### **GPU** based imager for radio astronomy

#### GTC2014, San Jose, March 27<sup>th</sup> 2014





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### Introduction

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  - Algorithms R&D Scientist at the National Radio Astronomy Observatory, Socorro, New Mexico



- Motivation:
  - Deploy all compute-intensive imaging operations on the GPU
  - Why? How? Listen on...

### **Overview of the talk**

- Introduction to NRAO
   What is it? Why it is?
- Quick intro. to the scientific projects that pose the HPC problem

- Overview of RA imaging
  - What is needed for imaging with current & future telescopes

- Details of the current hot-spots
  - Motivate the three Proof-of-Concept (PoC) projects
  - Progress so far, future plans



### **National Radio Astronomy Observatory**

- A NSF funded national observatory
- To build and operate large radio facilities
  - Operate three of the largest ground-based radio telescopes
    - » EVLA, ALMA, VLBA, GBT
  - Central Development Lab (CDL):
  - Digital Correlators for EVLA, ALMA, VLBA; digital back-end for the GBT
  - Off-line software for calibration, imaging and astronomical computing
    - » Open source
    - » Most widely used RA imaging software world-wide
    - » Runs on laptops, desk-tops, Compute Clusters
    - » Now exploring using GPUs to mitigate compute and memory footprint hotspots



### The Very Large Array (NM, USA)



- Very Large Array
- 27 antennas
- Antennas movable on rails 1 – 27 Km radius
- Spread over 27 Km radius
- Size of the "lens"
   30 Km
- Frequency range 300 MHz – 50 GHz

### Atacama Large MM Array (ALMA), Chile



- In partnership with EU & Japan
- •At an altitude of 16,500 ft
- 50 antennas
- Effective size of the lens: 3 Km
- Frequency range 100 GHz – 950 GHz
- Re-configurable with antennas movable on a special transporter.



### Very Long Baseline Array (VLBA), US



- 10 antennas
- Antennas across the US
- Size of the "lens" few 1000 Km
- Frequency range 100 GHz – 950 GHz
- Angular resolution milli arcsec



### **Other RA Observatories in the world**



### **Other RA Observatories in the world**



### Interferometric Imaging: Big Data

• Uses the technique of Aperture Synthesis to synthesize a "lens" of size equal to the maximum separation between the antennas

• Not a direct imaging telescope: Data is in the Fourier Domain

• Image reconstruction using iterative algorithms

Data volume with existing telescopes : 10 – 200 TB
 with SKA Telescope: Exa Bytes

Effective data i/o for image reconstruction: 10x



- Sensitivity improvements of 10x or more in modern telescopes
  - What was an ignorable/too weak an effect earlier, now limits the imaging performance of modern telescopes

- Need more compute-intensive imaging algorithms
  - Tera/Peta Flops now. Exa Flops SKA (soon....ish)

• Orders of magnitude more expensive algorithms for imaging using many orders of magnitude more data



Imaging algorithms in CASA for EVLA and ALMA The "aw-imager" for LOFAR (NL) – a modified version of CASA Imager ASKAP Imager (AU) optimized for large cluster computing

- Bottom line for computing
  - Tera Exa(SKA) scale computing using Tera Exa(SKA) Bytes of data to make Giga-Pixel images

• Full end-to-end processing will require a cluster



### **Computing hot spots**

- Gridding / de-gridding:
  - Irregularly sampled data to a regular grid for FFT
- Computing Convolution Functions (CF):
   PoC 2
  - Computing convolution kernels for Gridding
    - » Pre-compute-n-cache OR On-demand computing
    - » Memory foot print issues

- Wide-band Image Reconstruction:
  - Requires convolutions of many large images
    - » Pre-compute-n-cache OR
    - » On-demand Computing using GPU



PoC - 1

PoC - 3

# **Scientific projects: Deep Imaging**

- Requires high resolution, high dynamic range imaging
  - i.e. Big Data
  - Compute-intensive algorithms
- Large area surveys of the radio sky



