as:  $V_{12}^o = \langle \mathbf{E}_1'(u, v, w \neq 0) \mathbf{E}_2^*(0,0,0) \rangle$

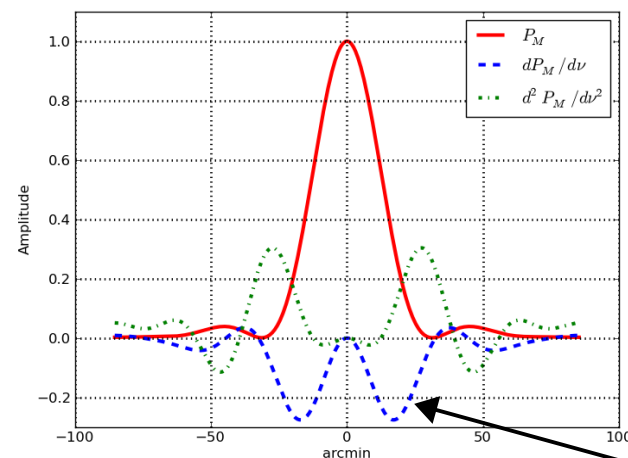
- We should interpret  $\mathbf{E}_1$  as  $[\mathbf{E}_1' \times \text{Fresnel Propagator}]$

# Wide-band Wide-field Imaging

- Wide band data to image beyond the  $\sim 50\%$  point of the PB at a reference frequency
  - Bandwidth ratio  $> \sim 20\%$
  - FoV  $> \sim \text{HPBW}$  @ reference frequency
  - Variable PB:
    - Long integration (rotation), Mosaicking (pointings at different PA), in-beam polarization is large (AA)



PB "Spectral Index"



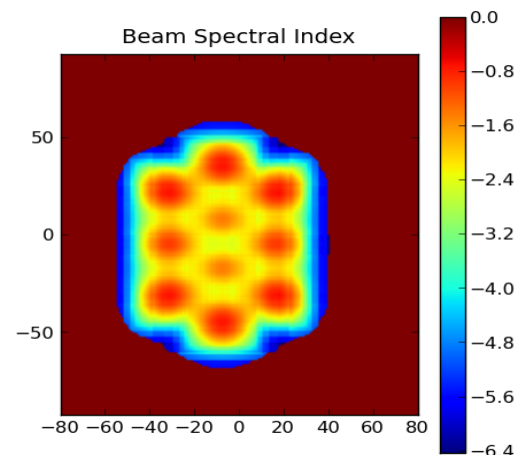
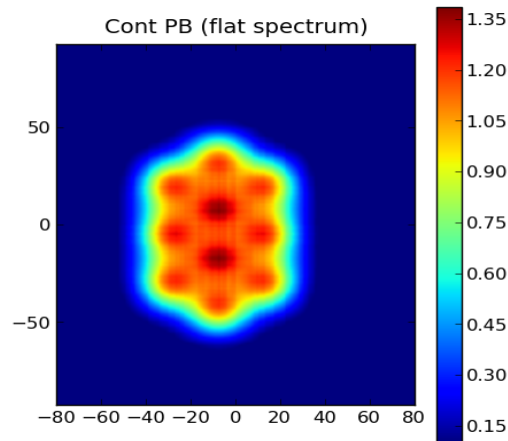
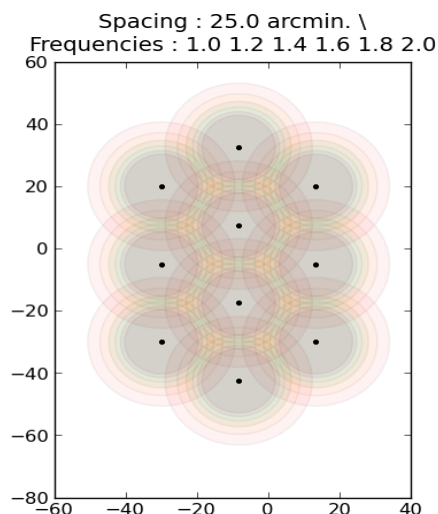
PB Frequency dependence (blue curve)

# Wideband Primary Beams – Mosaic

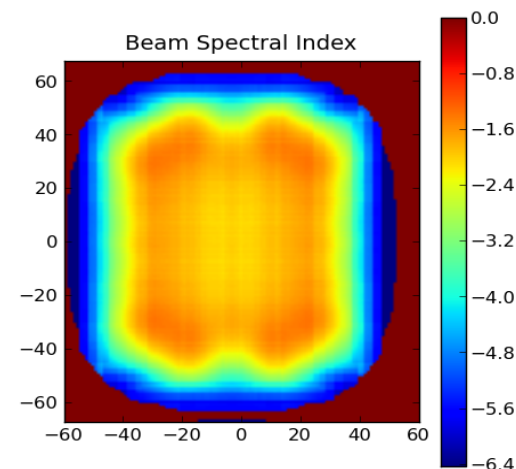
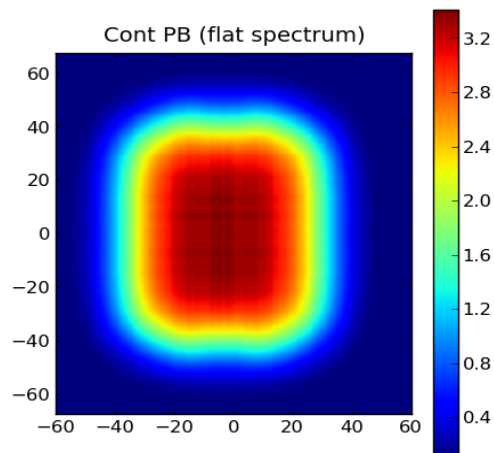
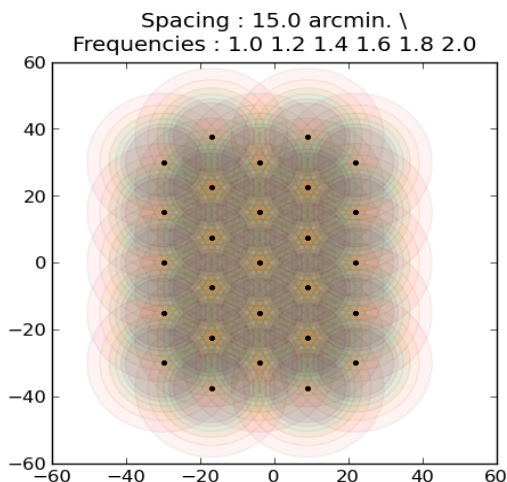
For single pointings, the wideband PB spectrum is relevant only away from the pointing center.

For mosaics, the wideband PB spectrum must be accounted-for all over the mosaic field of view

25 arcmin  
spacing  
(1-2 GHz)

