

NORTH AMERICAN NANOHERTZ OBSERVATORY
for
GRAVITATIONAL WAVES

Pulsar Timing Arrays and the Low-Frequency Gravitational Wave Sky

Michael T. Lam

NRAO Synthesis Imaging Workshop – 21 May 2024





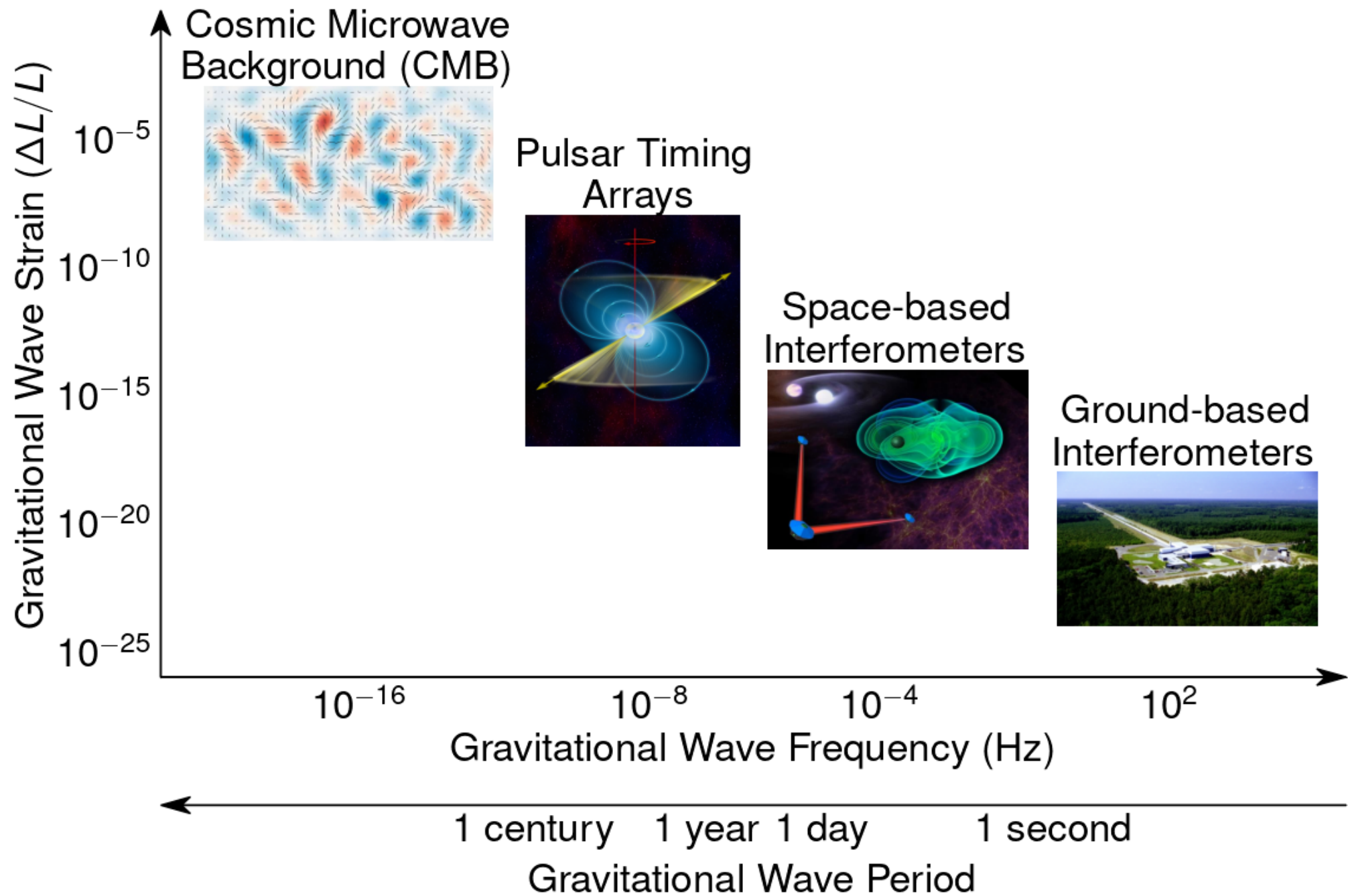
McGill



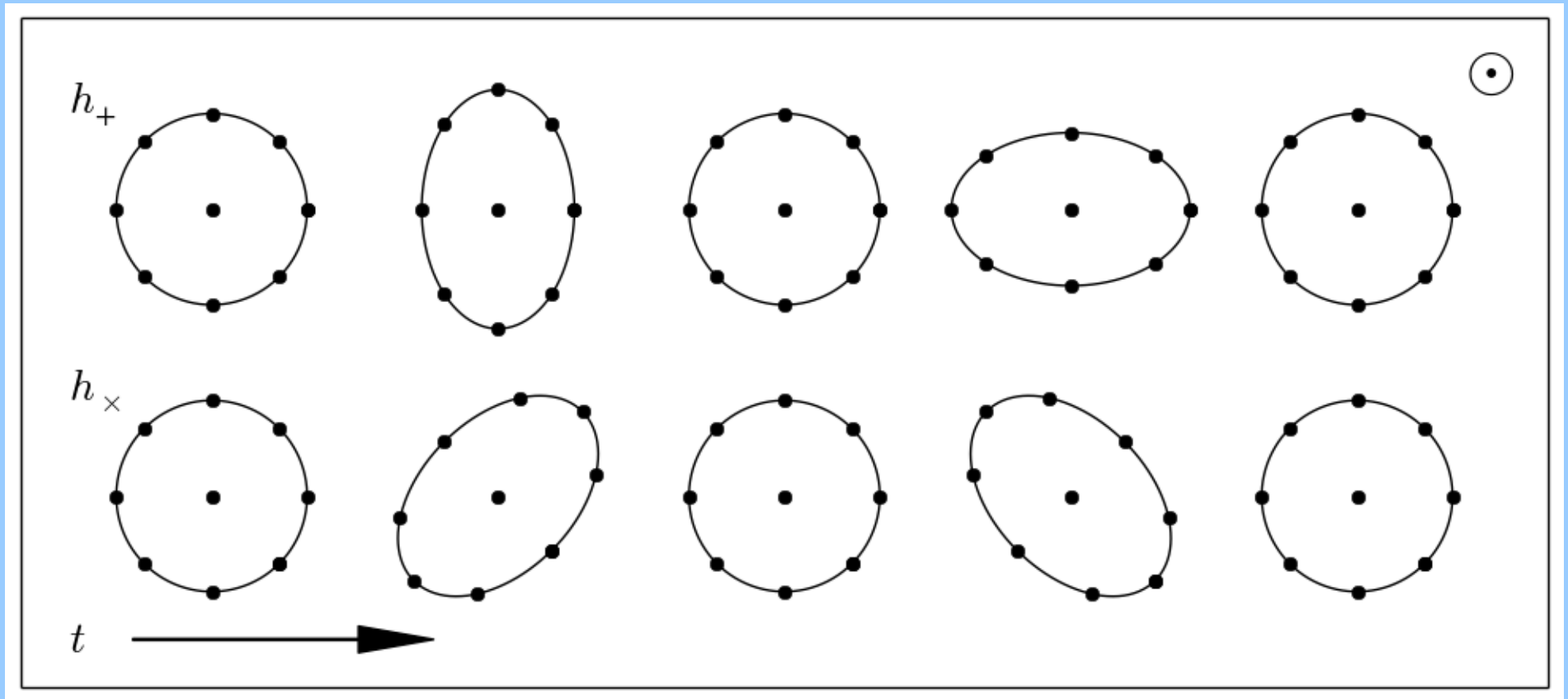
LAFAYETTE
COLLEGE



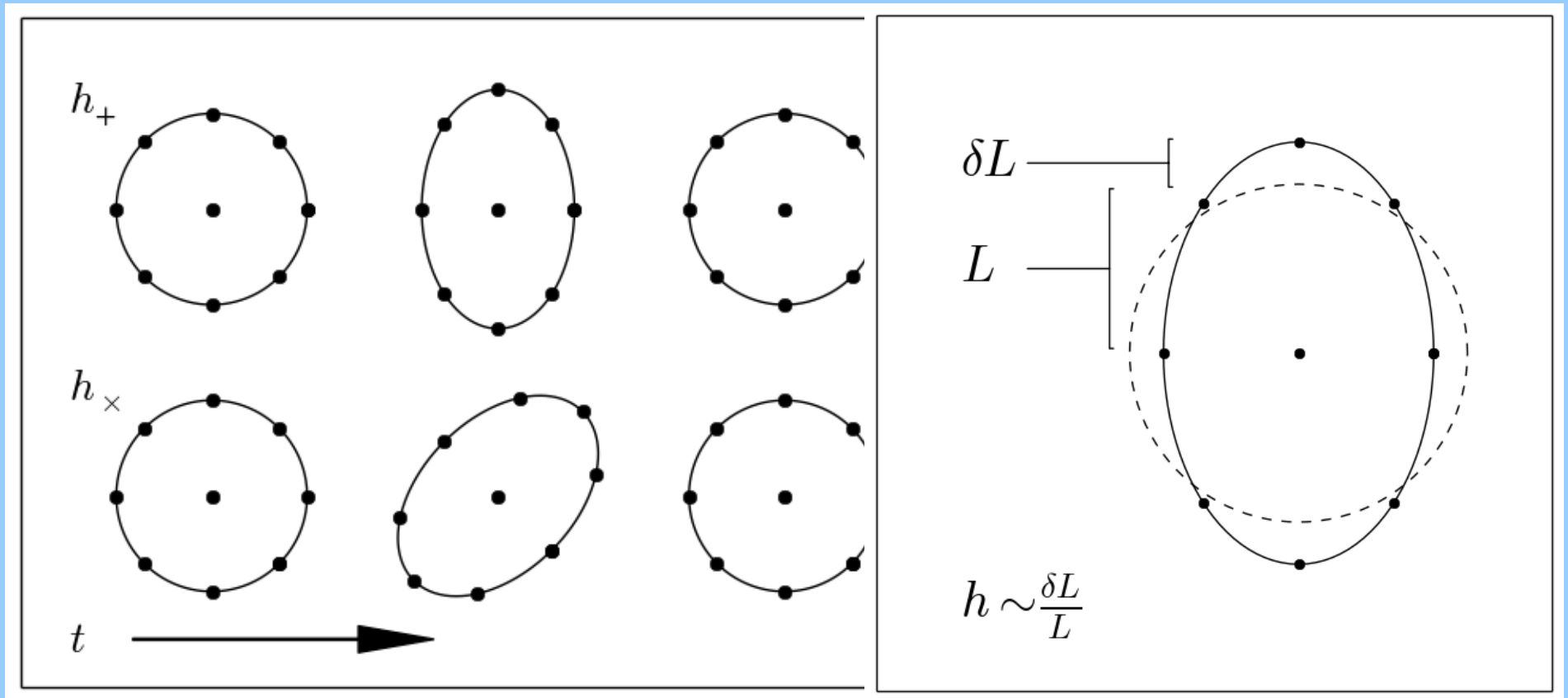
L, M: NRAO/AUI, R: NAIC



Effects of Gravitational Waves

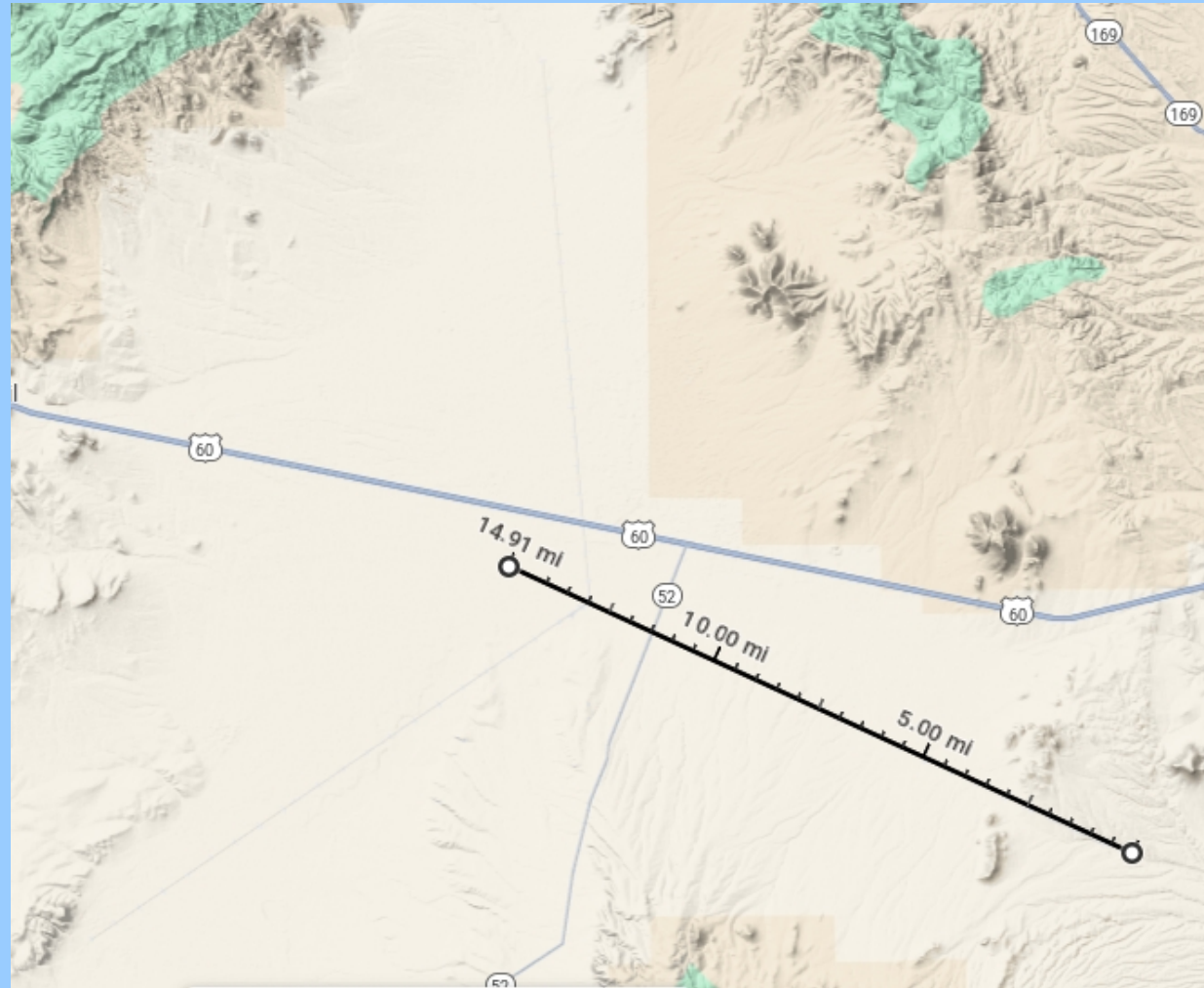
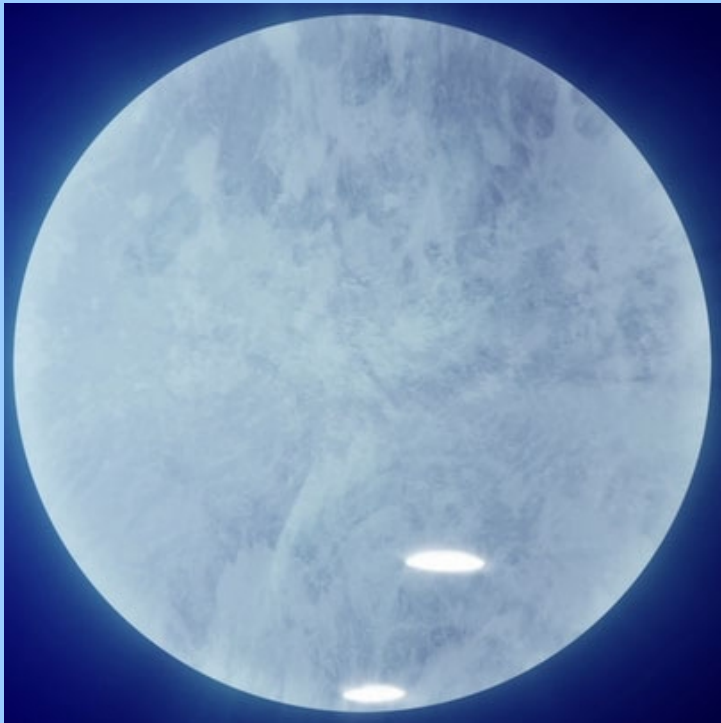


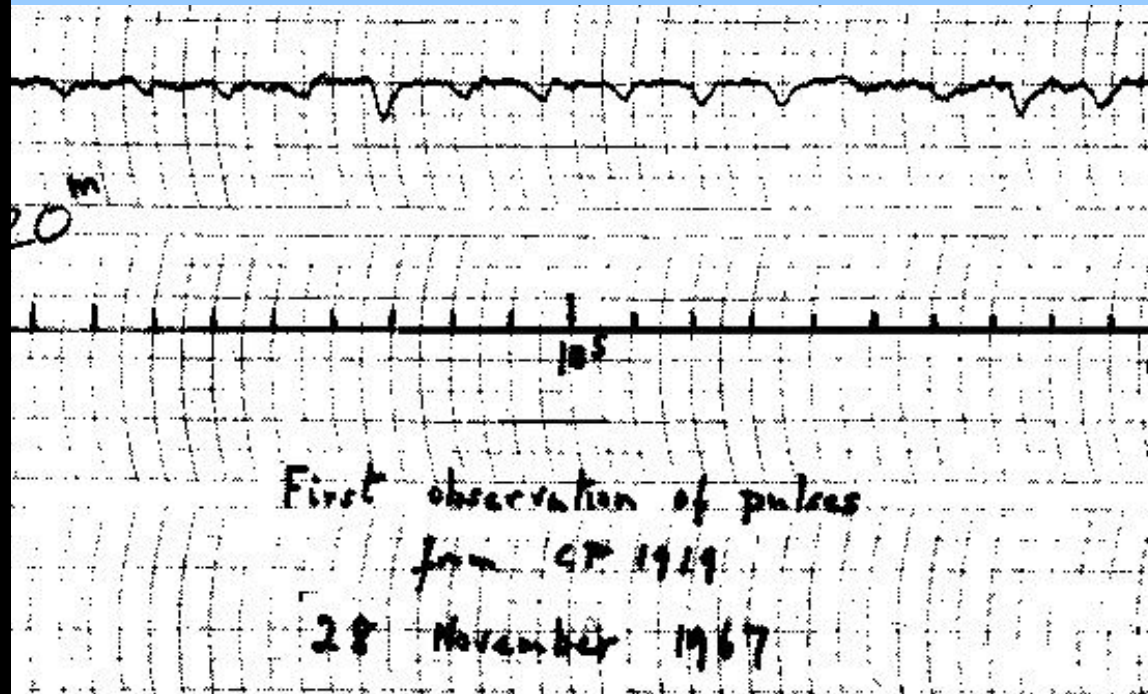
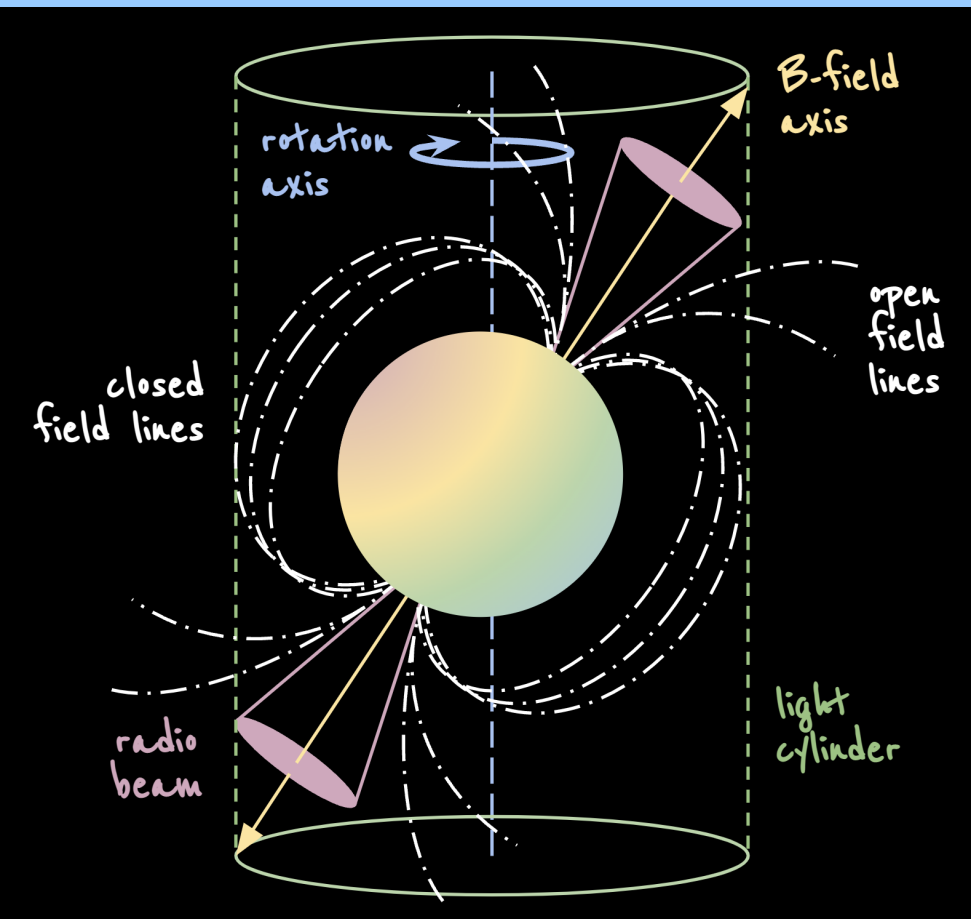
Effects of Gravitational Waves



