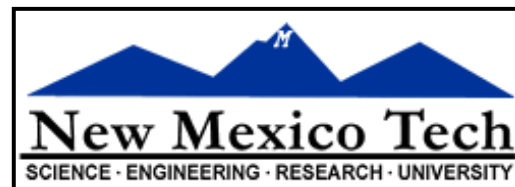


# Widefield Imaging II: Mosaic(k)ing + Short/Zero Spacing Correction



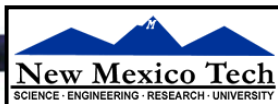
Thirteenth Synthesis Imaging Workshop  
2012 May 29 - June 5

Juergen Ott (NRAO)

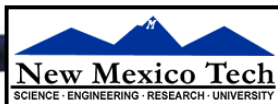


# Mosaicing: What is it all about?

- Imaging large regions on the sky, much larger than the primary beam
- The primary beam/field of view depends on the size of an individual dish, not the array configuration
- Mosaicing unlocks some short spacing information
- Is this important? Yes! The entire sky has about  $41,253 \text{ deg}^2$
- Primary beams:
  - JVLA (25m dishes): 20cm:  $0.25 \text{ deg}^2$ , 7mm:  $0.0003 \text{ deg}^2$
  - ALMA (12m dishes): band 3 (3mm):  $0.02 \text{ deg}^2$ , band 9 (650GHz):  $0.000005 \text{ deg}^2$
  - Nearby galaxies: M31 (@700kpc) :  $3 \text{ deg}^2$   
Arp 220 (@70Mpc):  $0.004 \text{ deg}^2$
- **Solution 1:** go to smaller dishes (e.g. ATA, 6m dishes @20cm:  $6.3 \text{ deg}^2$ ) but you will need a lot of dishes to gain sensitivity (ATA had planned hundreds)
- **Solution 2:** Mosaicing



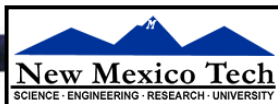
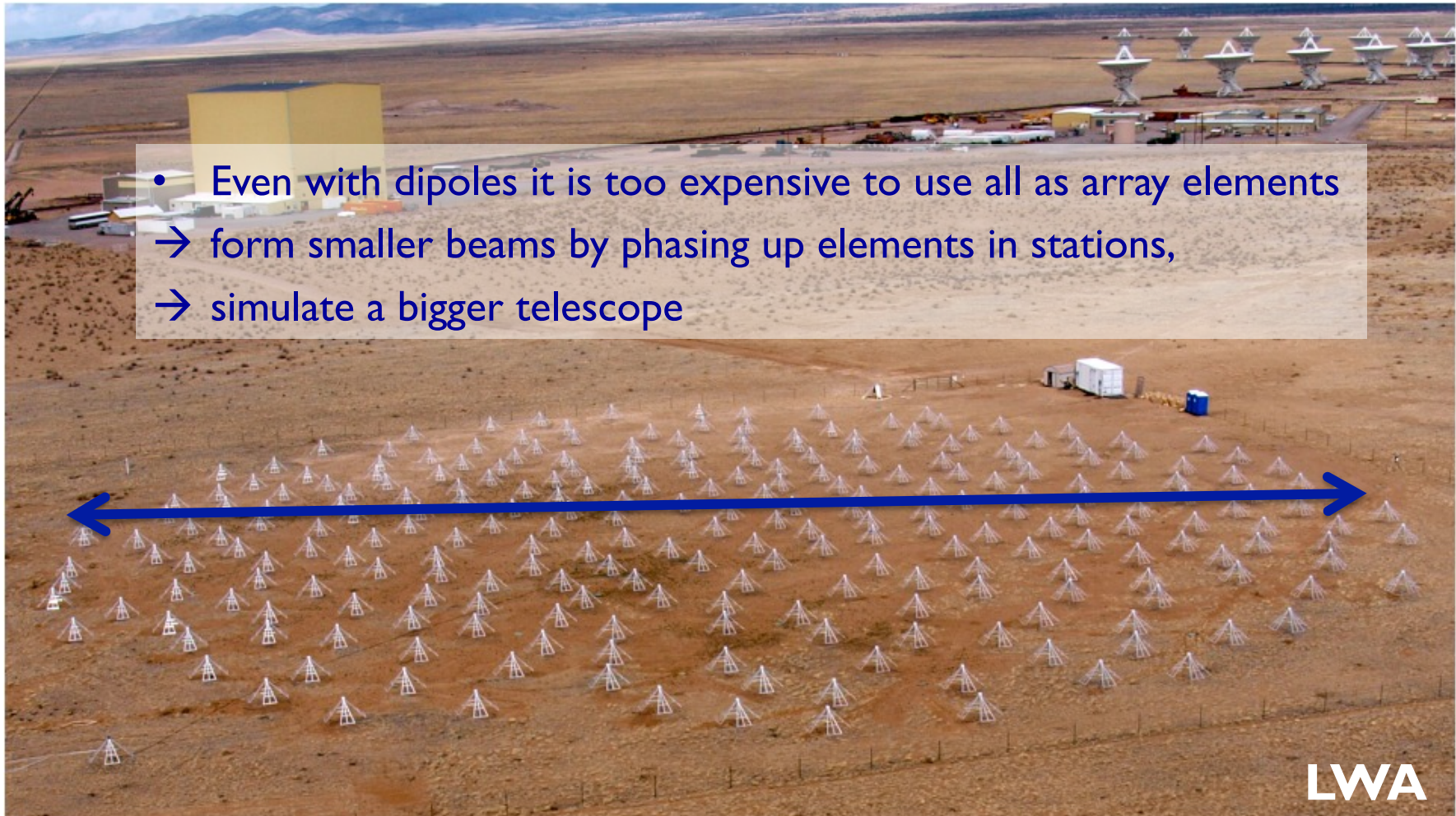
# Small Dishes: SKA