- Dynamic range
  - Ratio of strongest to weakest Source: 10<sup>6</sup>
  - Dynamic range of raw images  $10^{2-3}$
- Need high resolution to reduce background sky-noise ("confusion noise")





# **Scientific projects: Deep Imaging**

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### Scientific projects: Fast Imaging

- Transient sky
  - Storing data at high time resolution for later processing is not an option
  - Needs fast (near real-time) imaging  $\rightarrow$  as a trigger to store busts of data



- A short blip in time
  - Spike of ms in 10s of hours of data
- Data rate too high to be recorded at ms resolution
- Need fast imaging as a trigger to record short busts of data
- Need interferometric imaging to localize on the sky



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ms

- Single dish Resolution too low for many scientific investigations
  - Limited collecting area + resolution limits sensitivity at low frequencies



Single dish resolving power *Wavelength* Dish Diameter

#### Biggest steerable single dish = 100 m





- Single dish Resolution too low for many scientific investigations
  - Limited sensitivity/limits sensitivity at low frequencies



Synthesis Array resolving power *Wavelength* Max. separation between antennas

Max. separation in VLA = 35 km

#### Resolution: ~ 350x better





- Aperture Synthesis or Fourier Synthesis technique
  - An interferometric imaging technique (Nobel Prize in '74)

Each pair of antennas measure **one** Fourier Component

Many antennas separated by 10s – 100s Km







- Synthesized aperture equal to the largest separation between antennas
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- Aperture Synthesis
  - An interferometric imaging technique (Nobel Prize in '74)
  - Many antennas separated by 10s 100s Km
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  - An interferometric imaging technique (Nobel Prize in '74)
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- Synthesized aperture equal to the largest separation between antennas

- Aperture Synthesis
  - An interferometric imaging technique (Nobel Prize in '74)

**All** pairs with **one** antenna measure N-1 Fourier Component = 26

Many antennas separated by 10s – 100s Km







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- Aperture Synthesis
  - An interferometric imaging technique (Nobel Prize in '74)
  - Many antennas separated by 10s 100s Km
  - All pairs with all antenna measure N(N-1)/2 Fourier Component = 351







- Synthesized aperture equal to the largest separation between antennas
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- Aperture Synthesis
  - Use **Earth Rotation Synthesis** to fill the Fourier plane
  - **All** pairs with **all** antenna measures N(N-1)/2 Fourier Component
  - Measure N(N-1)/2 x 2 Fourier components over 2 integration time = 702







- Synthesized aperture equal to the largest separation between antennas

- Aperture Synthesis
  - Use **Earth Rotation Synthesis** to fill the Fourier plane
  - **All** pairs with **all** antenna measures N(N-1)/2 Fourier Component
  - Measure N(N-1)/2 x 10 Fourier components over 10 integrations = 7020







- Synthesized aperture equal to the largest separation between antennas

- Aperture Synthesis
  - Use **Earth Rotation Synthesis** to fill the Fourier plane
  - **All** pairs with **all** antenna measures N(N-1)/2 Fourier Component
  - Fourier Components measured over 10 hr: **O(10<sup>11-12</sup>)**





Up to Exa Bytes for SKA-class telescopes



- Data Size: 10s 100s TB now
  - Data not on a regular grid.
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- Aperture Synthesis Imaging
  - Indirect imaging: data in the Fourier domain
  - Incomplete sampling  $\rightarrow$  artifacts in the image



• Raw image (FT of the raw data) is dynamic range limited



Dynamic range: > 1 : 1000, 000



Dynamic range: 1:1000

- Processing: Remove telescope artifacts to reconstruct the sky brightness
- Image reconstruction is a High-Performance-Computing-using Big-Data problem



- Image reconstruction is an ill-posed Inverse Problem
  - $\mathbf{D} = \mathbf{A} \mathbf{I}^{\text{true}}$