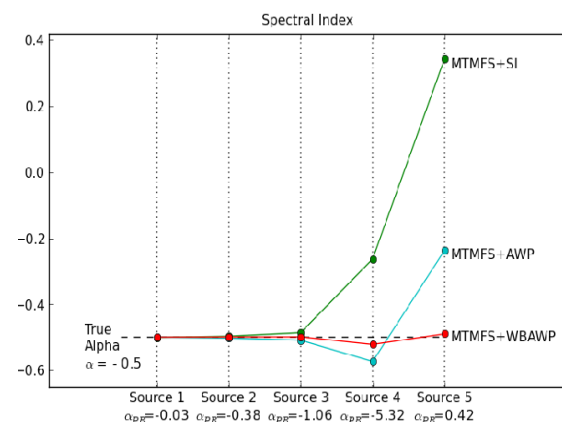
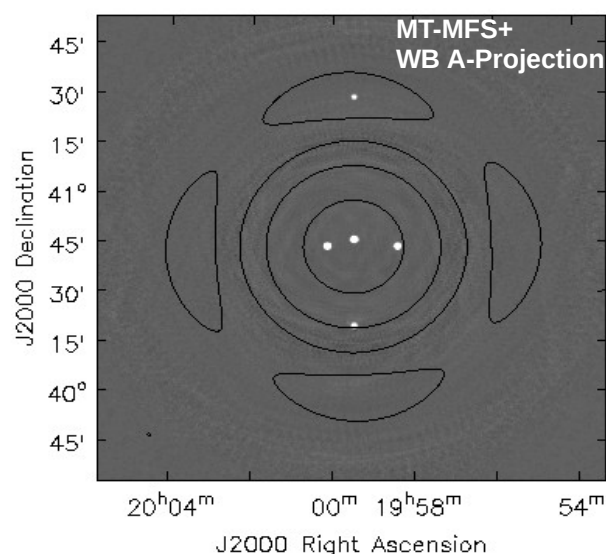
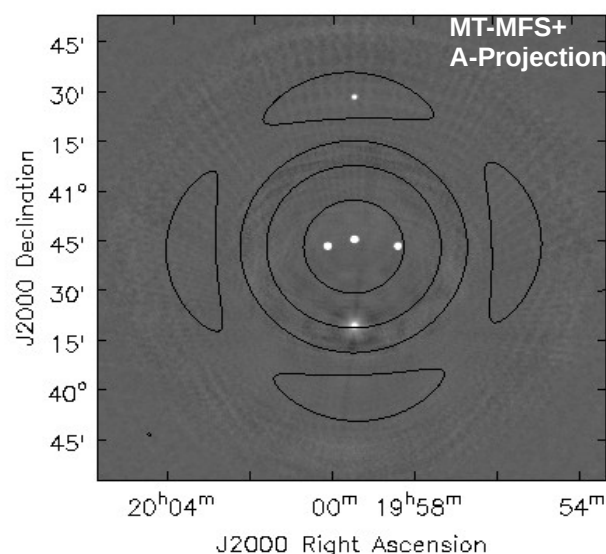
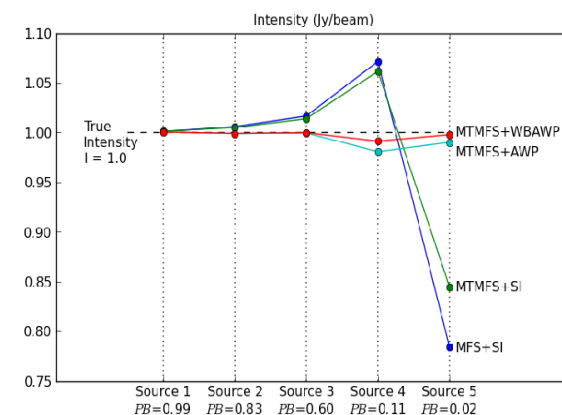
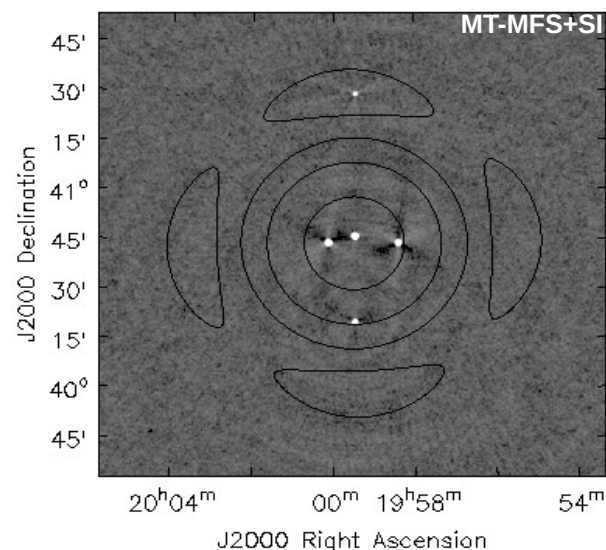
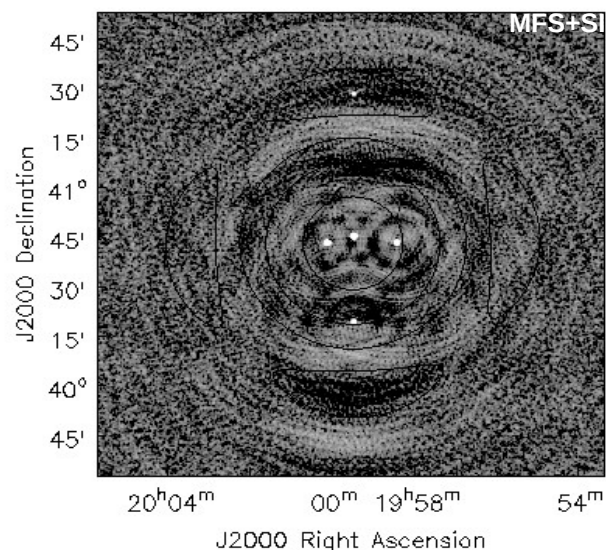


15 arcmin  
spacing  
(1-2 GHz)



# Wide-band Wide-field Imaging

- Characterization of the (WB) A-Projection + MT-MFS



# Why new algorithms?

$$V_{ij}(\nu) = G_{ij}^{DI} R_{ij} \int \underbrace{P_{ij}(s, \nu, t) I(s, \nu) e^{i[u_{ij}l + v_{ij}m + w_{ij}(\sqrt{1-l^2-m^2}-1)]}}_{\text{Direction Dependent (DD) terms}} ds$$

- Terms inside the integral cannot be accounted-for before imaging
  - Conventional imaging ignores DD terms
  - Also ignores time, frequency and polarization dependence
- Solutions: Project-out the effects during imaging + model frequency dependence of the sky during deconvolution
  - WB AW-Projection + MT-MFS
  - AWP with *conjbeams=True*
- Spectral cube imaging + image-plane corrections/averaging
  - AW-Projection for Cube Imaging + MT-MFS on collapsed cube
  - AWP with *conjbeams=False*

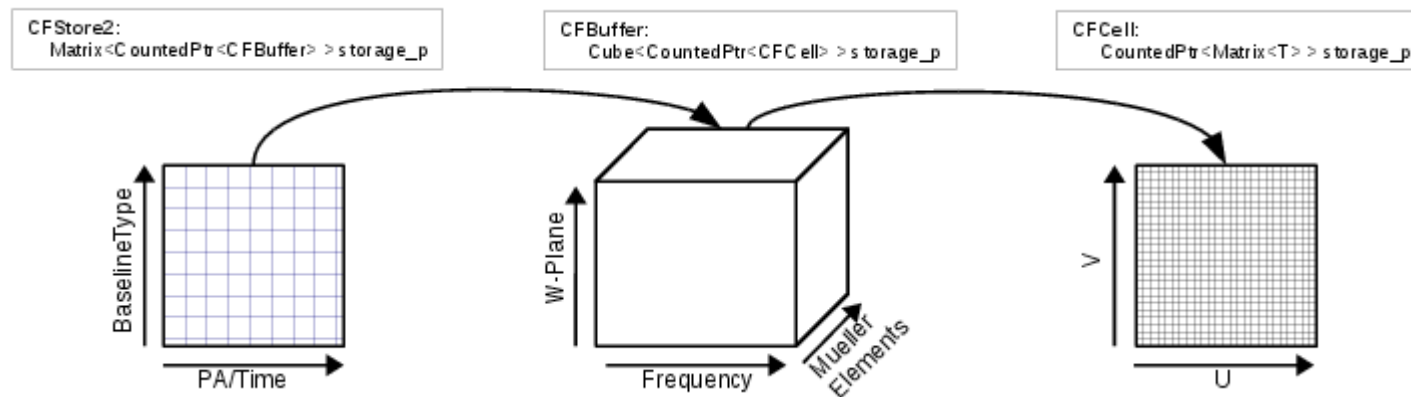
$$V_{ij}(\nu) = G_{ij}^{DI} R_{ij} \int P_{ij}(s, \nu, t) I(s, \nu) e^{i[u_{ij}l + v_{ij}m]} e^{i w_{ij}(\sqrt{1-l^2-m^2}-1)} ds$$

# Why new algorithms?

$$V(v, u_{ij}, v_{ij}, w_{ij}) = R_{ij} \int \left[ P_{ij}(s, v, t) I^M(s, v) e^{i w_{ij} (\sqrt{1-l^2-m^2}-1)} \right] e^{i [u_{ij} l + v_{ij} m]} ds$$

$$V(v, u_{ij}, v_{ij}, w_{ij}) = R_{ij} \left[ A(u_{ij}, v_{ij}, v, t) * W(u_{ij}, v_{ij}) * V^o(u_{ij}, v_{ij}) \right] = R_{ij} CF_{ij} * V_{ij}^o$$

- **A** : A-term/Aperture term. Fourier transform of the antenna PB
- **W** : W-term/Non-coplanar array. Fourier transform of the w-term (Fresnel propagator)
- CF is the Convolution Function. A 2D function that varies with frequency, time, polarization, w-value and antenna pairs (baseline)



# Projection algorithms

- Direction-dependent effects in the image domain are convolutional terms in the data domain
- Projection algorithms for DD corrections:
  - Project-out various DD effects as part of the gridding operator

- ME:

$$V_{ij}^{Obs} = A_{ij} * V^o + N_{ij}$$

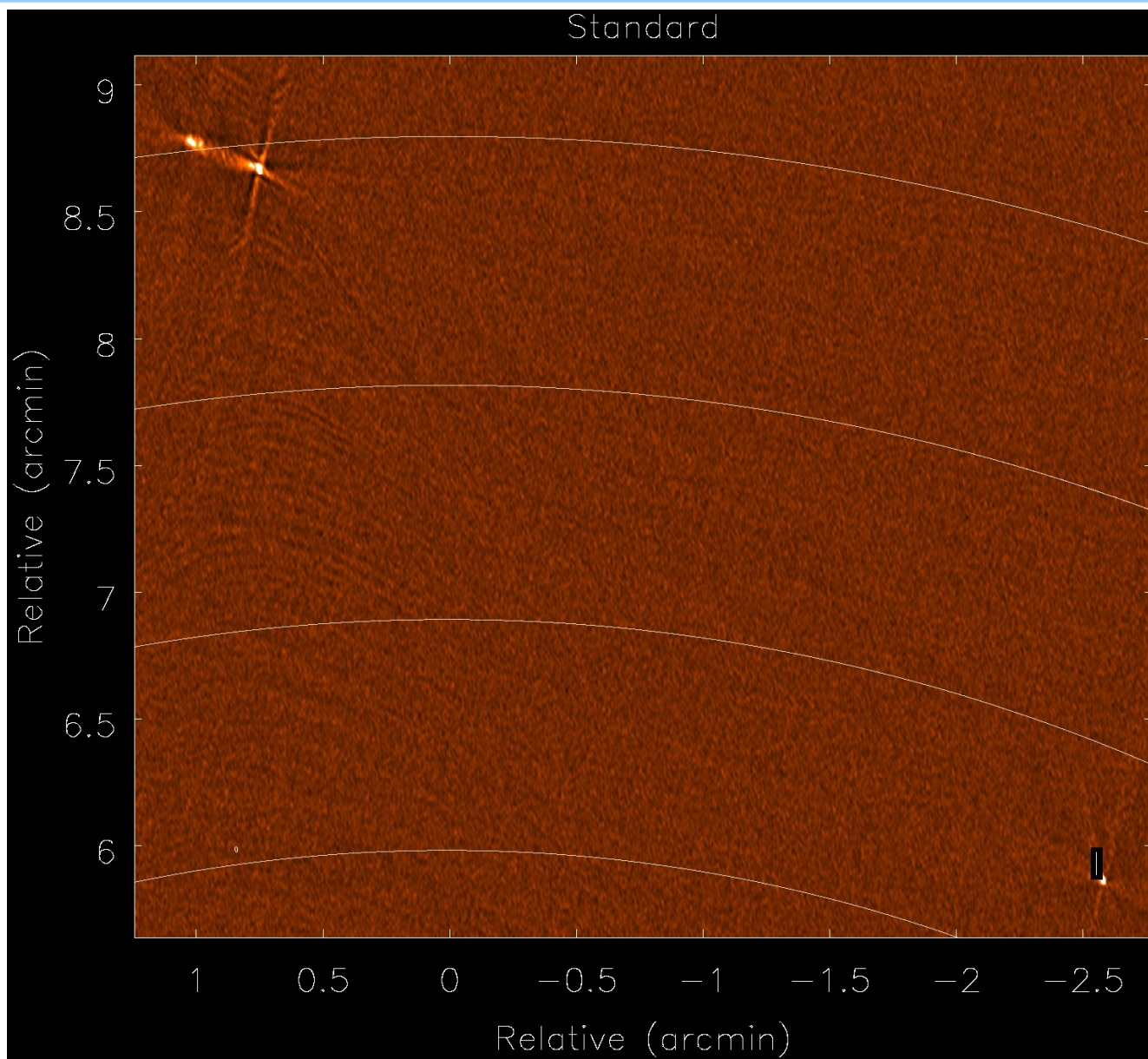
- Construct D, such that

$$D_{ij}^T * A_{ij} \approx \text{Time/Freq./Pol. indep.}$$

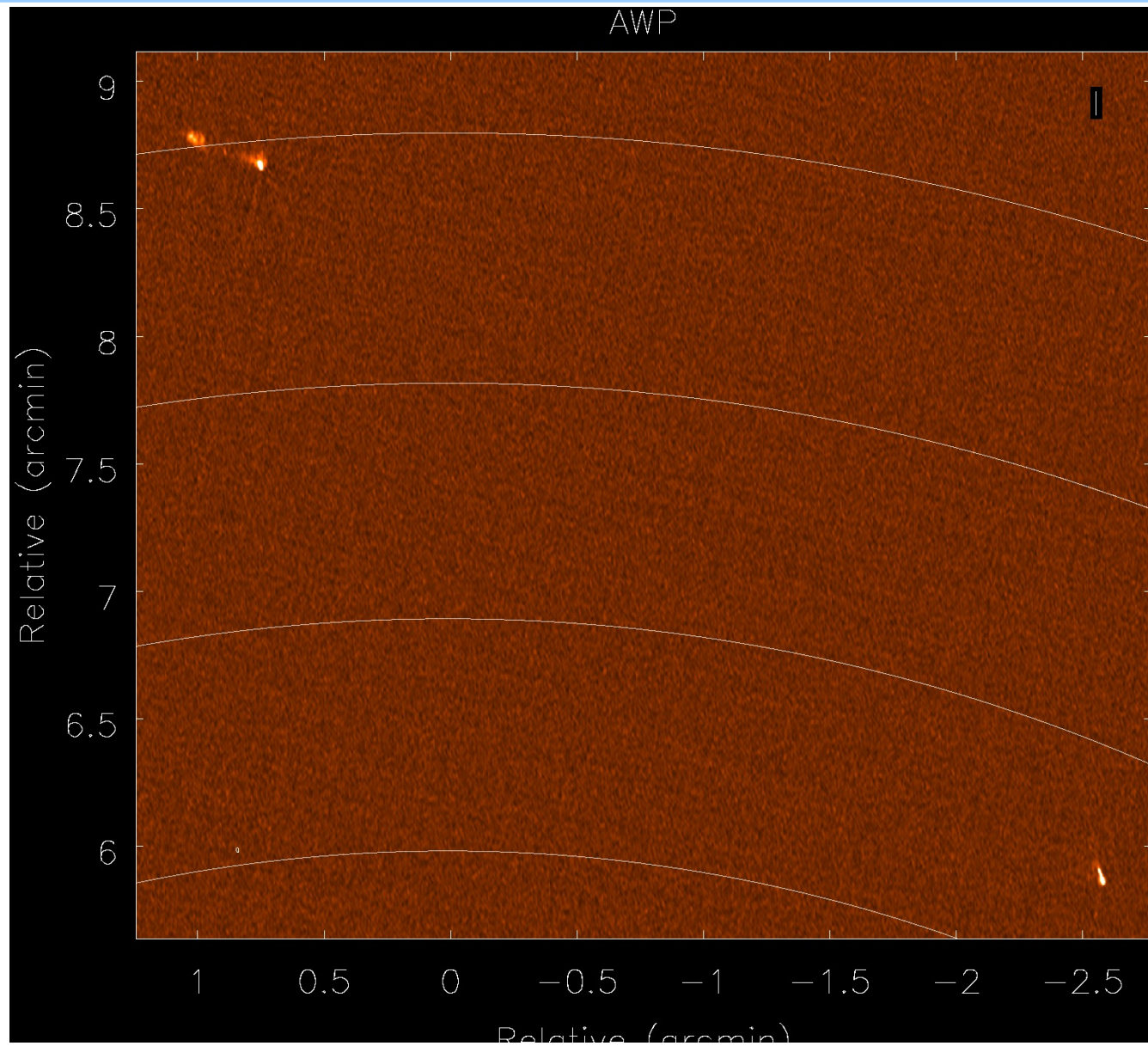
- Imaging:

$$I = F^{-1} \sum_{ij} D_{ij}^T * V_{ij}^{Obs} = F^{-1} \frac{\sum_{ij} D_{ij}^T * A_{ij} * V_{ij}^o + D_{ij}^T * N_{ij}}{\text{Normalization}}$$

# S-Band A-array imaging: Standard gridder

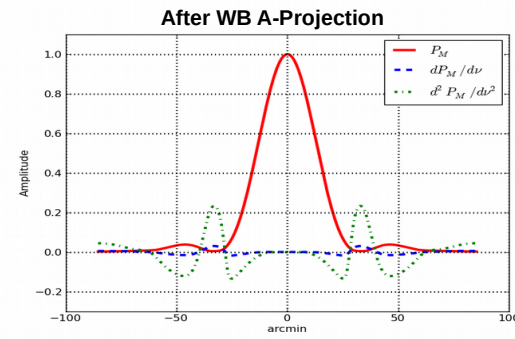
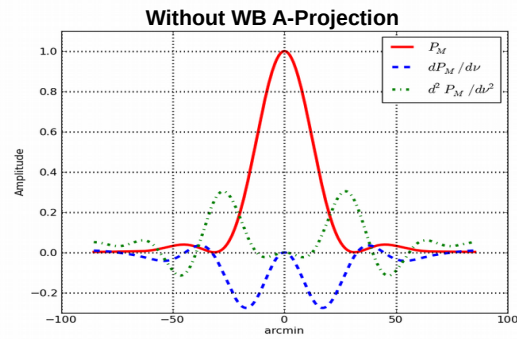


# S-Band A-array imaging: AWP gridder

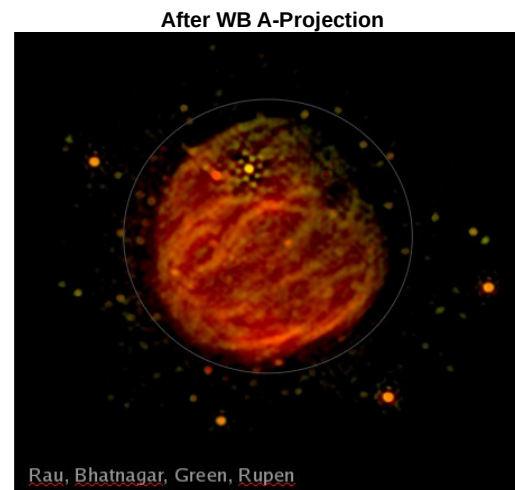
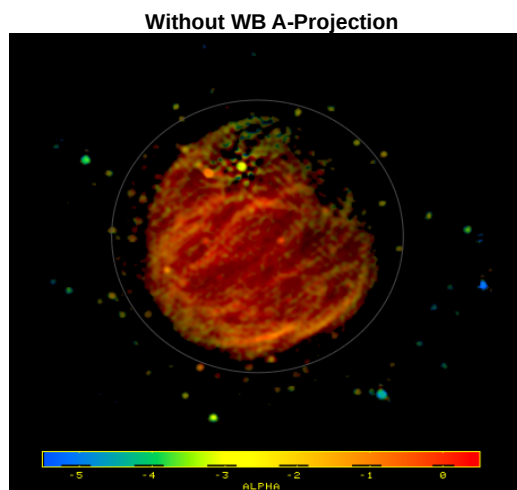