Neutron Stars

$M \sim 1\text{-}2 M_{\odot}$, $R \sim 12 \text{ km}$

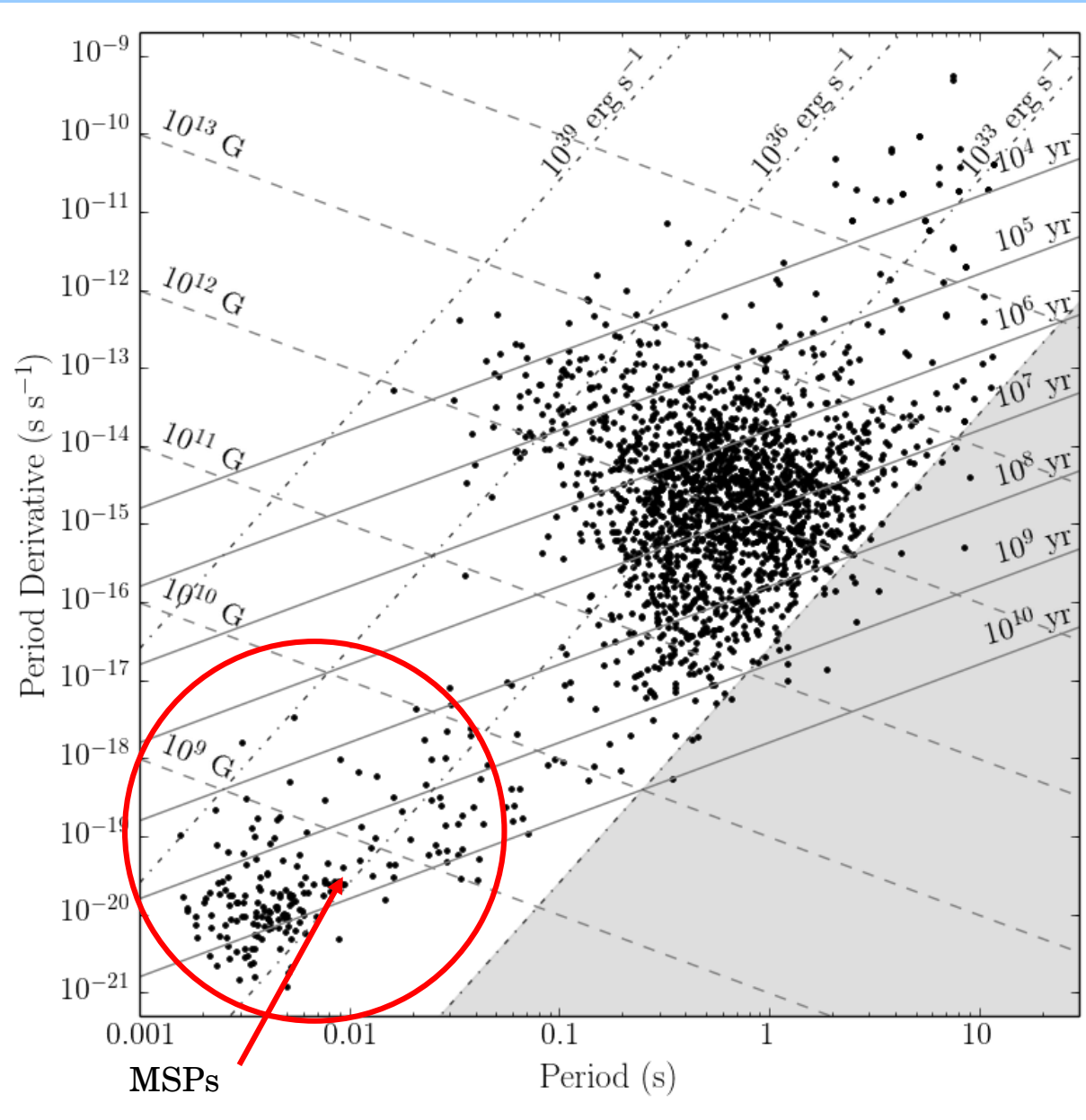




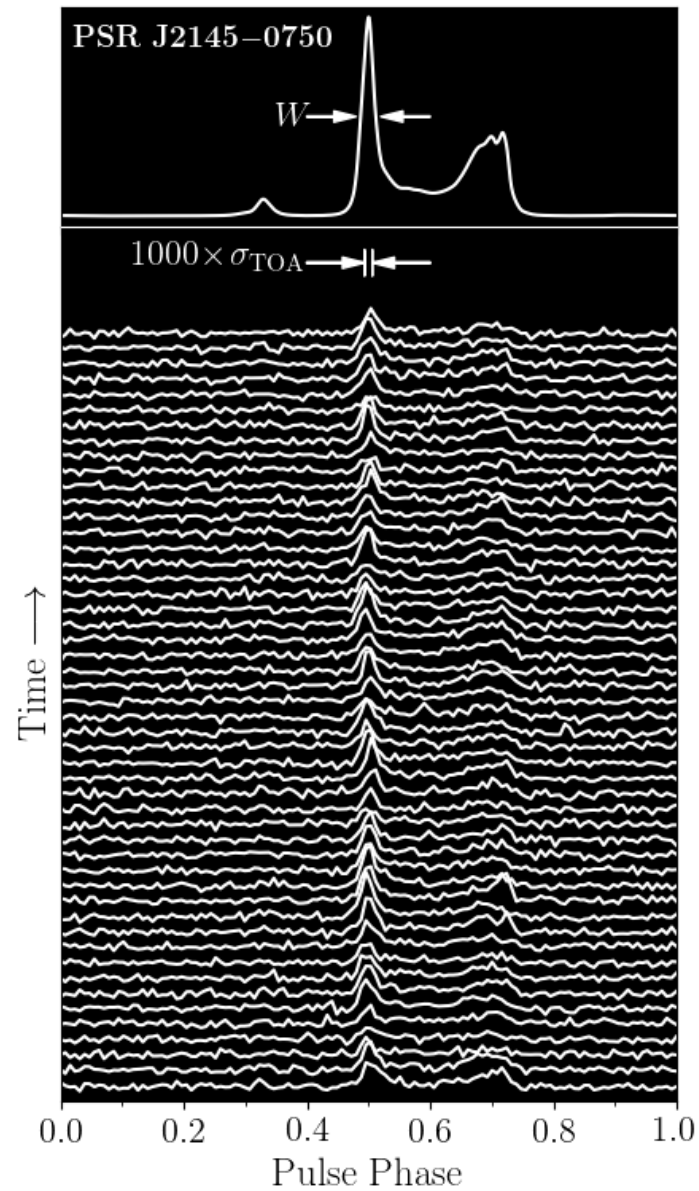
L: Thankful Cromartie

R: http://www.cv.nrao.edu/course/ast534/images/PSRs_discovery.jpg

Millisecond Pulsars



Measuring Pulses



Pulsars as Precise Clocks: J1909-3744

On July 13, 2012 at 00:00:00 UTC:

$$P = 2.947108025429647 \pm 0.000000000000000002 \text{ ms}$$

Pulsars as Precise Clocks: J1909-3744

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The last digit changes by 1 every 713 seconds

Pulsars as Precise Clocks: J1909-3744

On July 13, 2012 at 00:00:00 UTC:

$$P = 2.947108025429647 \pm 0.00000000000000002 \text{ ms}$$

The last digit changes by 1 every 713 seconds

This digit changes by 1 every 226 years

Pulsars as Precise Clocks: J1909-3744

On July 13, 2012 at 00:00:00 UTC:

$$P = 2.947108025429647 \pm 0.00000000000000002 \text{ ms}$$

The last digit changes by 1 every 713 seconds

This digit changes by 1 every 226 years

Between that time and the start of this talk, May 21, 2024 at 15:00 UTC, the pulsar has completed nearly 126,960,395,221 rotations (0.22 shy!)

More fun with J1909-3744

It's also completed over 2824 orbits around its companion white dwarf (0.11 over!)

Smallest eccentricity of any known binary in the Universe:

$$e = 0.000000109 \pm 0.0000000008$$

Orbit has radius= $(5.7014 \pm 0.0004) \cdot 10^8$ m (0.82 R_{sun})

But, we know the difference between the semi-major and semi-minor axis is $3.4 \pm 0.5 \mu\text{m}$!

The Tiny Effects of GWs

$$\begin{aligned} h &\sim \frac{G}{c^4} \frac{2 \times \frac{1}{2} I \omega^2}{D} \sim \frac{G M a^2 \omega^2}{c^4 D} \sim \frac{G M a^2}{c^4 D} \left(\frac{G(2M)}{a^3} \right) \sim \frac{2G^2 M^2}{c^4 D a} \\ &\approx 4.5 \times 10^{-15} \left(\frac{M}{10^8 M_\odot} \right)^2 \left(\frac{D}{10 \text{ Mpc}} \right)^{-1} \left(\frac{a}{\text{mpc}} \right)^{-1} \end{aligned}$$

$$\begin{aligned} f &\sim \frac{1}{2\pi} \left(\frac{G(2M)}{a^3} \right)^{1/2} \\ &\approx 150 \text{ nHz} \left(\frac{M}{10^8 M_\odot} \right)^{1/2} \left(\frac{a}{\text{mpc}} \right)^{-3/2} \end{aligned}$$

The Tiny Effects of GWs

$$h \sim \frac{G}{c^4} \frac{2}{r} \frac{d^2 Q}{dt^2}$$

$$\approx 4.5$$

$$\Delta L \sim hL \sim hcT$$

$$\approx 100 \text{ m} \left(\frac{h}{10^{-15}} \right) \left(\frac{T}{10 \text{ yr}} \right)$$

$$\sim \frac{2G^2 M^2}{c^4 D a}$$

$$\sim -1$$

$$\Delta t \sim \frac{\Delta L}{c} \sim hT$$

$$f \approx 300 \text{ ns} \left(\frac{h}{10^{-15}} \right) \left(\frac{T}{10 \text{ yr}} \right)$$

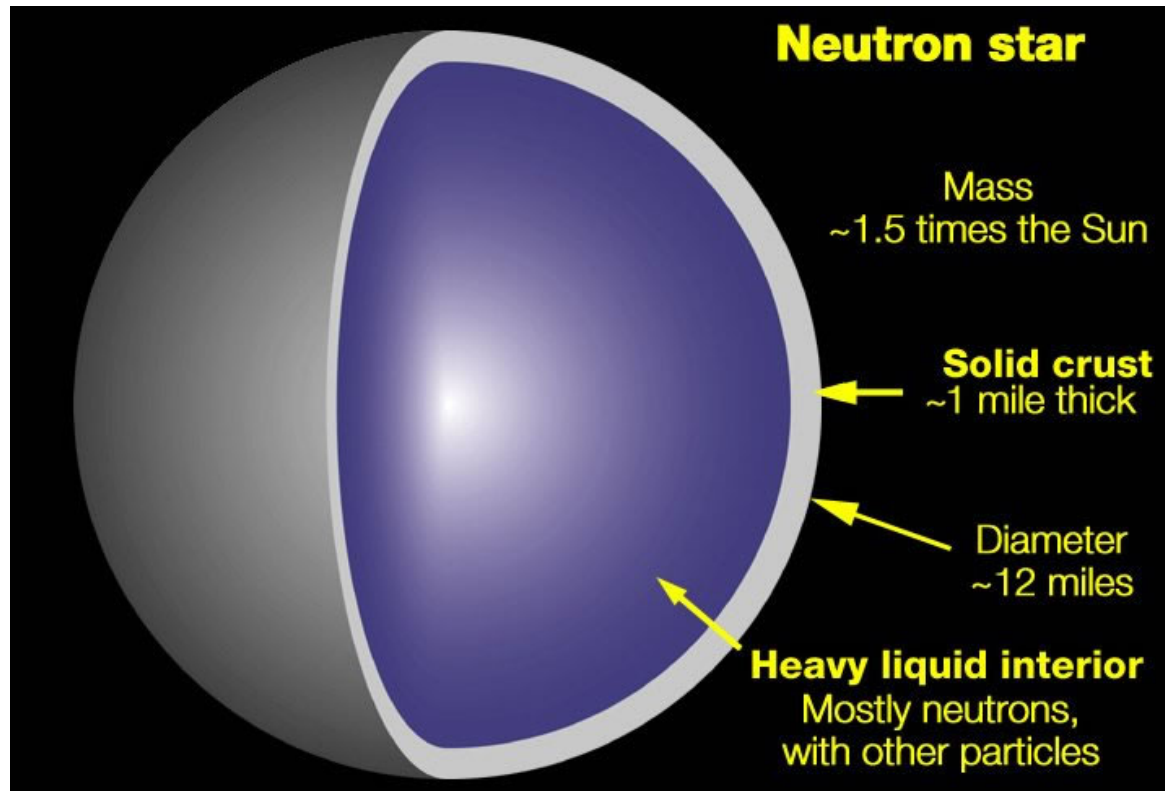
$$\approx 150 \text{ nHz} \left(\frac{M}{10^8 M_\odot} \right) \left(\frac{a}{\text{mpc}} \right)^{-3/2}$$

The Tiny Effects of GWs

$$h \sim \frac{G}{c^4} \frac{\Delta L}{T} \sim \frac{2G^2 M^2}{c^4 D a} \sim 10^{-21}$$

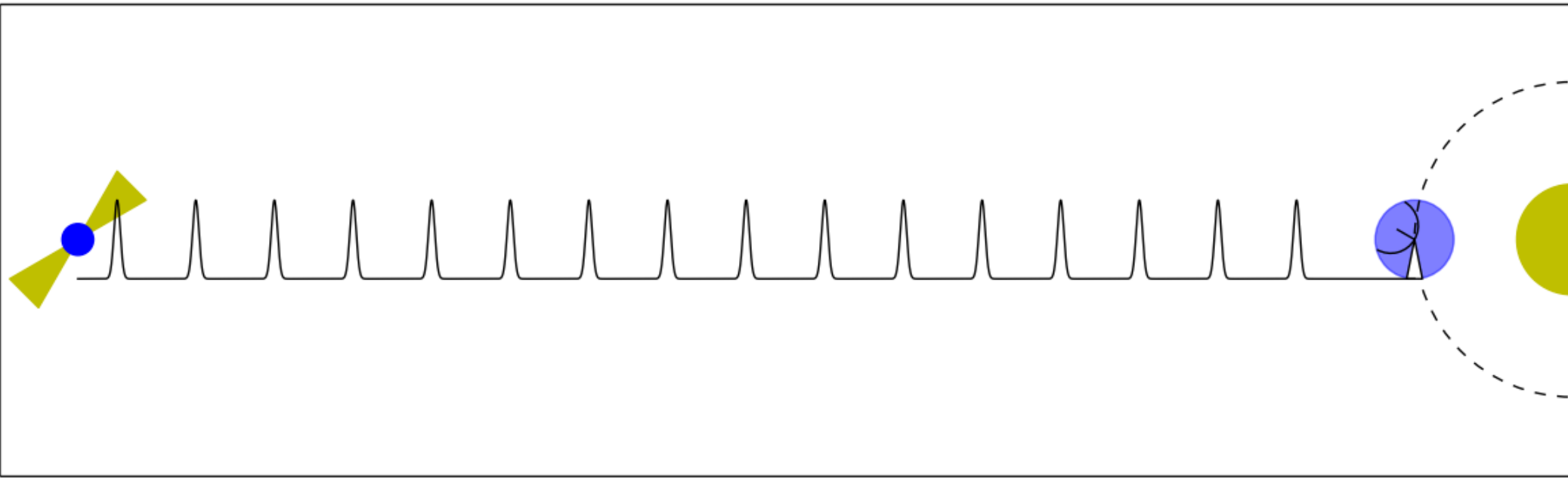
$$\Delta L \sim h L \sim h c T$$

$$\approx 100 \text{ m} \left(\frac{h}{10^{-15}} \right) \left(\frac{T}{10 \text{ yr}} \right)$$