D: The Raw Data
A: The Measurement Matrix
I<sup>true</sup>: The True Sky Brightness distribution

• Recover I<sup>true</sup> given D

 $\mathbf{A}^{-1} \mathbf{D} = \mathbf{I}^{\text{True}}$ 

- A is singular ==> Non-linear (iterative) algorithms required to reconstruct the Sky Brightness distribution
- Typically 10 iterations, using **ALL** the data in each iteration



Raw Data: 10 – 100 TB Effective data volume: 100 – 1000 TB

# **The Computing Problem**

### Basic computing steps

- 1. Use FFT to transform to the image domain: Gridding + FFT
- 2. Image-plane deconvolution of the PSF :
- 3. Inverse transform to the data domain:

Search and subtract on images De-gridding + Inv. FFT



### **The Computing Problem**

- Basic computing steps
  - 1. Use FFT to transform to the image domain: Gridding + FFT
  - 2. Image-plane deconvolution of the PSF : Search and subtract on images
  - 3. Inverse transform to the data domain:
- Search and subtract on images De-gridding + Inv. FFT
  - 2 Supply Convolution Functions Gridding De-Gridding De-Gridding 1



### **Computing architecture**

- Make images on the GPU
  - Use GPU as a Gridding + FFT server
  - CPU host for image reconstruction





### **Computing architecture**

- Make images on the GPU
  - Use GPU as a Gridding + FFT server
  - CPU host for image reconstruction + GPU as a image convolution server





### **Computing architecture**

- Fast imaging
  - 100s of image in milli seconds on the GPU
  - Search for peak on the GPU
  - If peak found, send a trigger to the host to save the data buffer on the disk





### **The Computing Problem: Why Gridding?**

- Use FFT to transform to the image domain
  - Raw data is not on a regular grid




# **The Computing Problem: Why Gridding?**

Use FFT to transform to the image domain ullet



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# **The Computing Problem: Why Gridding?**

• Use FFT to transform to the image domain

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# **The Computing Problem: Why Gridding?**



- Gridding/De-gridding  $\leftarrow \rightarrow 2D$  Interpolation via convolutional reulletsampling
- Convolution Function  $\leftarrow \rightarrow 2D$  Weighting Function •



- Gridding/De-gridding  $\leftarrow \rightarrow$  2D Interpolation via convolutional resampling
- Convolution Function  $\leftarrow \rightarrow 2D$  Weighting Function



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- Gridding/De-gridding  $\leftarrow \rightarrow$  2D Interpolation via convolutional resampling
- Convolution Function  $\leftarrow \rightarrow 2D$  Weighting Function



- Divide the grid into sub-grids, each with multiple pixels
- Map each sub-grid to a CUDA Block of threads
  - One thread per sub-grid pixel

For each data D<sub>i</sub>

Calculate the range of the CF centered on  $D_i$ If this block in range For all threads in range local\_Grid<sub>j</sub> +=  $D_i * Cf_{i-j}$ Write local Grid to GMEM Grid





For Data 1

Calculate the range of the CF centered on D

this block in range

For all threads in range local\_Grid, += D, \* Cf<sub>i,i</sub>

Write local\_Grid to GMEM Grid



Sub-grids/Blocks of 10x10 threads

For Data 2

Calculate the range of the CF centered on D

this block in range

For all threads in range local\_Grid, += D, \* Cf,

Write local\_Grid to GMEM Grid



Sub-grids/Blocks of 10x10 threads

For Data 3

Calculate the range of the CF centered on D

this block in range For a

Write local\_Grid to GMEM Grid



Sub-grids/Blocks of 10x10 threads

- No thread contentions
  - No atomic-operations required
- But current implementation is limited by global memory accesses

- Solution: reduce GMEM access
  - Coarse-grid the raw data / sort the raw data
  - Copy data required for each block to SMEM
- Cache-coherent access
  - Re-arrange GMEM buffers