# Wide-band Wide-field Imaging

- WB A-Projection + MT-MFS
  - WB A-Projection for PB

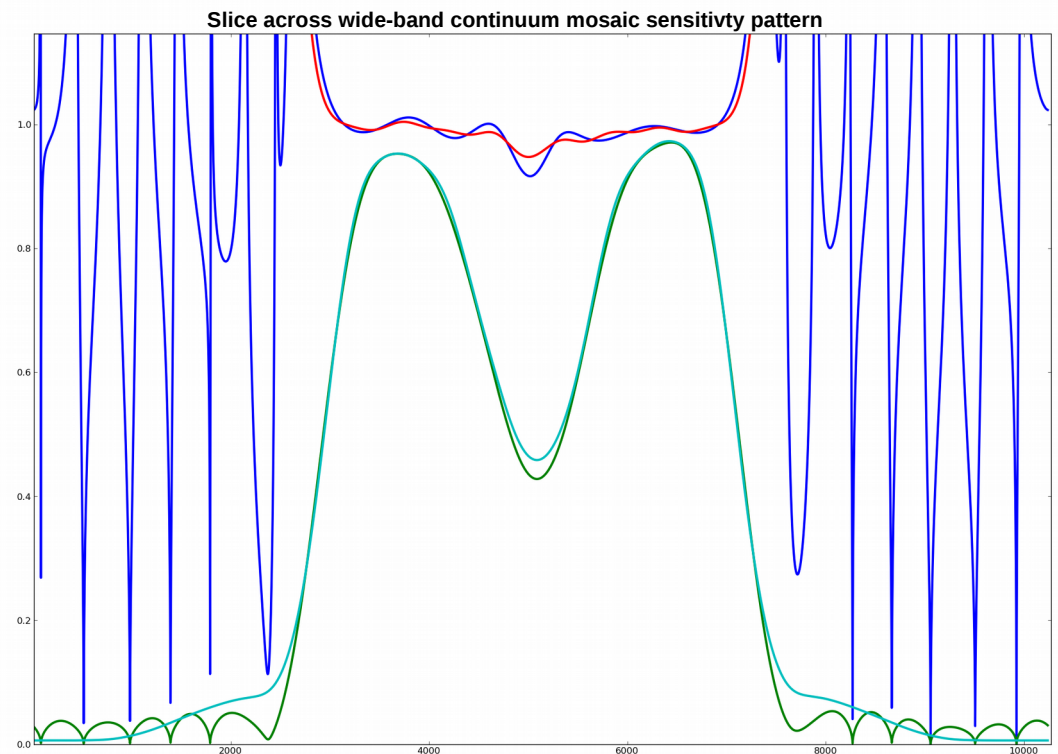
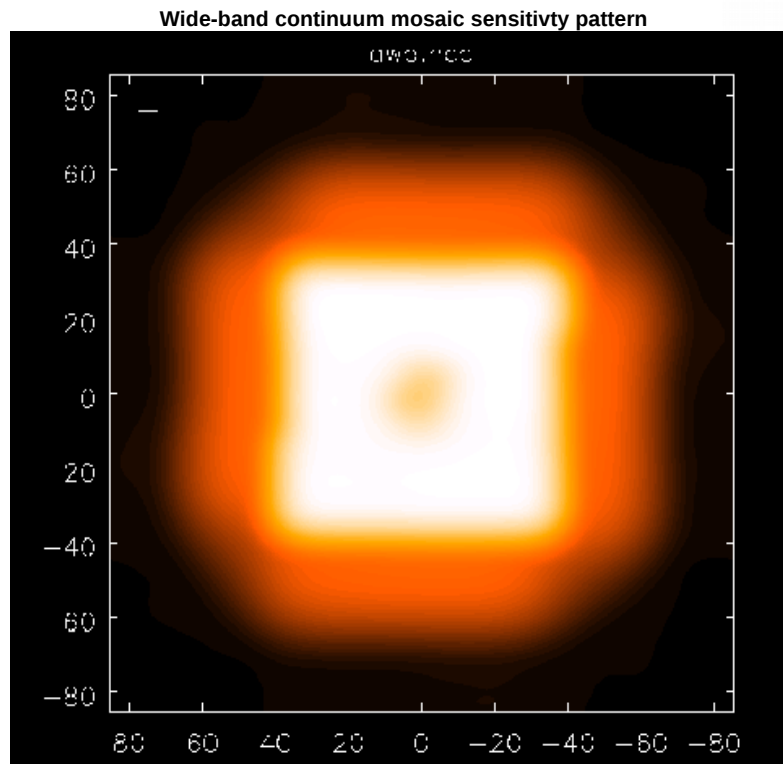


- MT-MFS for sky
  - Reconstructed spectral index increases with distance from the center without PB correction



# Wide-band sensitivity pattern

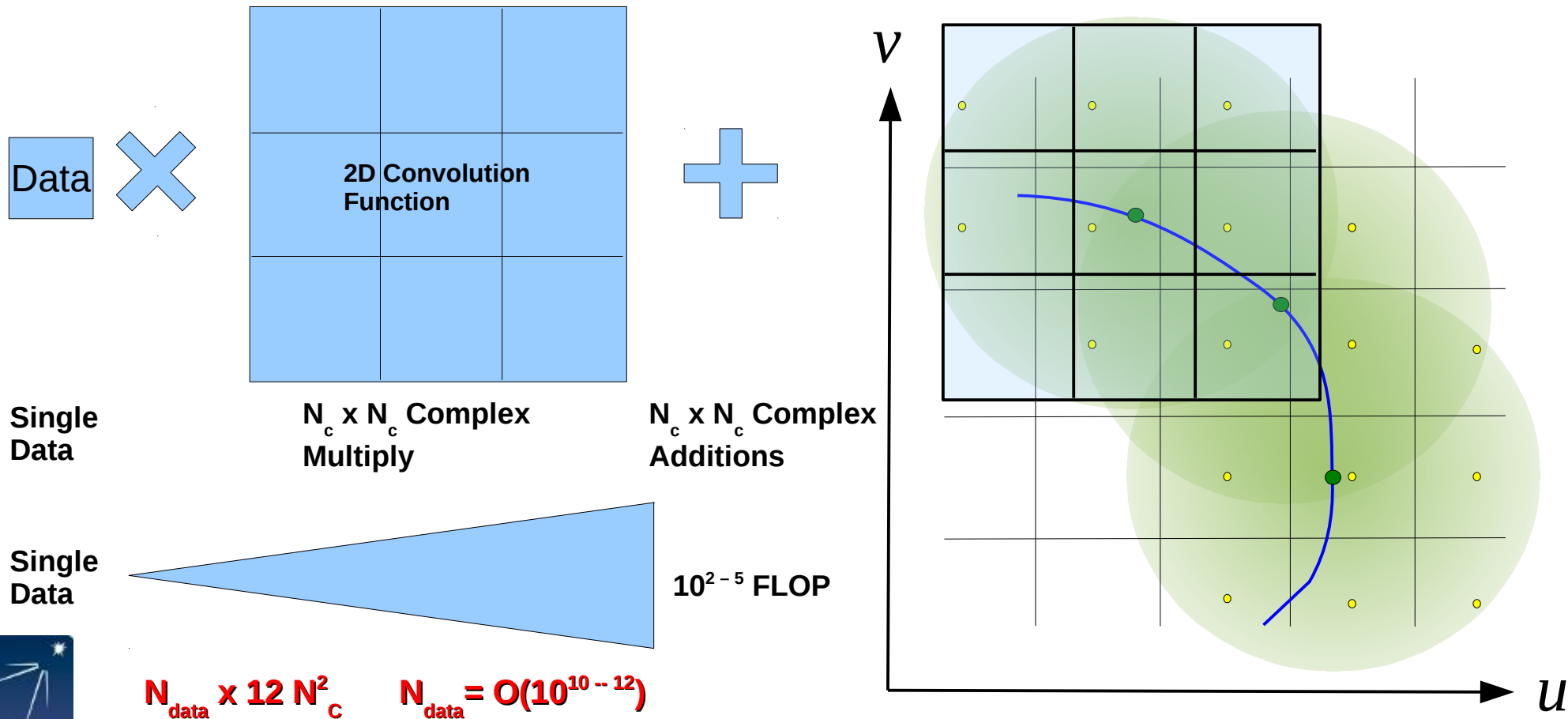
- Wide-band mosaic continuum sensitivity pattern



- Red and light green curves are from AWP gridded
- Blue and dark green curves are from mosaic gridded
- Red and blue curves are ratio of PB with conjbeams=True and conjbeams=False