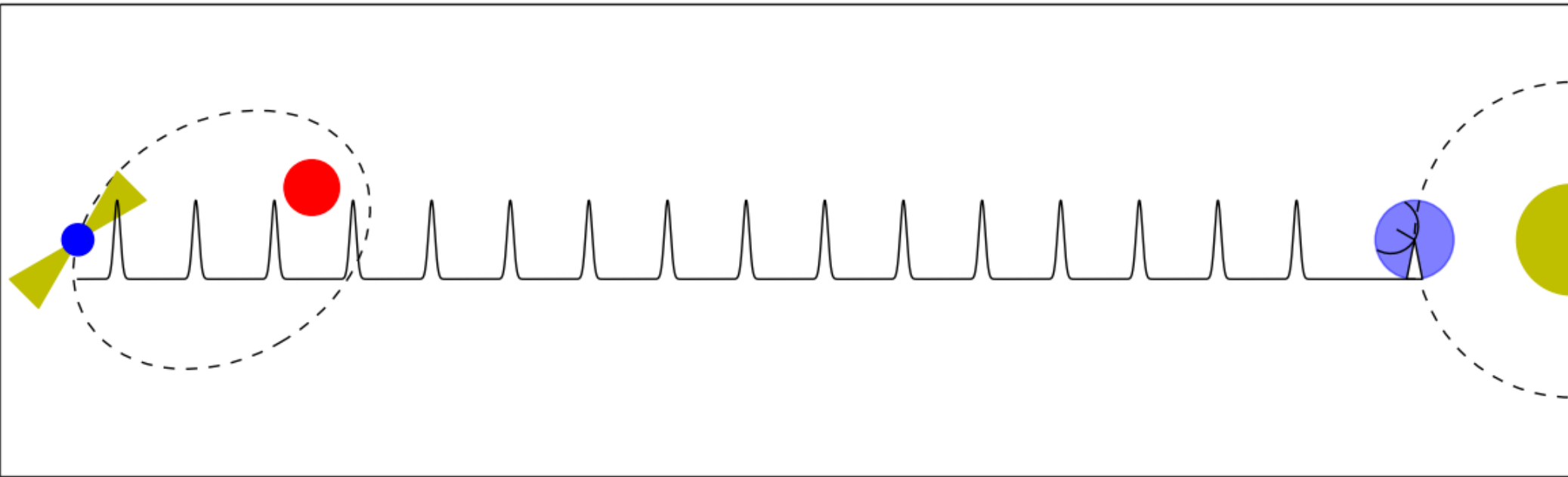


$$\approx 0.01 R_{\text{NS}}$$

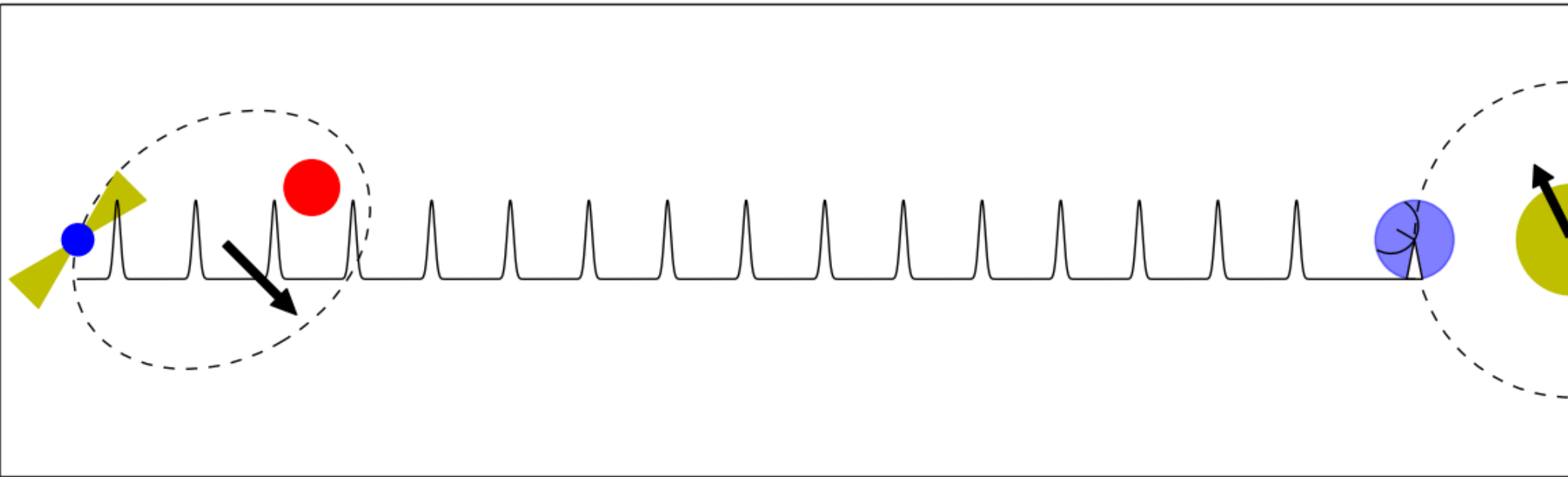
Timing Model



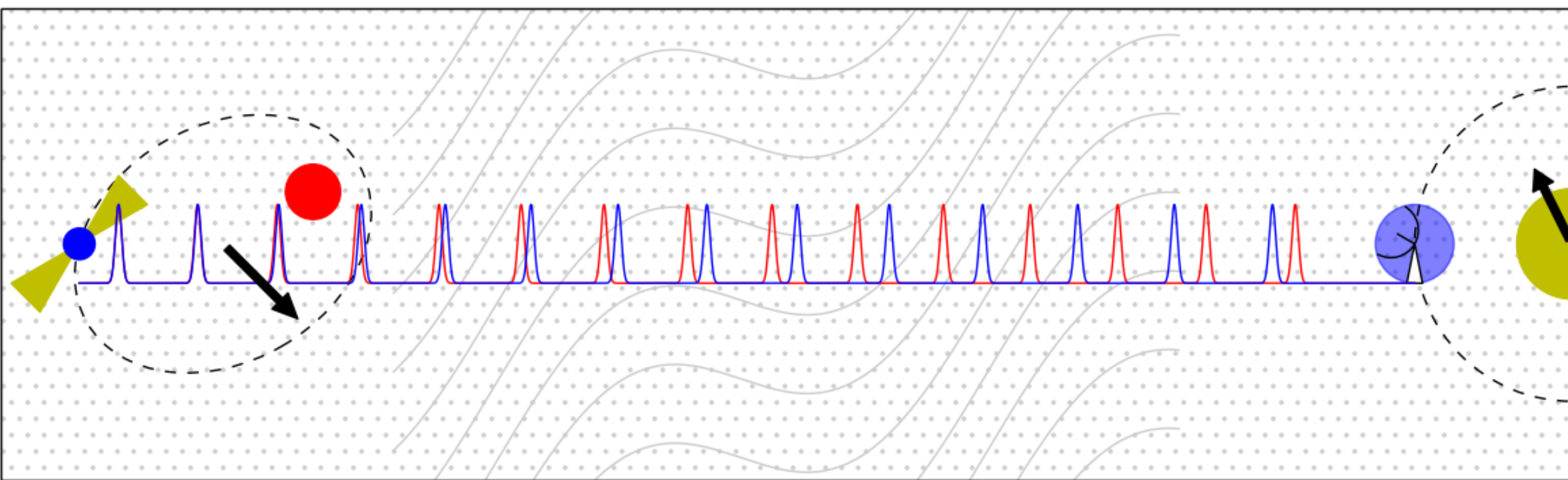
Timing Model



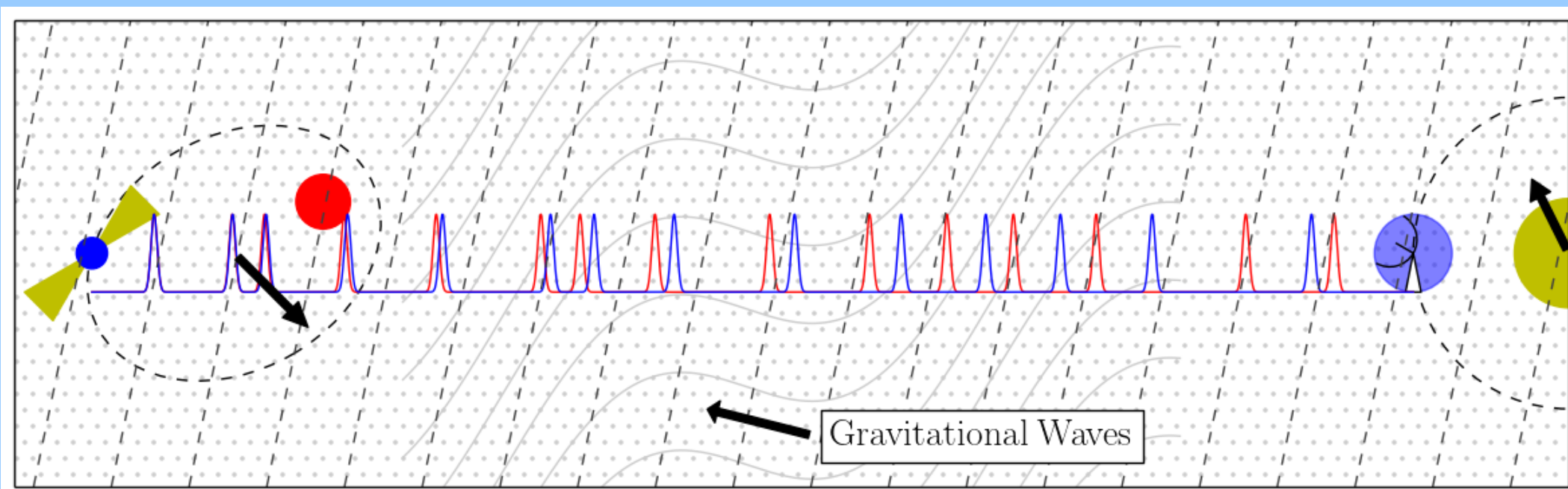
Timing Model



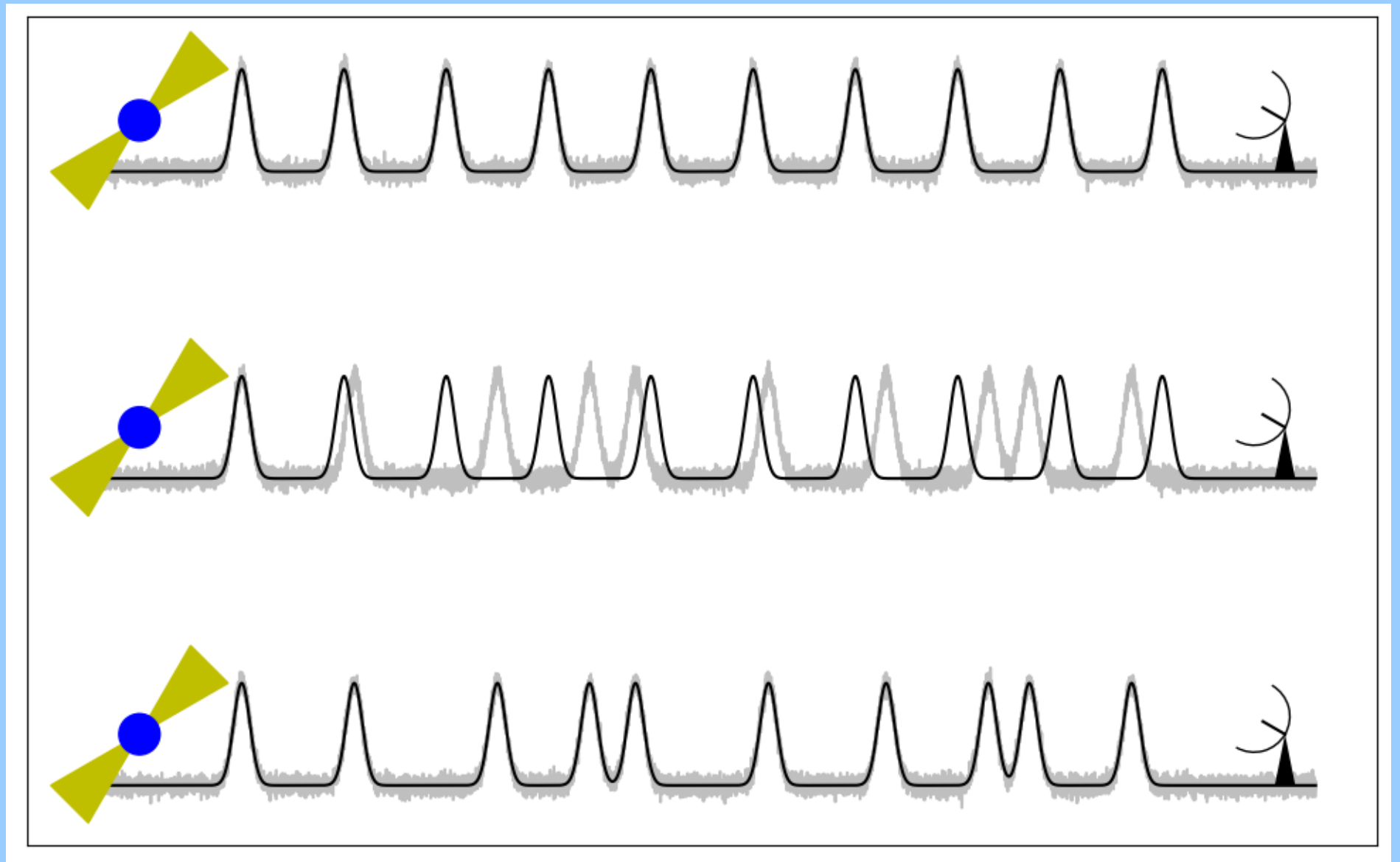
Timing Model



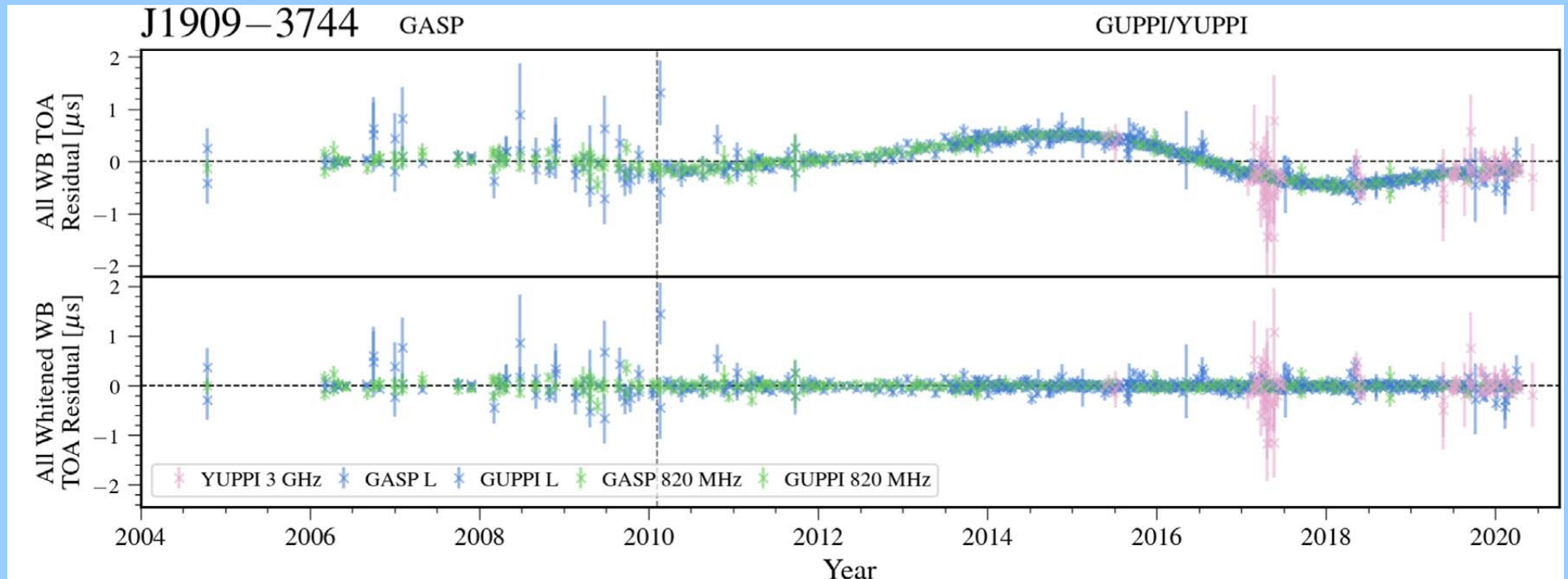
Timing Model



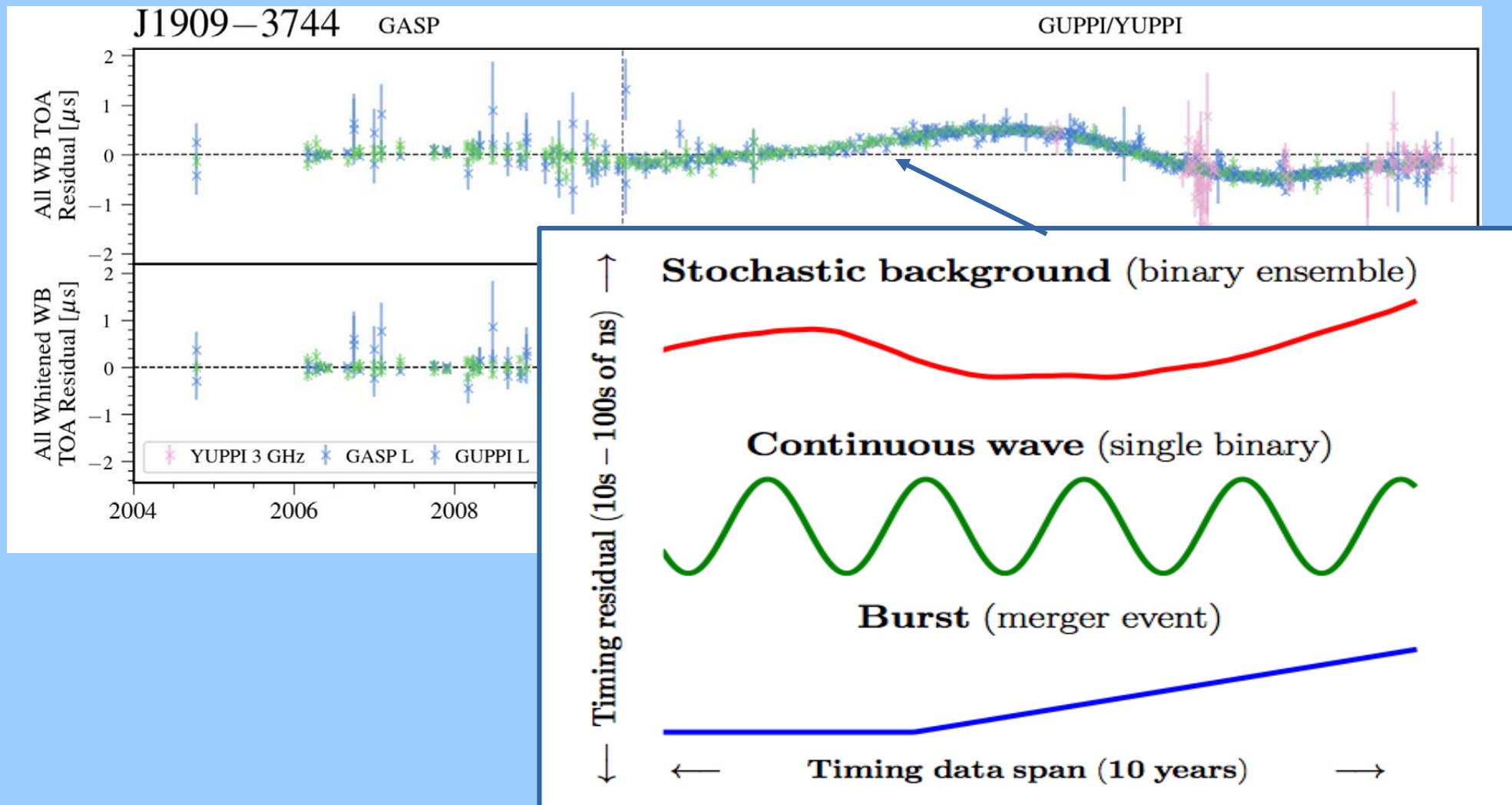