# **Convolution Functions (CFs)**

- Convolution Functions encode the physics of the measurement process
- Prolate Spheroidal: As anti-aliasing operator
- W-Term: Account for Frensel Propagation term
- A-Term: Account for antenna optics

Bhatnagar et al. (2008)

Cornwell et al. (2008)

- Final function: Convolution of all three
  - PS \* W-Term \* A-Term
  - N×N = 10×10 few x 100×100

In use in CASA (NRAO), "aw-imager" for LOFAR (NL), ASKAP Imager (AU)









# **Compute CFs on the GPU: PoC - 2**

- CFs as tabulated functions in the computer RAM
- Minimize the quantization errors, by over-sampling
  - Typical over-sampling 10x 100x
- Memory footprint gets prohibitive
  - Total Memory =  $10^{3-8} \times 1000$ s of CF = 10s 100s GB

PoC-2: Can we compute the CF s on-the-fly (as against compute-n-cache)?

– Compute + Multiply + FFT









### Status-1: CF Computations – PoC-2



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### Status-1: Compute CFs on GPU – PoC-2

• Negligible I/O – mostly computing



- GPU: Pre-compute A-Term and cache it in GPU GMEM
  - Compute W-term OTF one thread per pixel
  - Multiple A x W
  - FFT
- Sizes involves: 2K x 2K Complex images
- GPU: 1024 CFs made in ~1 ms.
  - ~20x faster than CPU
  - Room for improvement by another 2 3x





### Image reconstruction: PoC - 3

#### • Simplest algorithm: CLEAN

Iteratively search for the peak in the Raw image and subtract the PSF image at the location of the peak





- Most complex algorithms: Multi-scale Multi-freq. Synthesis (MS-MFS)
  - Requires convolutions of large images +
  - Requires CLEAN
- Use GPU as a convolution-server PoC 3
  - Do deconvolution on the GPU (future)



### Status-2: Image deconvolution – PoC-3

- Wide-band image reconstruction
  - Multi-Term Multi-Scale

$$- N_{terms} = 2 - 3 \qquad N_{scales} = 3 - 10$$

- Computing cost
  - N<sub>terms</sub> gridding cycles
  - Convolutions of  $N^2_{Terms} \times N^2_{scales}$  images
  - Search in N<sub>terms</sub> images





### Status-2: Image deconvolution – PoC-3

- High memory footprint: High resolution wide-band imaging currently not possible
- Solution being pursued
  - Use GPU as an enabler technology (high resolution wide-band imaging)
  - Compute the multi-scale images OTF
  - Use GPU as a convolution-server







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# Low DR, fast imaging needs

- Transient source localization on the sky
  - Data rates too high for store-n-process approach
  - Need fast, low-DR imaging to trigger storage of short busts of data
- EVLA: Data dumps every 5 ms
- Computing
  - Make 119 images (DM search): 1K x 1K size
  - Trigger storage if peak > threshold

- Current CPU based processing (14 nodes x 16 cores)
  - ~ 10x slower than real-time



# Fast-imaging GPU pipeline

- Simplify the gridder
- On-GPU FFT
- On-GPU peak detection
  - If (peak > threshold) trigger data storage

- Compute to I/O ratio ~  $O(10^{5-6})$ 
  - Data (@900MB per sec) goes into the GPU
  - Only trigger info. Comes out



# Fast-imaging GPU pipeline estimates

• Imaging is FFT-limited

- GPU: Gridding + FFT + Peak search
  - Once per  $\sim 1 \text{ ms}$
  - 50 (100x?) faster than single CPU core

- Initial estimates for fast-imaging (work-in-progress):
  - 5 (2?) K20Xs become comparable to 14x16 CPU cores
    - » 10x slower than real-time
  - 50 (25?) K20X GPU cluster can enable real-time processing