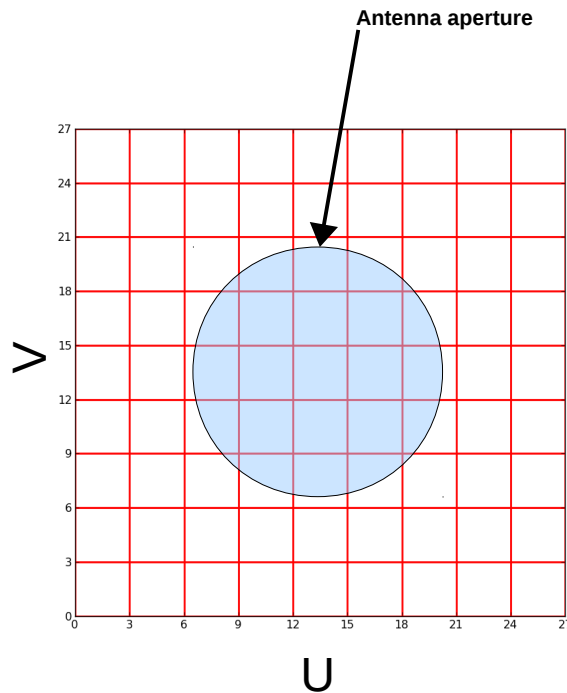
# Gridding: Computations

- Gridding/de-gridding: 2D interpolation via convolutional resampling
- 2D convolution functions  $\leftrightarrow$  2D weighting functions

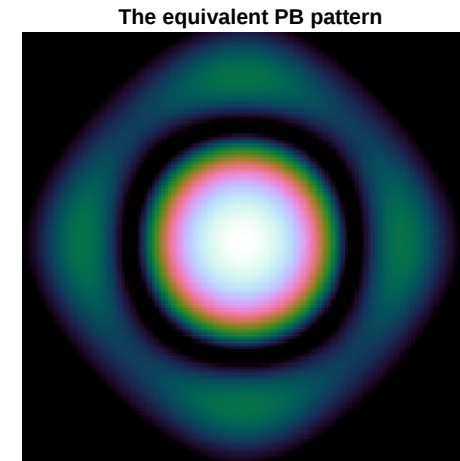


# WF imaging: A-Projection

- WF imaging needs larger convolution functions (CF)



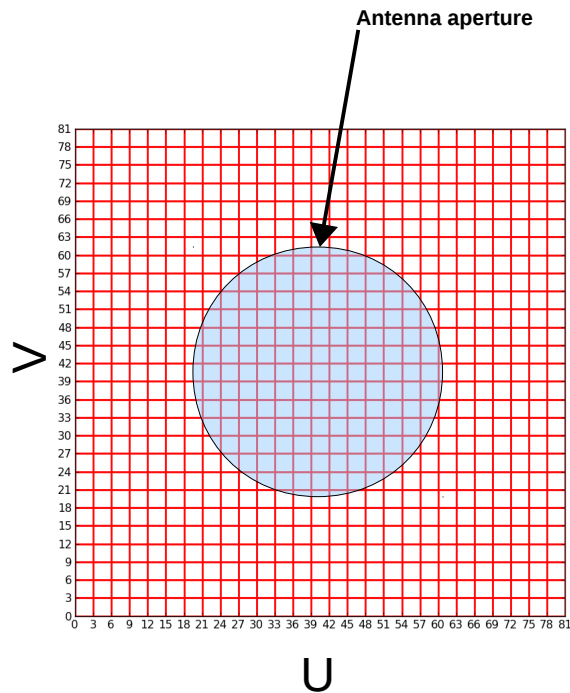
Number of uv-pixel  
across antenna aperture



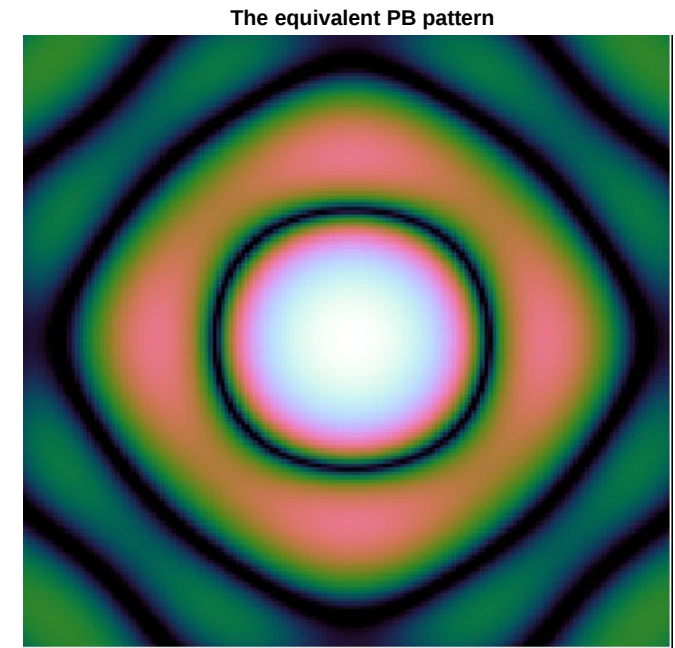
Include the first sidelobe (few%)

# WF imaging: A-Projection

- WF imaging needs larger convolution functions (CF)



Number of uv-pixel  
across antenna aperture



..beyond the first sidelobe

# Imaging Memory footprint

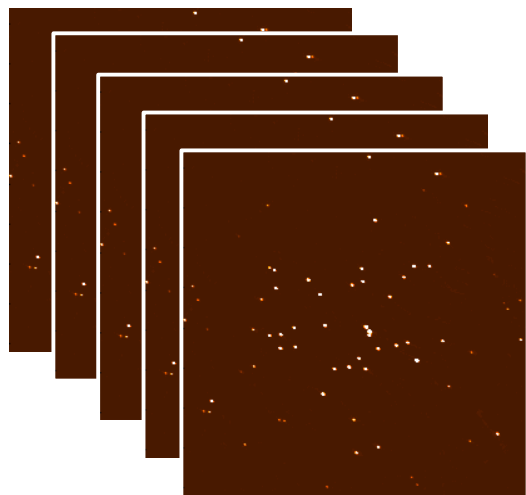
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- Each sky-image of size  $N_x \times N_y$  requires
  - $2 \times \text{Complex} \times (N_x \times N_y) + (N_x \times N_y) = \mathbf{5 \times (N_x \times N_y) \text{ floats}}$

# Imaging Memory footprint

- Each sky-image of size  $N_x \times N_y$  requires
- $2 \times \text{Complex} \times (N_x \times N_y) + (N_x \times N_y) = \mathbf{5 \times (N_x \times N_y) \text{ floats}}$