Pulsar Timing



Residuals and GW Signatures



Residuals and GW Signatures

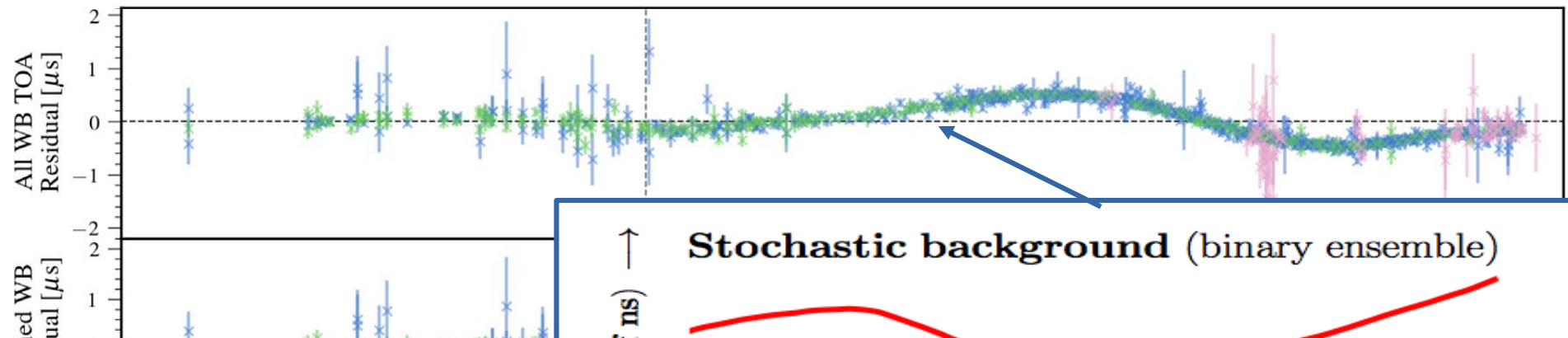


Residuals and GW Signatures

J1909–3744

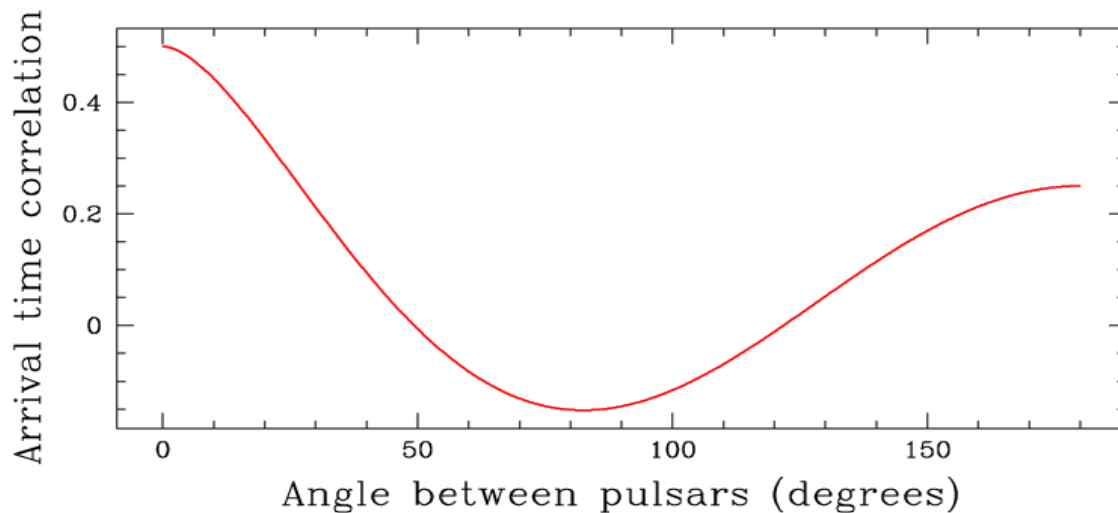
GASP

GUPPI/YUPPI



↑
ns

Stochastic background (binary ensemble)



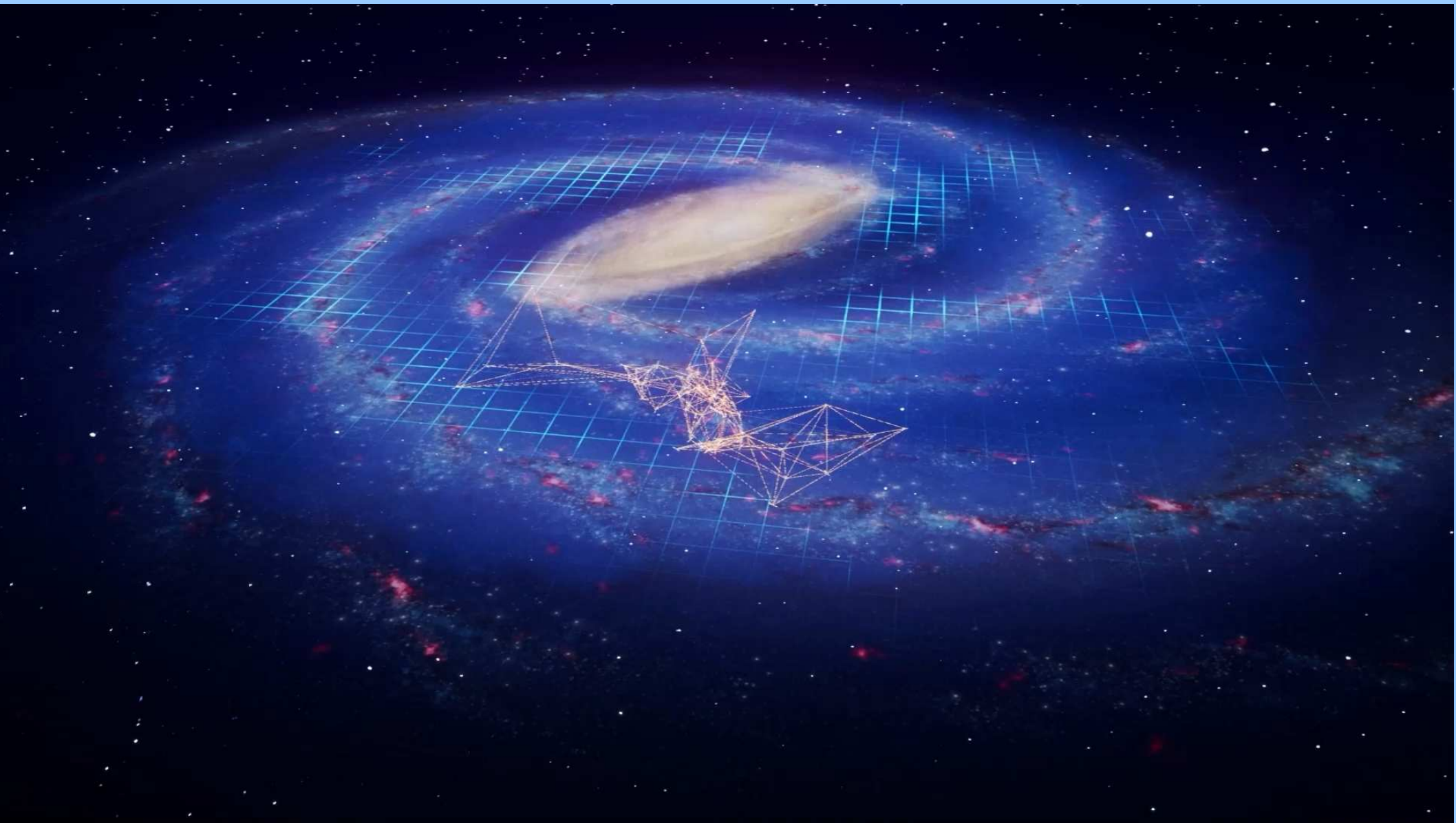
Continuous wave (single binary)

Burst (merger event)