# **Conclusions, future work**

- The algorithms for the three hot-spots ported on GPU (the three PoCs)
- Work in progress on the gridding algorithm
  - Minimize Global Memory transactions, other optimizations
  - Take decision about which algorithm to use
- Optimize the CF severe code and image convolution code
- Integrate to make a imaging pipeline
- Scientifically test the results
  - Measure actual run-time performance with real data
- Prototype and check Fast Imaging pipeline
  - If the estimates of run-time improvements hold up, deploy for real-time fast-imaging



# Back up slides



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# **Number of CFs required**

- Not all CF terms can be computed analytically
  - Final convolution function can't be computed analytically



 No. of CF s required for wide-band, full-polarization high-dynamic range imaging is large

Total number of CF s : 10s – 1000s

- Expensive to compute
  - Current solution: Pre-compute and cache
  - Memory Footprint issues





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# **Computing architecture**

- Make images on the GPU
  - Use GPU as a Gridding + FFT server
  - CPU host for deconvolution



• GPU as a Image Convolution + on-demand CF server





# **Computing architecture**

- Make images on the GPU
  - Use GPU as a Gridding + FFT server
  - CPU host for deconvolution
- GPU as an Enabling Technology
  - GPU as a Convolution and Convolution Functions server
  - Where GPU RAM is not sufficient to hold all CF and buffers for MS-MFS
  - Imaging + Deconvolution loops on the Host
- GPU as a trigger for fast-transients
  - 100s of images from a given set of data
  - Image + search for transients on the GPU



# **Aperture Synthesis Imaging: How?**



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# **Aperture Synthesis Imaging: How?**

- Aperture Synthesis
  - An interferometric imaging technique (Nobel Prize in '74)
  - Many antennas separated by 10s 100s Km
  - Each pair of antennas measure **another (one)** Fourier Component







- Synthesized aperture equal to the largest separation between antennas

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# Gridding on the GPU: PoC - 1

• Each data point is multipled by a NxN complex Convolution Function followed by NxN additions to the Global Grid

• 
$$N_{data} \times N_{CF}^2 \times 8 FLOP + overheads$$
  
=  $O(10^{10-12}) \times (10 \times 10) \times 8.2 = 100s TFLOP$   
 $\times (100 \times 100) \times 8.2 = \sim PFLOP$ 



• SKA

 $O(10^{15}) \times ... \times 8.2 = \sim ExaFLOP$ 

- Gridding cost dominates computing load for all imaging
- Compute to I/O ratio: 10<sup>2-5</sup>

Massively Parallel H/W should help: PoC 1





- Gridding / de-gridding:
  - Dominates to cost of High Dynamic Range imaging
- Compute to i/o ratio:  $10^{2-5}$ 
  - Dominant cost for most imaging
  - Wide-band imaging: comparable to the cost of the deconvolution step
- Scaling:
  - Run-time cost: (data volume) x (CF size)
  - W-, AW-Projection:  $10^{12} \times 10^{2-5}$  FLOP
  - A-Projection:  $10^{12} \times 10^{2-3}$  FLOP

- Existing literature
  - GPU: Cornwell et al. (2010), Romien (2012), Daniel Mascot (2014)
    Non-imaging: Margo et al. (2013),
    FPGA: Clarke et al. (2014)





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Gridding

### Status-2: Image deconvolution – PoC-3



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### Status-1: CF Memory footprint – PoC-2

• Negligible I/O – mostly computing



- Tabulated CF requires oversampling to minimize quantization errors
- Memory per CF for high DR imaging with the EVLA:
  - Oversampling: 100; Pixels: 2K x 2K = 8 Mbytes
  - No. of CF s : 100 W-Terms x 100-ATerms =  $10^4$
  - Total memory footprint : 80 GB
- Memory footprint for SKA several orders of magnitude larger



Conv

Sridding → FF
## Status-3: Gridding – PoC-1 (on-going)

- Solutions: Load balancing
  - Non-regular sub-grids





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Gridding

Image

Conv