Mem. Buffers during  
gridding



Imaging



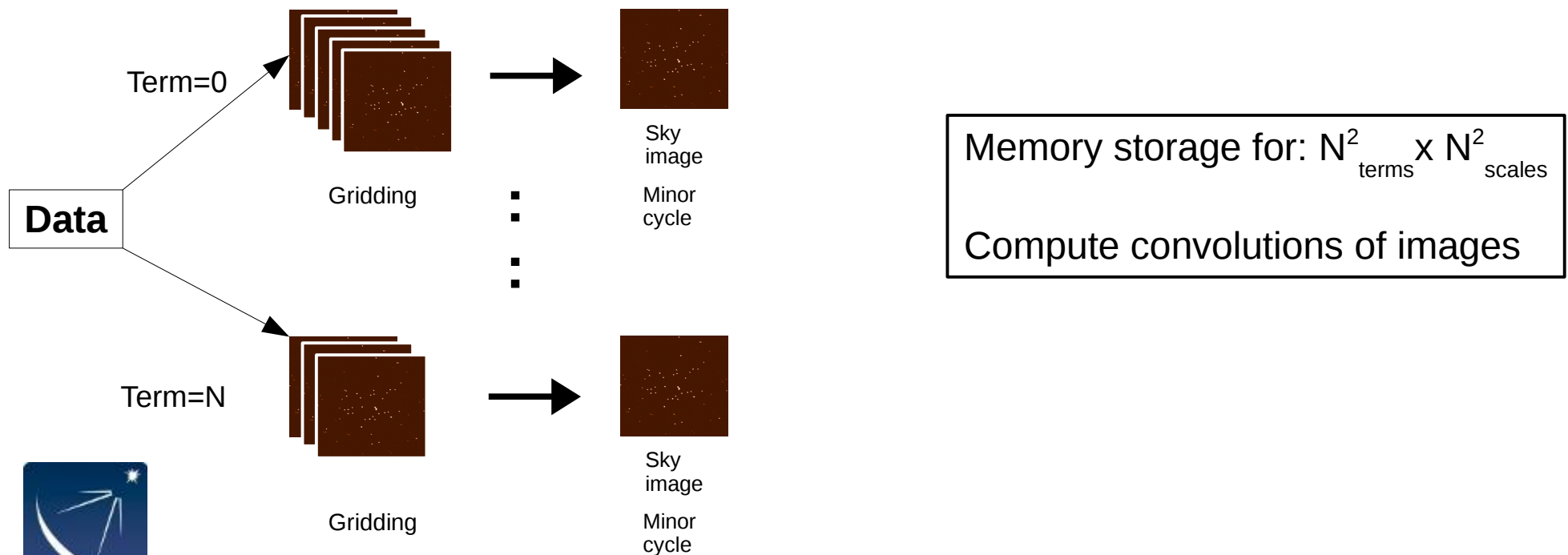
Sky image

Major cycle

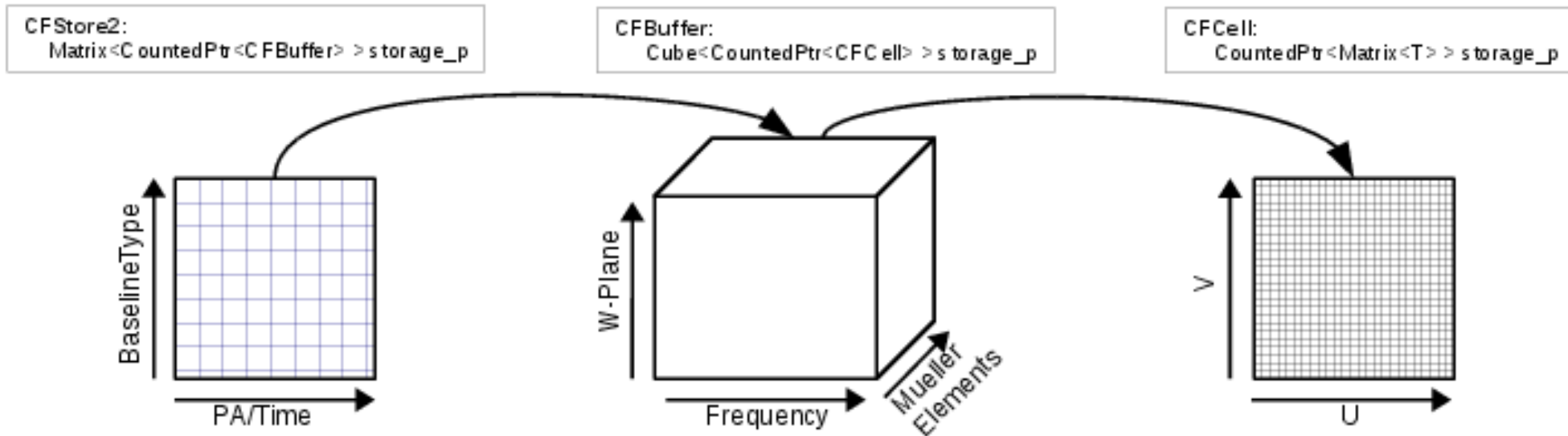
Minor cycle

# MT-MFS: Higher memory footprint

- WB A-Projection:  $N_A \times N_{SPW}$  (order 10x increase in CF memory footprint)
- MS-MFS
  - **Compute load:** Gridding for  $N_{\text{terms}}$  images+ Convolution of large images
  - **Memory:** Multiple minor-cycle images ( $N_{\text{scales}}$ )
  - **Total images (each of size  $N_x \times N_y$ ):**  $N_{\text{terms}}^2 \times N_{\text{scales}}^2$



# Convolution Functions



- WB AW-Projection needs  $2 \times 2 \times N_w \times N_{SPW}$  complex-valued functions
- $N_{SPW} = 16$ ,  $N_w = 128$ . Total CFs = 8K.
- Saved in a CFCache on the disk.
- Size:  $(\text{SupportSize})^2 \times \text{Oversampling} \times 2 \times \text{SizeOfFloat}$ 
  - $[4 - O(100)]^2 \times 20 \times 2 \times 4 \times N_{CF}$  bytes =  $O(15\text{-}20\text{GB})$  per SPW

# Convolution Functions

```
CASA <6>: execfile("/users/sbhatnag/Scripts/checkcfc.py")
```

```
CASA <7>: checkcfc('cfcache.prediction.im10000conjbeams.True', 16, 64)
```

```
0| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 6 6 7 7 8 8 9 9 10 10 11 11 12 12 12 12 13 13 14 12 14 14 15 16 17 17 18 19 19 20 21 22 23 23 24 25 26 27 28 28 29 30 Total lazy-fill size: 439982836.0 B 13516
1| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 6 7 7 7 8 8 9 10 10 11 11 12 12 13 13 12 13 13 14 14 15 15 16 16 17 18 18 19 20 21 21 22 23 24 24 25 26 27 28 29 Total lazy-fill size: 411898444.0 B 12467
2| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 6 7 7 7 8 8 9 10 10 11 11 12 13 13 13 13 13 14 14 15 15 16 16 17 17 18 19 19 20 21 22 22 23 24 25 25 26 27 Total lazy-fill size: 383527380.0 B 11441
3| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 6 7 7 7 8 8 9 10 10 11 11 12 12 13 14 13 13 13 14 14 15 15 16 16 16 17 17 18 19 19 20 21 21 22 23 24 24 25 26 Total lazy-fill size: 361747036.0 B 10711
4| 4 4 4 4 4 4 4 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 6 7 7 7 8 8 9 10 10 11 11 12 12 13 13 14 14 15 14 14 14 15 16 16 17 17 17 18 18 19 20 20 21 22 22 23 24 25 Total lazy-fill size: 346504332.0 B 10125
5| 4 4 4 4 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 10 10 11 11 12 12 12 13 13 14 14 15 14 14 14 15 16 16 17 18 18 18 19 19 20 21 21 22 23 23 Total lazy-fill size: 328226964.0 B 9529
6| 4 4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 10 10 11 11 12 12 13 13 14 15 15 16 16 16 16 17 17 18 18 19 19 20 19 20 21 21 22 23 Total lazy-fill size: 333836556.0 B 9667
7| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 10 10 11 11 12 12 13 13 14 14 15 16 16 17 17 17 17 18 18 19 19 20 20 20 21 22 Total lazy-fill size: 324689972.0 B 9350
8| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 9 10 10 11 11 12 12 13 13 14 14 15 16 16 17 17 17 17 18 18 19 19 20 20 21 21 Total lazy-fill size: 319928364.0 B 9169
9| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 9 10 10 11 11 12 12 13 13 14 14 15 16 17 17 18 18 19 18 18 19 19 20 20 21 21 Total lazy-fill size: 316565412.0 B 9074
10| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 9 10 10 11 11 12 12 13 13 14 14 15 16 16 17 17 18 18 19 18 18 19 19 20 20 21 Total lazy-fill size: 311490780.0 B 8873
11| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 9 10 10 10 11 11 12 13 13 14 14 15 15 16 16 17 17 18 18 19 19 20 19 18 19 19 20 20 Total lazy-fill size: 308449676.0 B 8785
12| 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 6 6 7 7 7 8 8 8 9 9 10 10 10 11 11 12 12 13 13 14 14 15 16 16 17 17 18 18 19 19 20 20 21 20 20 19 20 Total lazy-fill size: 313597148.0 B 8926
13| 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 7 7 7 7 8 8 8 9 9 9 10 10 10 11 11 12 12 13 13 14 14 15 16 16 17 18 18 19 20 20 20 21 21 22 21 Total lazy-fill size: 318544796.0 B 9096
14| 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 7 7 7 7 8 8 8 9 9 9 10 10 10 11 11 12 12 13 13 14 15 15 16 17 17 18 19 20 19 20 20 21 21 22 Total lazy-fill size: 309371412.0 B 8804
15| 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 7 7 7 7 8 8 8 9 9 9 10 10 10 11 11 12 12 13 13 14 14 15 16 16 17 18 18 19 20 21 21 20 21 21 Total lazy-fill size: 306764828.0 B 8708
Total CFC size: 5435125936.0 B
```

```
CASA <8>:
```

- Peak CFC memory footprint: Max. of the “lazy-fill size”

- Compute load scaling  $\sum_{w,v} N_{vis}(w,v) \times N_{support}^2(w,v)$

- The second number is  $\sum_w N_{support}^2(w,v)$



# tclean interface

```

gridder      = 'awproject'      # Gridding options (standard, wproject, widefield, mosaic, awproject)
wprojplanes  = 1                # Number of distinct w-values for convolution functions
normtype     = 'flatnoise'      # Normalization type (flatnoise, flatsky, pbsquare)
psterm       = False           # Use prolate spheroidal during gridding
aterm        = True            # Use aperture illumination functions during gridding
cfcache      = 'cube_8K.cf'     # >Convolution function cache directory name
computeastep = 360.0            # At what parallactic angle interval to recompute AIFs (deg)
rotateastep  = 360.0            # At what parallactic angle interval to rotate nearest AIF (deg)
wbawp        = True            # Use wideband A-terms
conjbeams    = False           # Use conjugate frequency for wideband A-terms
pblimit      = 0.001           # >PB gain level at which to cut off normalizations

```

- **cfcache**: Name of the disk CFCache. CF computation is triggered if CFC is not found (or is empty?). *w* and freq quantization, *aterm*, *psterm*, *computeastep*, *conjbeams* settings determined from existing CFC.
  - Can be reused for the same *imsize*, *cellsize*, and the above parameters are unchanged.
    - **Code will not detect an invalid CFC.**
- **aterm, psterm, wprojplanes**: In general,  $CF = PS * A * W$

Operation	aterm	psterm	wprojplanes	CF
AW-Projection	True	True False	>1	PS*A*W A*W
A-Projection	True	True False	1	PS*A A
W-Projection	False	True	>1	PS*W
Standard	False	True	1	PS