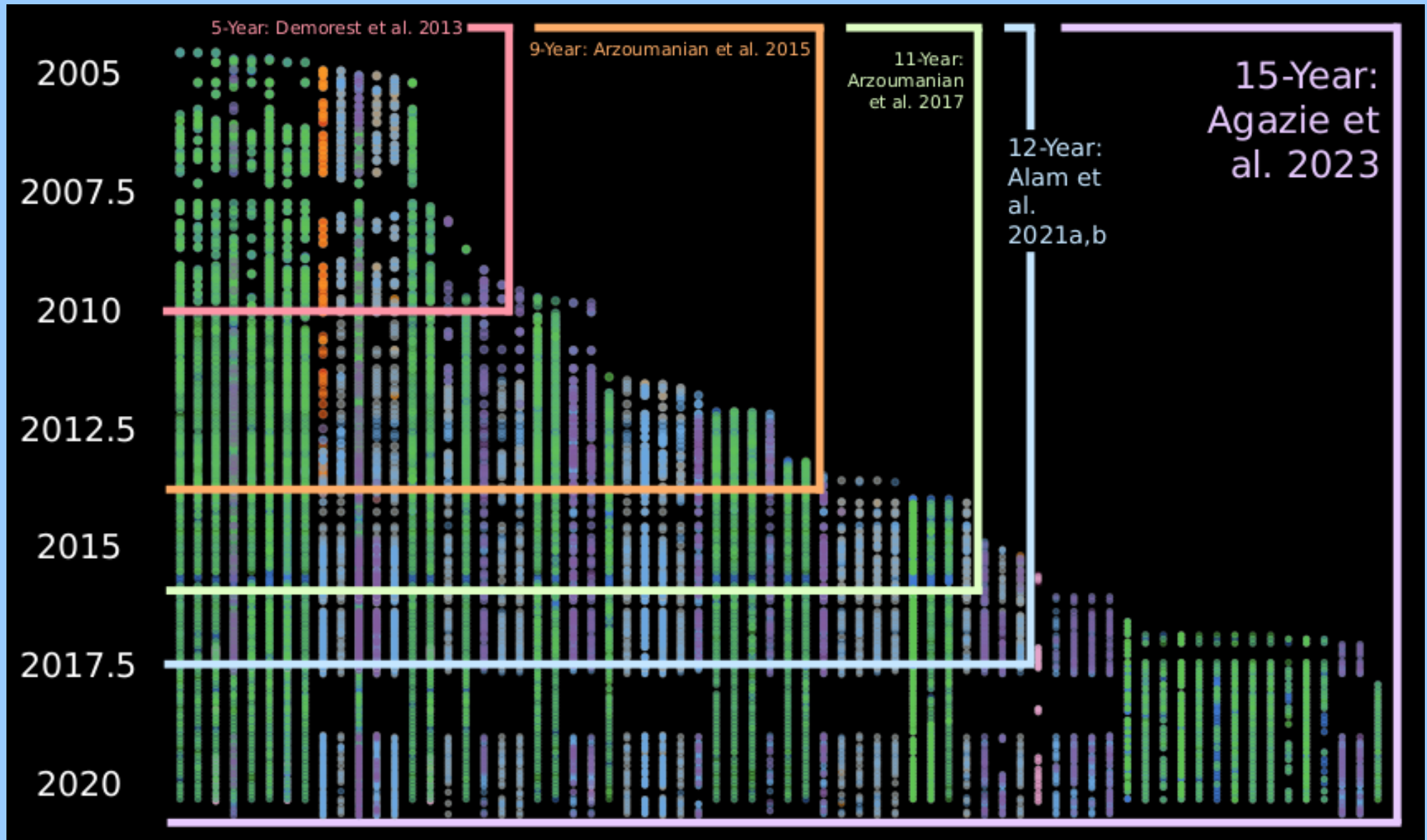
Long data span (10 years)