# Dipoles: $2\pi$

- Even with dipoles it is too expensive to use all as array elements  
→ form smaller beams by phasing up elements in stations,  
→ simulate a bigger telescope

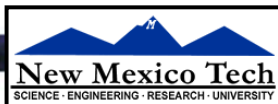




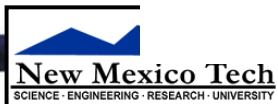
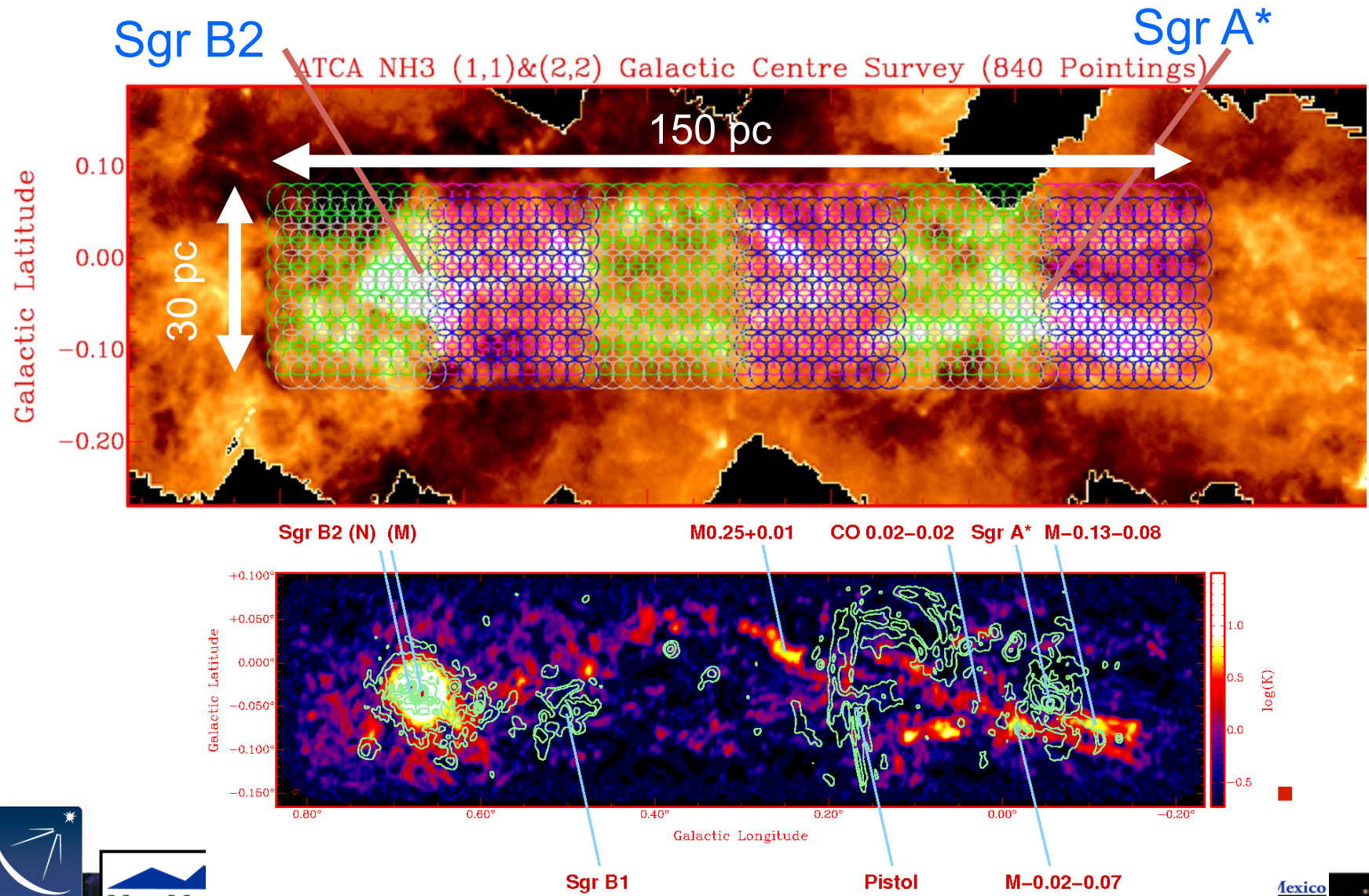
# Mosaicing