- **At least one out of *aterm* and *psterm* needs to be set to True**

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```

- **conjbeams**: Correct for frequency dependence of the PB
  - Use the A-term at  $\mathbf{v}^* = \sqrt{2\mathbf{v}_{ref}^2 - \mathbf{v}^2}$  when imaging data at  $\mathbf{v}$ 

$$I(\mathbf{v}) = F \sum_{\mathbf{v}} A^{M^T}(\mathbf{v}^*) * V^{obs}(\mathbf{v}) = F \sum_{\mathbf{v}} A^{M^T}(\mathbf{v}^*) * A^o(\mathbf{v}) * V^o(\mathbf{v})$$
- **wbawp**: Computes one CF per SPW if set to True. Else one CF for the entire band.
  - **When wbawp=False, conjbeams setting is irrelevant.**
- **computeastep**: PA-step to trigger computation of a new CF-cube (w,freq,Pol).
  - Value of 360 ==> Compute for only the first PA value
- **rotateastep**: PA-step to trigger in-memory rotation of the PA-cube.
  - Value of 360 ==> never rotate
  - Trade-off between computation vs CFC size



# tclean interface

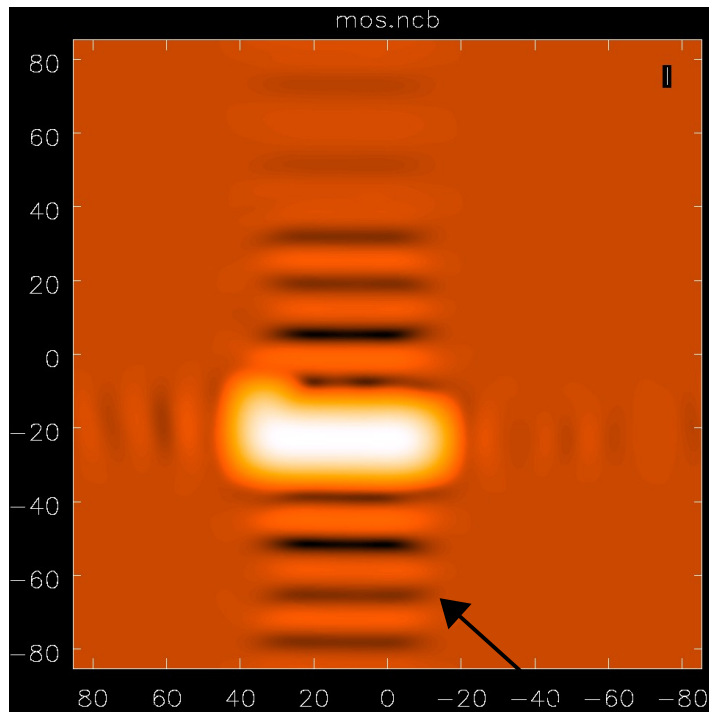
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conjbeams    = False           # Use conjugate frequency for wideband A-terms
pblimit      = 0.001           # >PB gain level at which to cut off normalizations
  
```

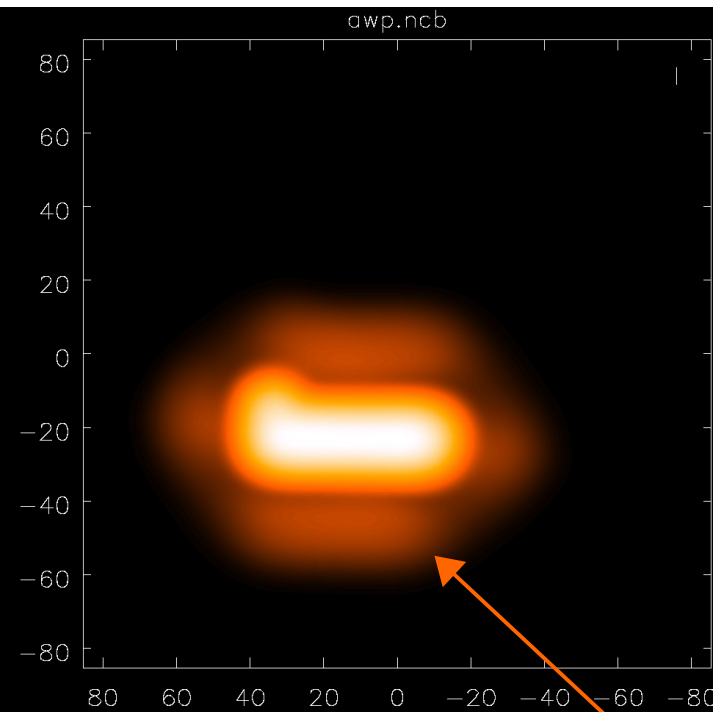
- **pblimit:** PB model (the *.pb.tt0* image) considered to be consistent with zero when the  $\text{gain} < \text{pblimit}$ . Sky images masked where  $\text{PB gain} < \text{pblimit}$ .
  - PB model = FT [ CF \* CF ]
  - With only PS term, a circular footprint is not indicative of antenna PB mask
- **normtype:** 
$$I = \frac{\sum_{\nu} [P^M(\nu^*) P^o(\nu) I^{\text{sky}}(\nu) + P^M(\nu) n]}{\text{Norm}}$$
 where  $P^M(\nu)$  is the frequency dependent PB model
  - “flatsky”:  $\text{Norm} = \sum_{\nu} P^M(\nu^*) P^M(\nu)$  [Norm is saved in the *.weight* image in a *tclean* run]
  - “flatnoise”:  $\text{Norm} = \sqrt{\sum_{\nu} P^M(\nu^*) P^M(\nu)}$

# Aliasing and ringing

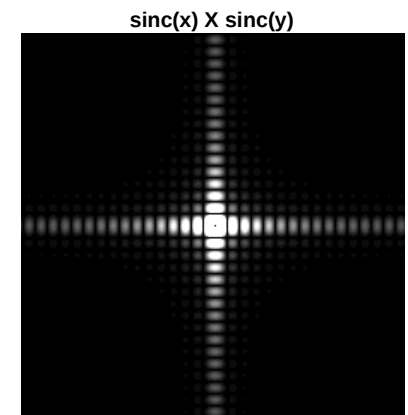
- Sharp cut-off of the CF leads to ringing in the image domain
  - $(\text{True PB}) * [\text{sinc}(x) \times \text{sinc}(y)]$



Not PB sidelobes!

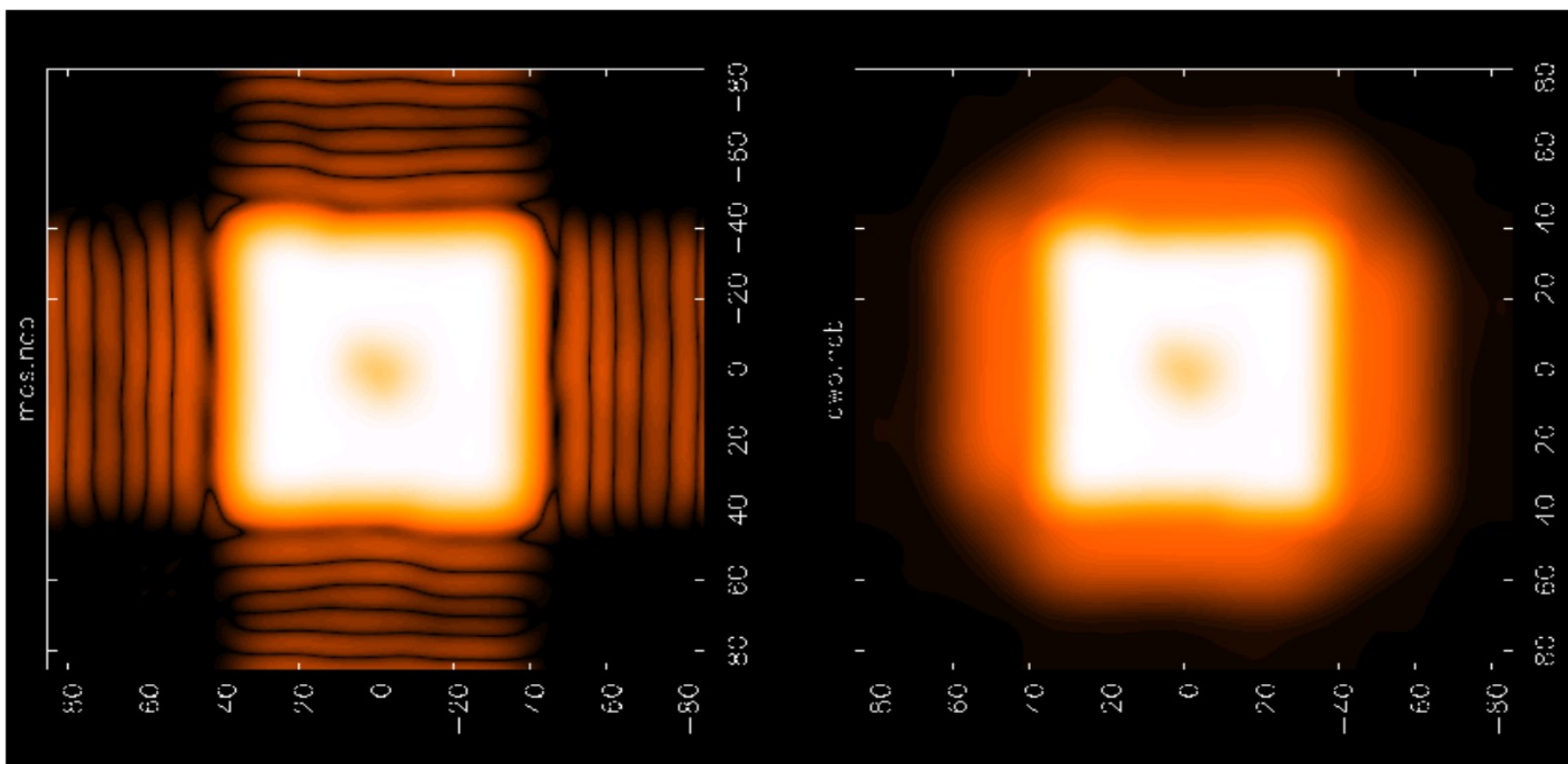


PB sidelobes



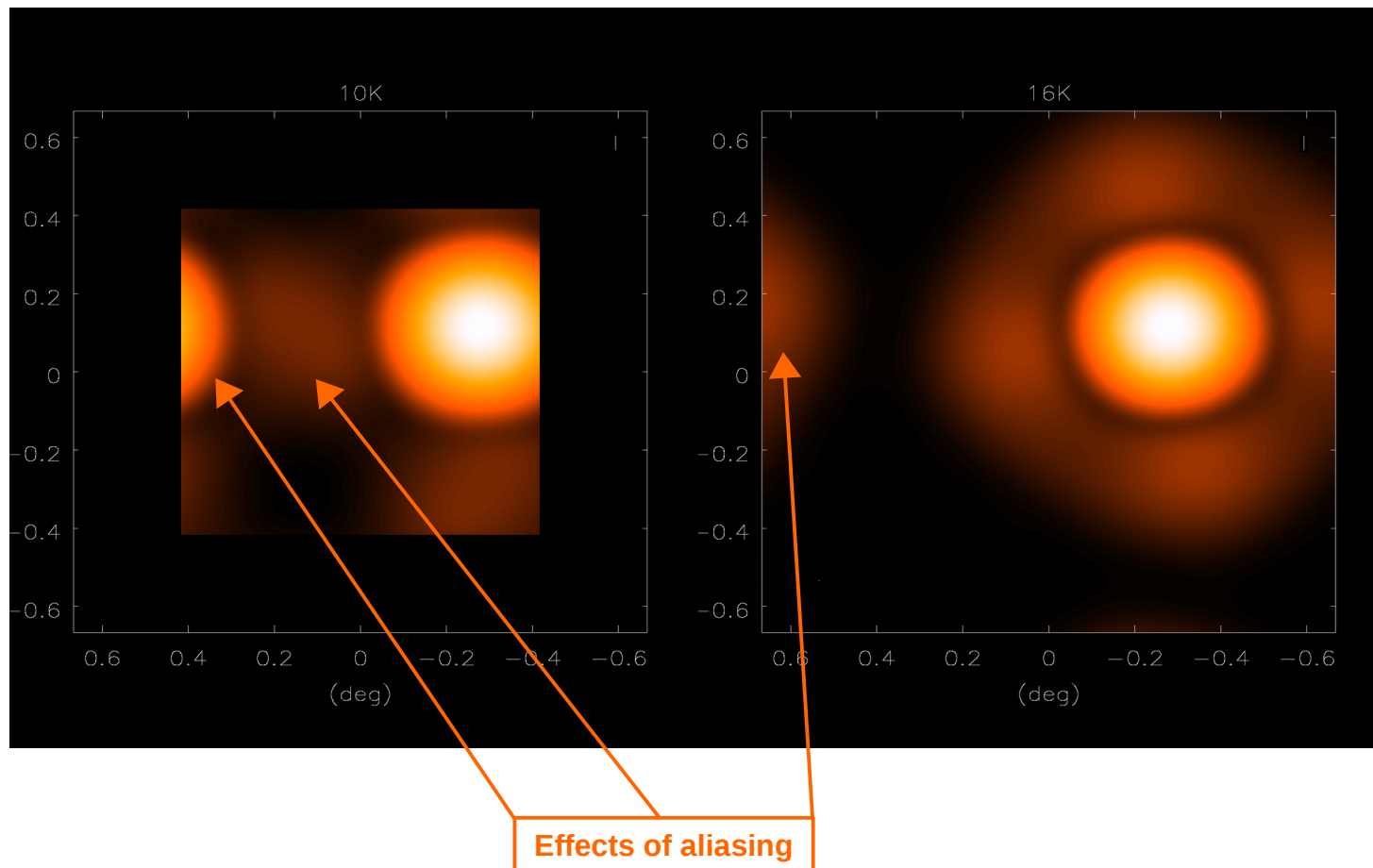
# Aliasing and ringing

- Sharp cut-off of the CF leads to ringing in the image domain