→

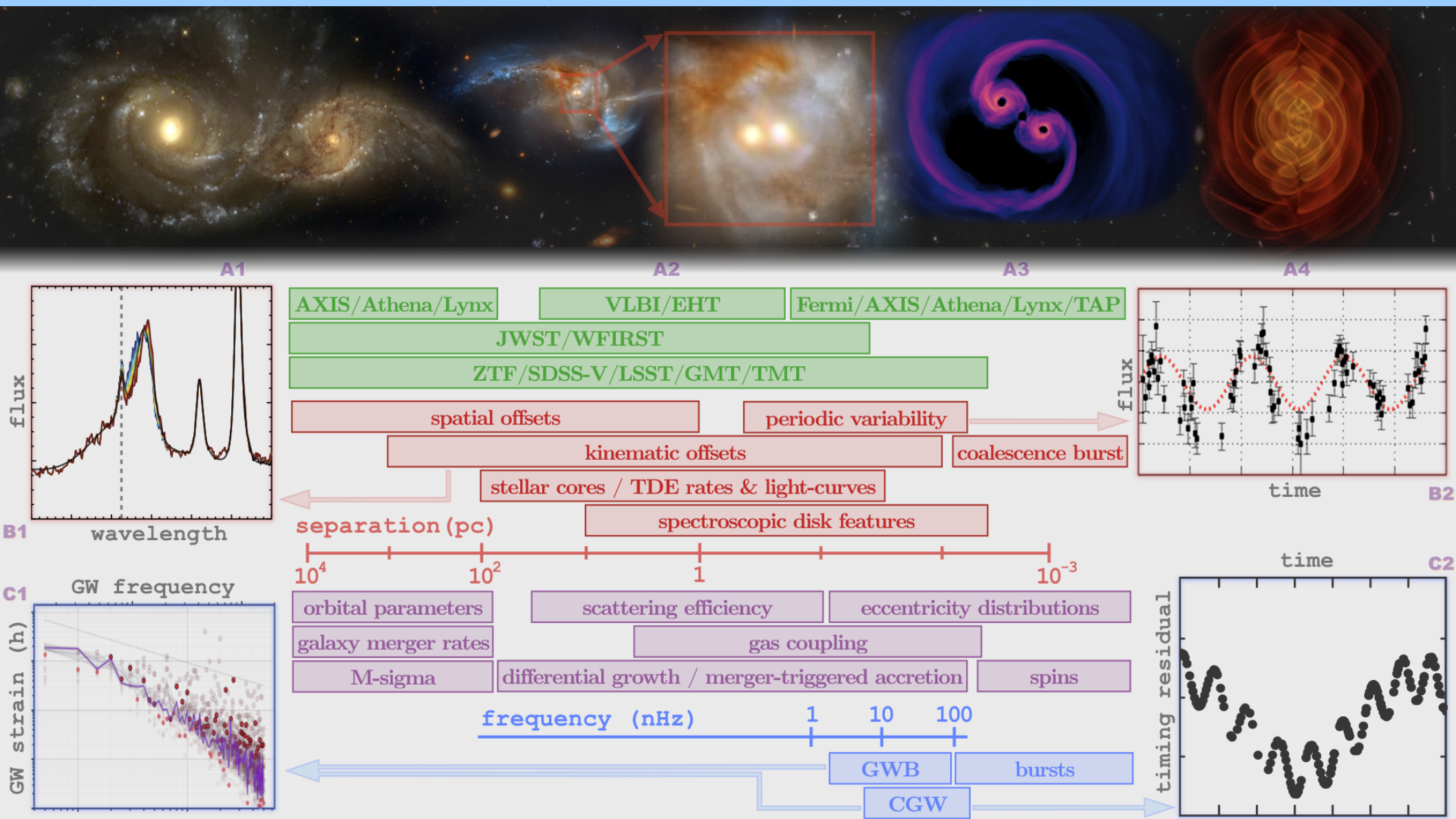
The Pulsar Timing Array



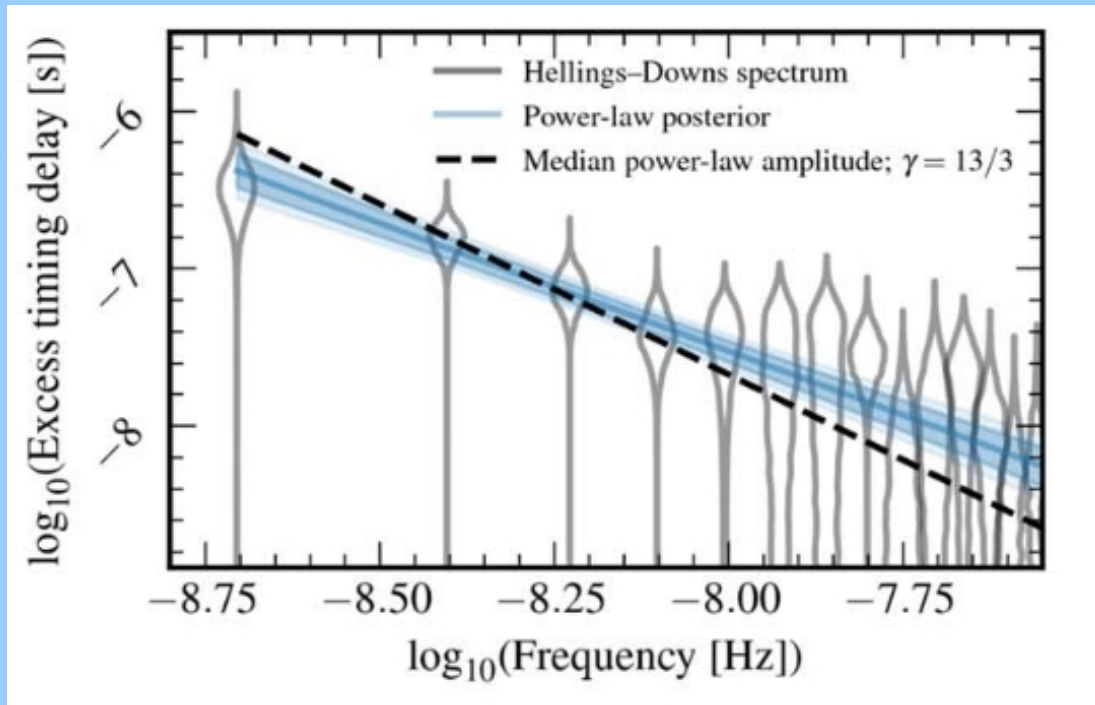
The Datasets



Multimessenger Science

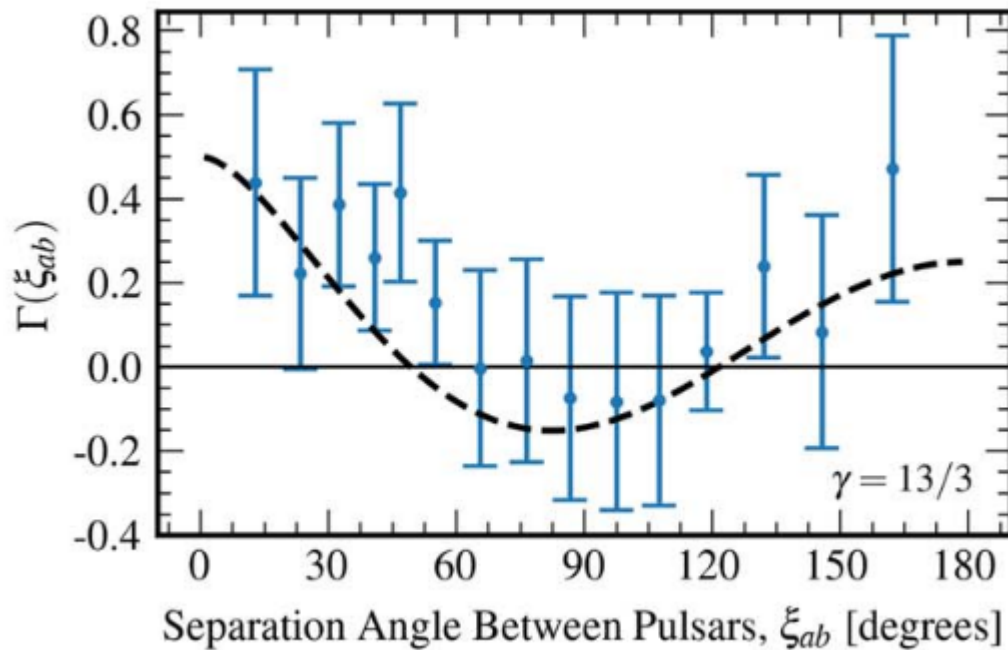


15-Year Data Set GWB Analysis



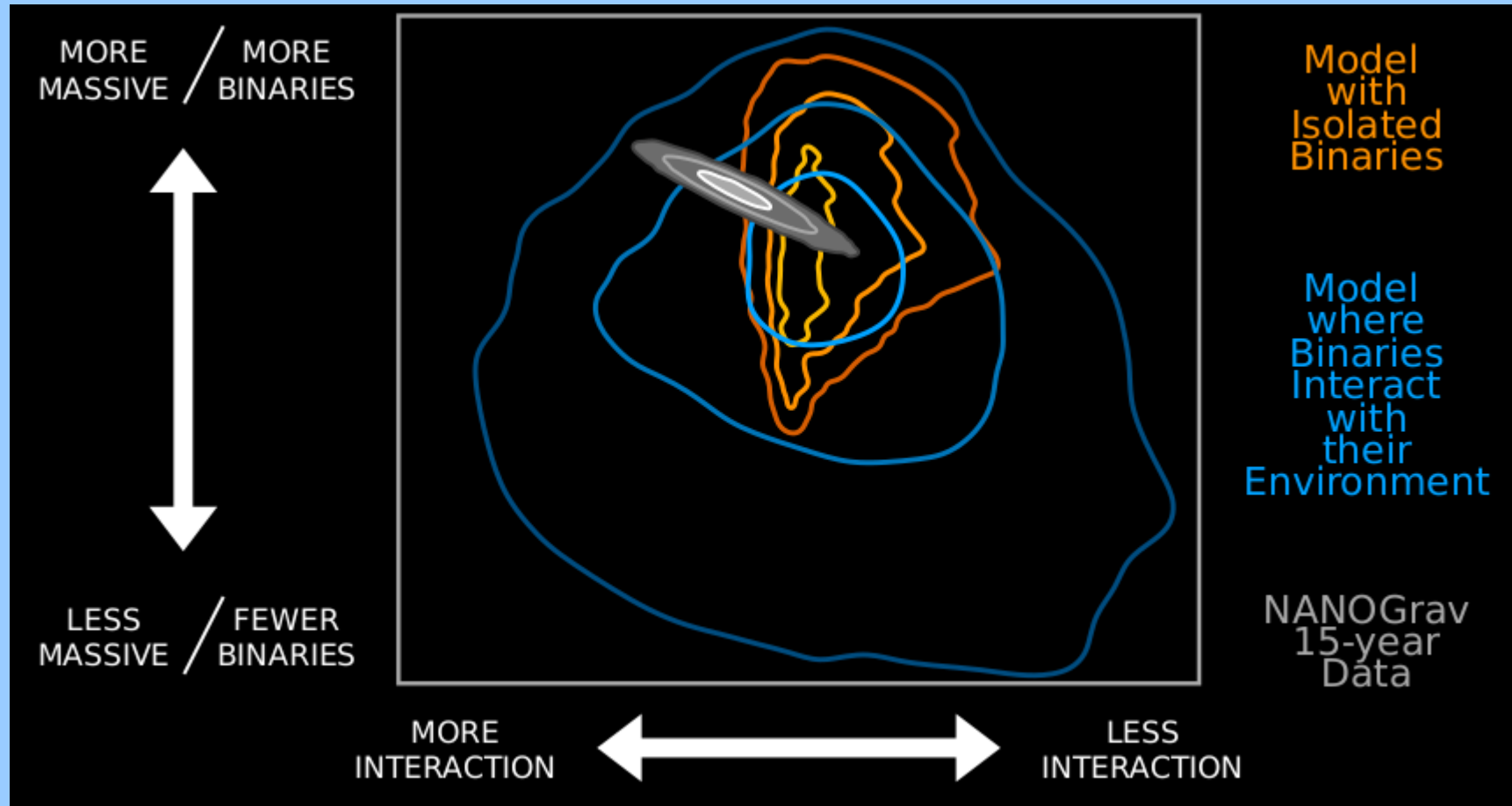
$\text{BF} \sim 10^{12}$ for Common Process

15-Year Data Set GWB Analysis

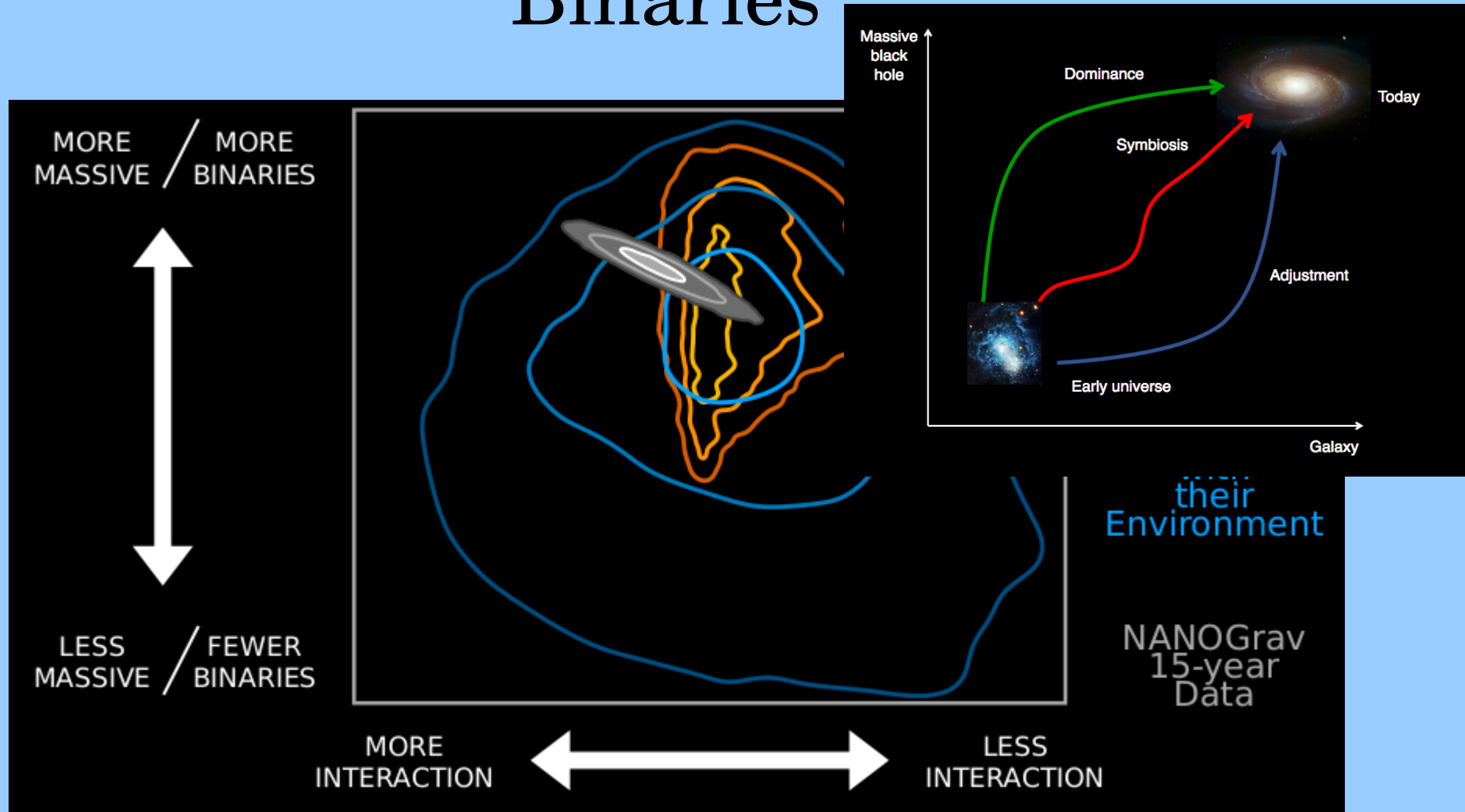