Single Dish Mapping

Interferometric Mosaicing

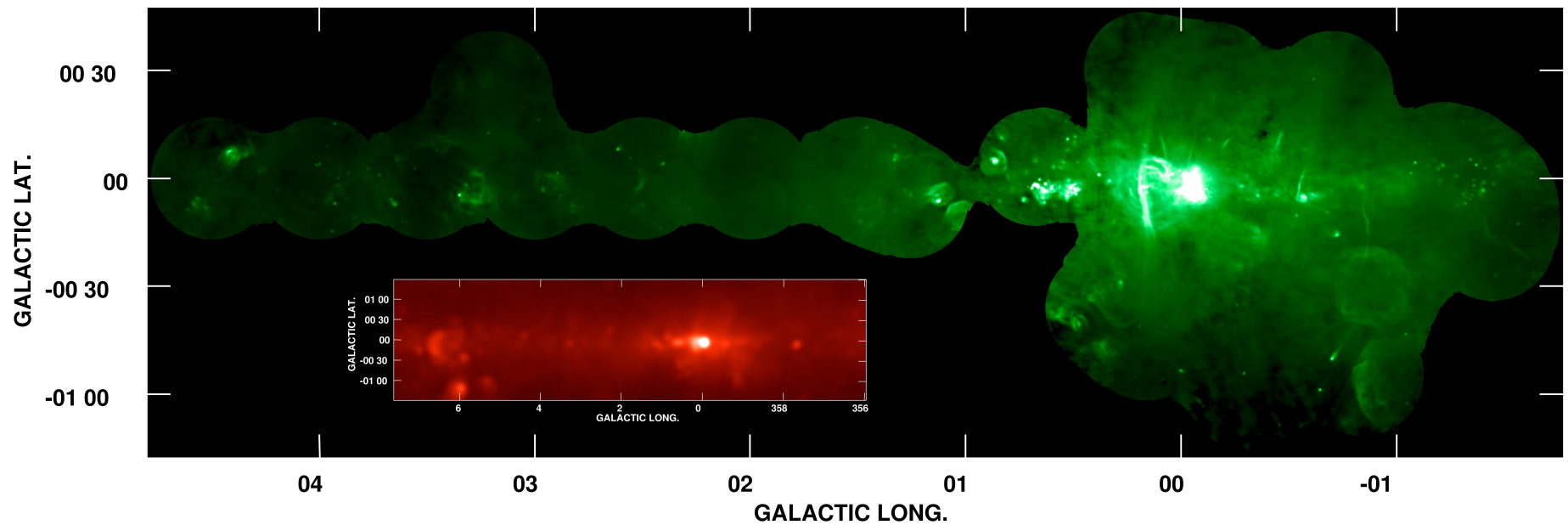


# Galactic Center

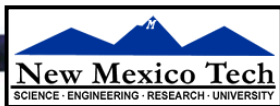




# Galactic Center

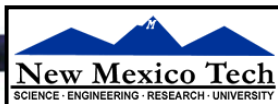


Yusef-Zadeh et al.