  - $(\text{True PB}) * [\text{sinc}(x) \times \text{sinc}(y)]$



# Aliasing and ringing

- Sidelobes of the WB PB alias back on the opposite side from an edge pointing if the image size is not large enough.
  - Sources in the aliased regions will lead to deconvolution divergence

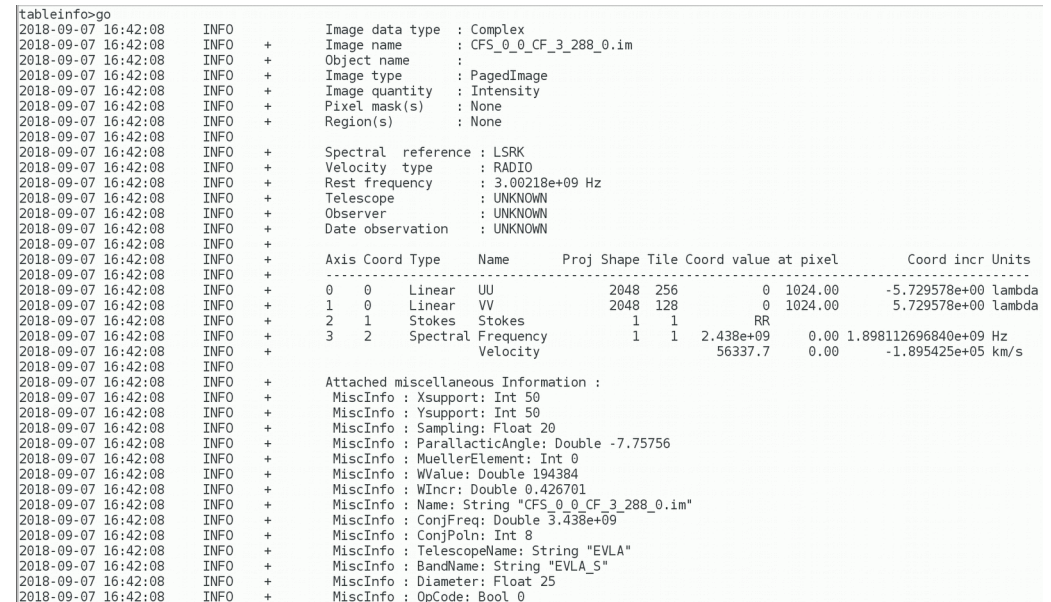


# *tclean* interface

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- Hidden/internal parameters. Controlled via `~/.aipsrc` or `~/.casarc`
  - Can be controlled via similarly named environment variables (but there is a bug!)
- *Aterm.CONVSIZE:*            *Default = 2048*
  - Size of the internal buffer used to compute the CFs
  - Increasing it will increase CFC computation time
- *Aterm.OVERSAMPLING:*    *Default = 20*
  - Oversampling used for computing CFs
  - Larger value improves accuracy, run-time for building CFC and CFC memory footprint
  - When used as W-Projection-only, OS=4 to match *gridder='wproject'*
- *CFCach.LAZYFILL:*            *Default = 1*
  - Activate CF garbage collection/paging
  - Empty the in-memory CFC when data from a new SPW is encountered

- Hold 2D complex-valued CF for all W, Freq., Polarizations, PA and Baseline type. Also holds CFs for computing the weighted sensitivity pattern



- Actual values written in the image header and *MiscInfo* database in the images



# The CFCache

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- CFC is re-usable. For VLASS-style imaging, can be computed once.
- Can be computed with *parallel=True*
  - Serial:
    - Does a dry-run to determine (a) number of CFs and (b) their parameters
    - Writes them as 2x2 pixel images in the on-disk CFC
  - Parallel:
    - Divide the total CFs equally among the parallel processes
    - Each process computes its share of CFs
    - Currently each process holds its share of CFs in memory till it finishes.
  - Example:
    - Computed 32K CFs in ~1hr using 98 processes on the cluster
- To-Do
  - Fix the bug for *specmode='cube'* and *chanchunks > 1*
  - Allow using smaller wprojplanes than what's in the CFC
  - Allow use of existing read-only CFC
  - More aggressive CFC garbage collection
  - Automatically adjust *Aterm.CONVSIZE* parameter
  - Separate PS from the .pb image. The latter is used for making PB-corrected final images.