$\text{BF} \sim 10^{12}$ for Common
Process,
 $\text{BF} \sim 200\text{-}1000$ for
Hellings-Downs
Null Distribution Tests
 $p = 10^{-3} - 5 \times 10^{-5}$ ($3\text{-}4\sigma$)

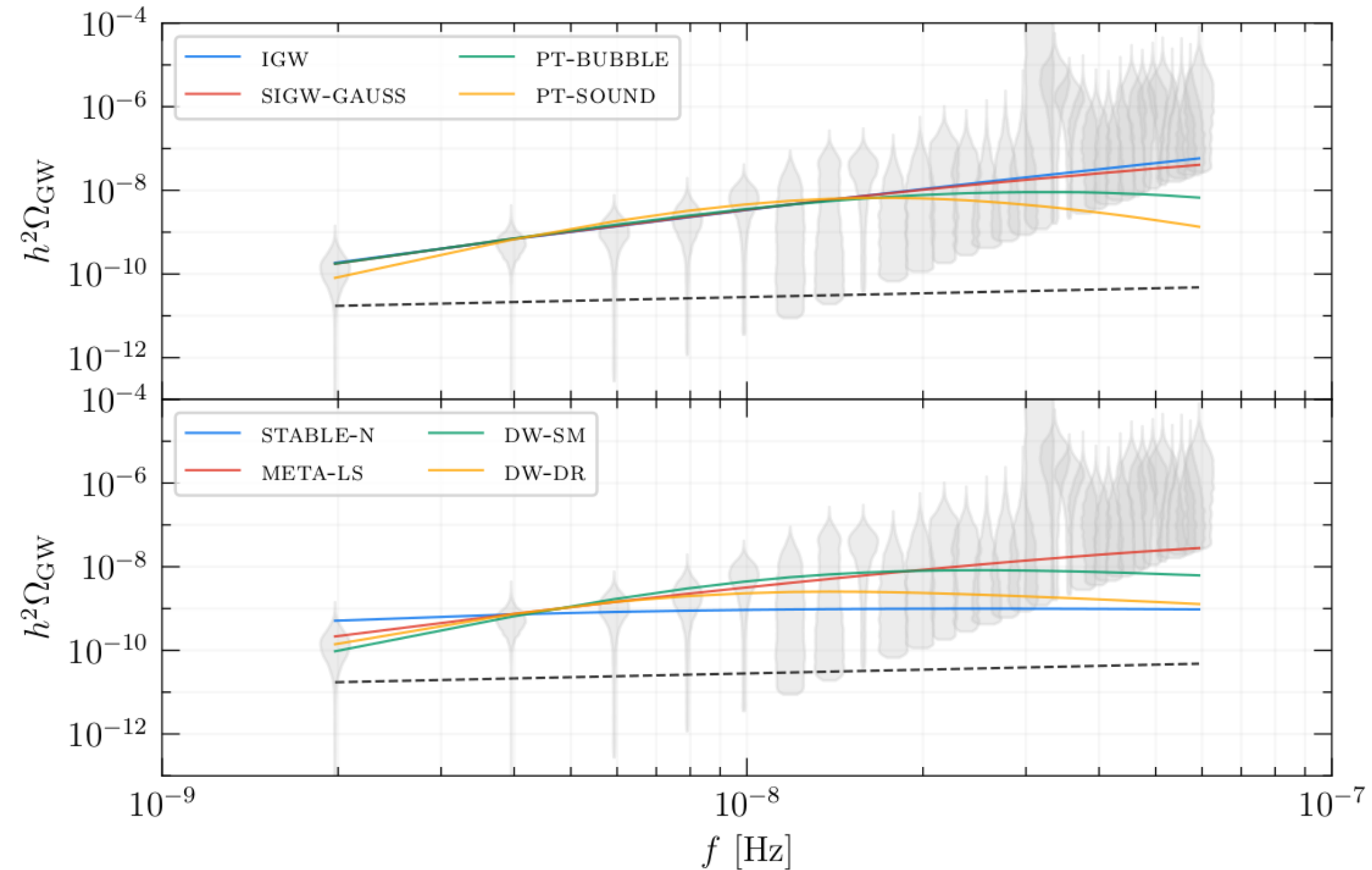
Astrophysics: Supermassive Black Hole Binaries



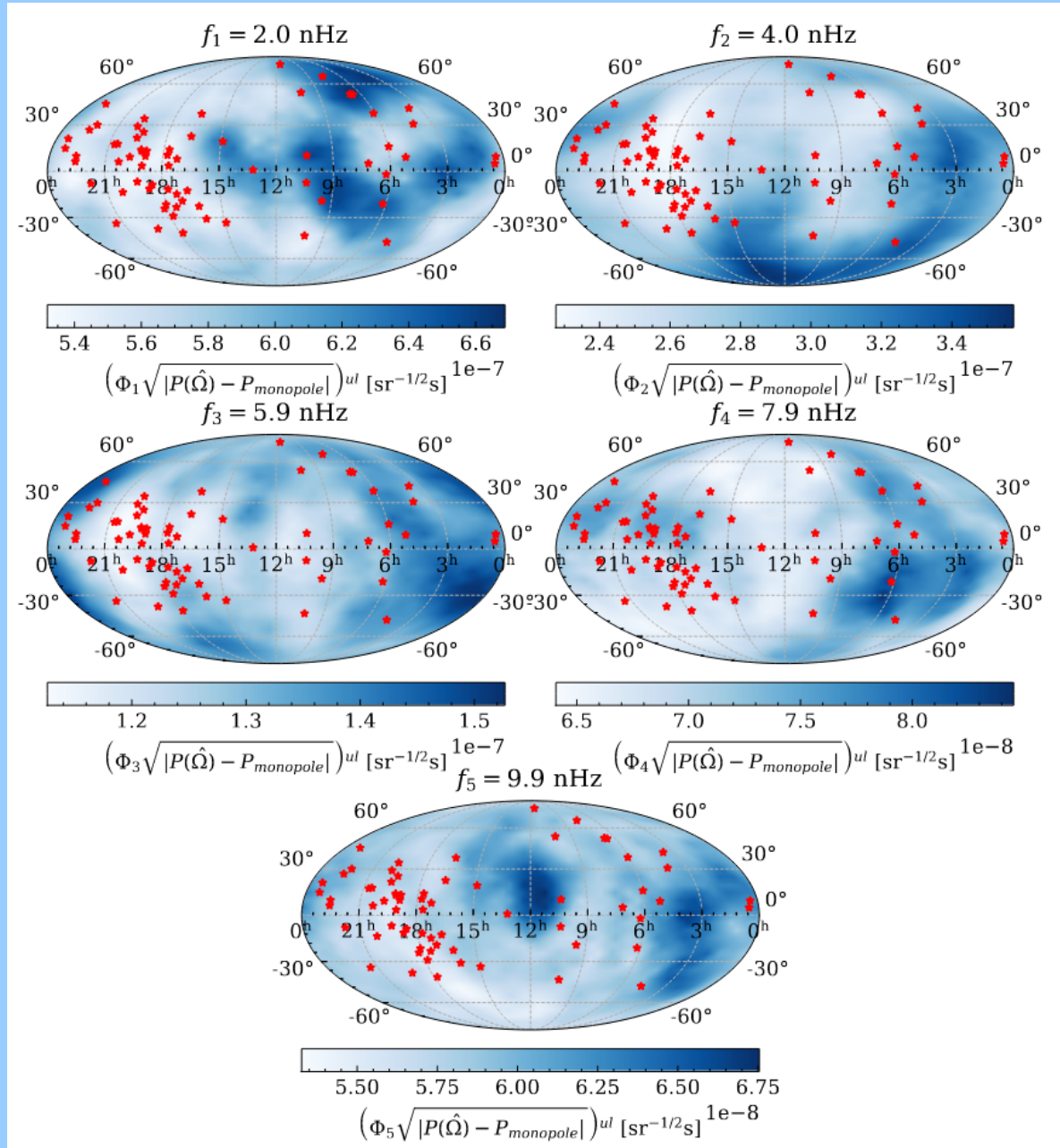
Astrophysics: Supermassive Black Hole Binaries



Astrophysics: New Physics



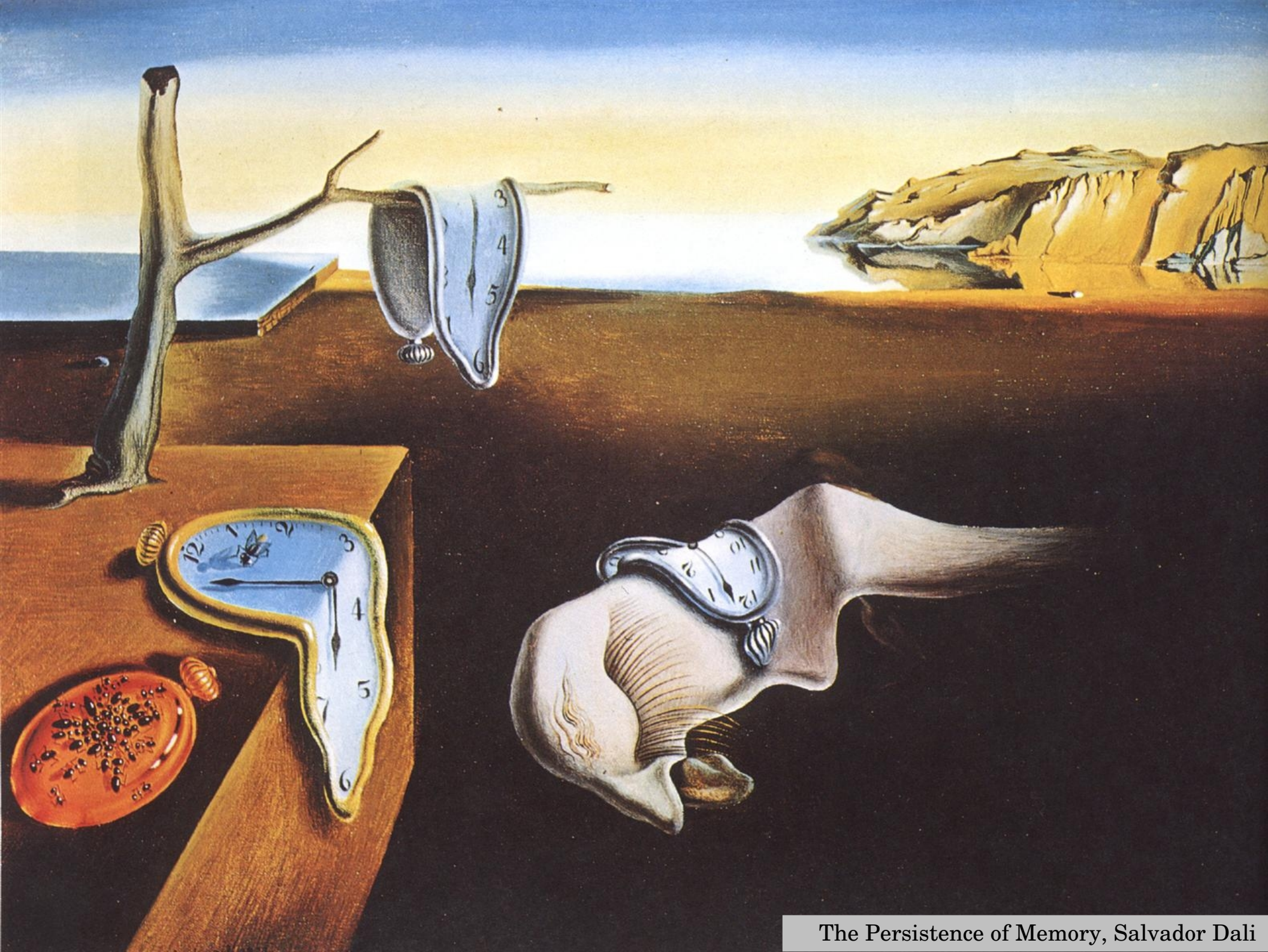
Mapping the Low-Frequency Gravitational Wave Universe



Future Facilities

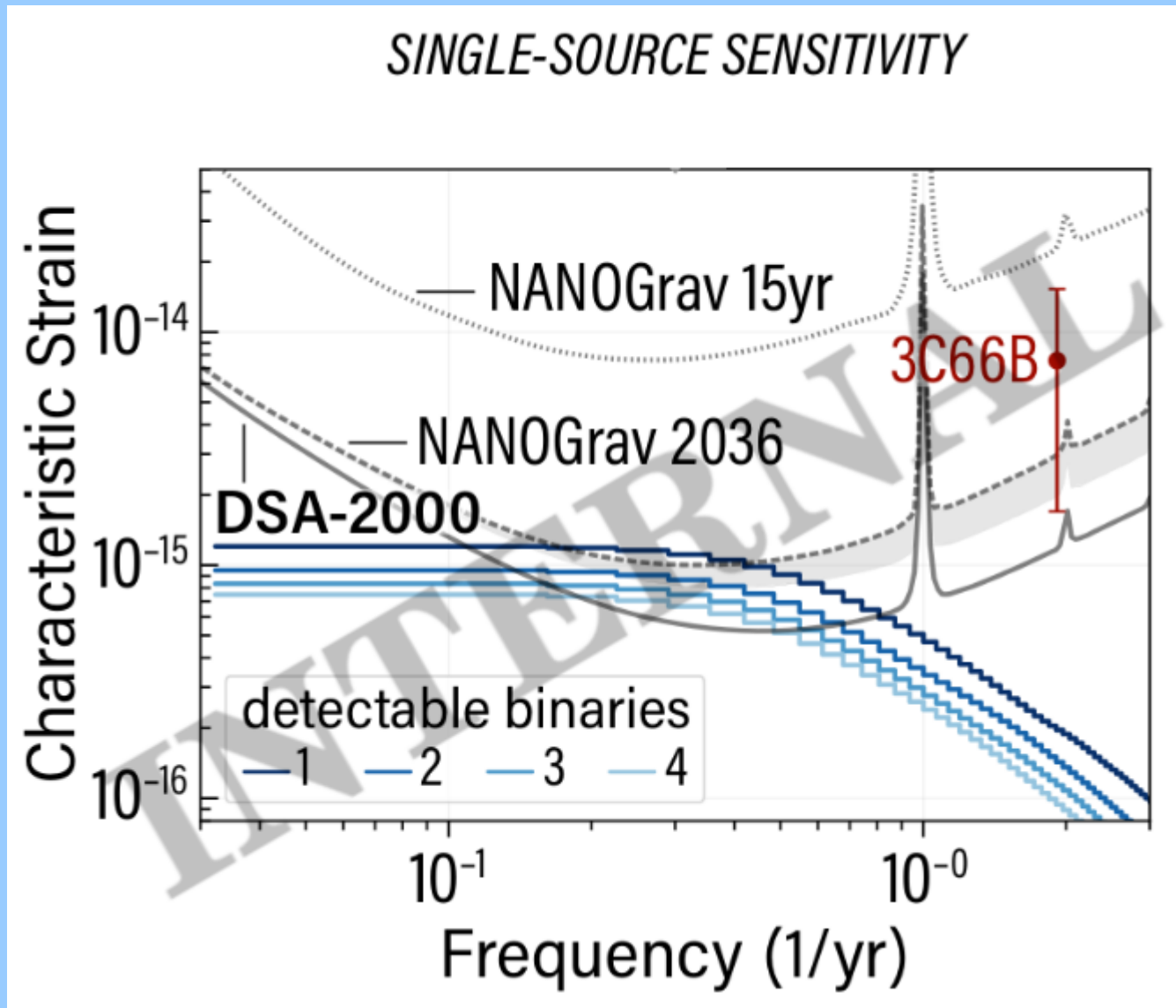


Top: NSF/AUI/NRAO, Bottom: DSA-2000 / C. Carter

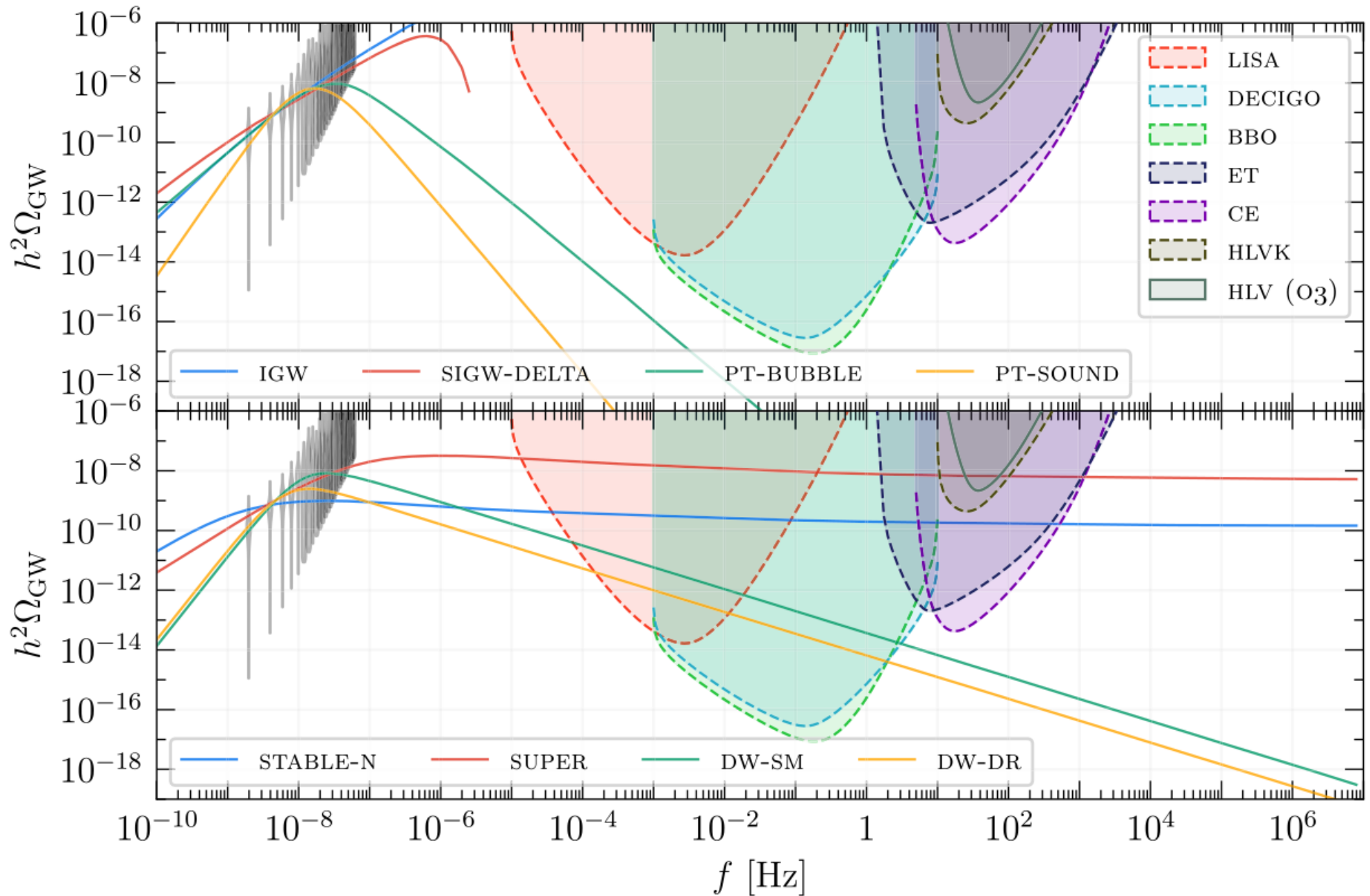


The Persistence of Memory, Salvador Dali

Future Facilities



Astrophysics: New Physics



The Next Generation

LIGO $\rightarrow$ aLIGO

NANOGrav $\rightarrow$ “aNANOGrav”