# Problems to solve

- Each primary beam is an attenuation which needs to be accounted for
- Pointings are in a time sequence:
  - Each pointing has a different uv-coverage
  - In addition: deconvolution is non-linear, so even identical uv-coverage but at a slightly different part on the sky with different sources in the field will result in a somewhat different image
  - Atmospheric water vapor/ionospheric variations from pointing to pointing
- Adequate sky coverage: Best uv-coverage? Uniform sensitivity? Maximal sky coverage?
- Minimize drive time but maximize well spaced uv-coverage across map to retain information
- Mosaicing is frequently used for very extended structures, short/zero spacing correction may be required (Ekers-Rots theorem: mosaicing can gain back some of the shorter spacings)





# The effect of the Primary Beam

PB defined by single antenna (SD). Not by the array configuration.

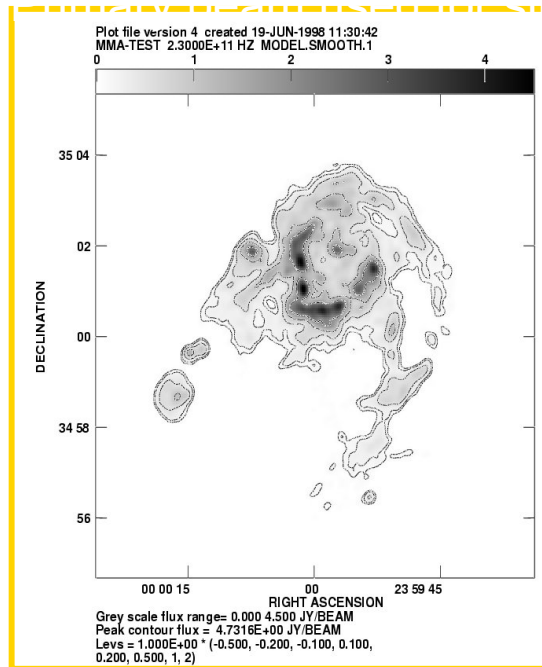
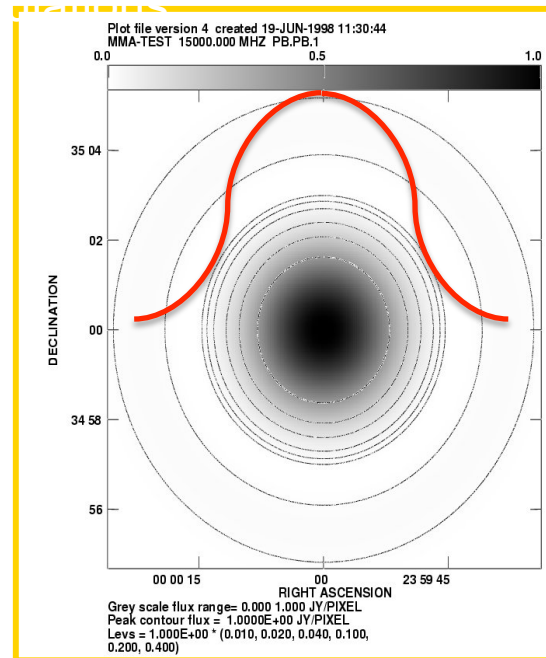
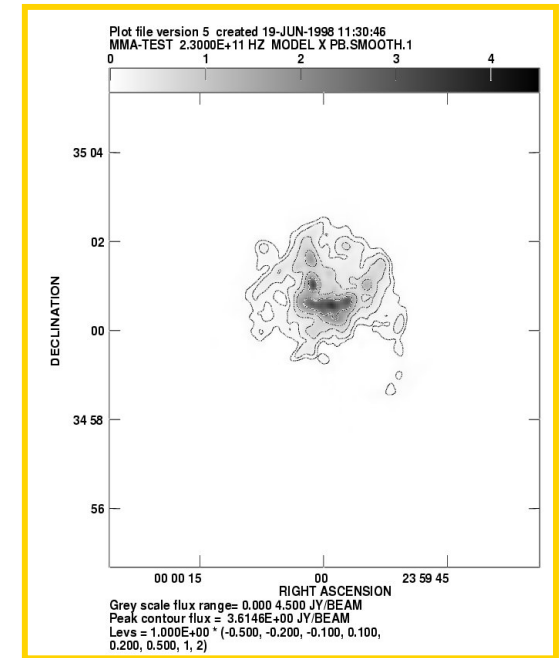


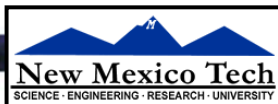
Image larger than PB



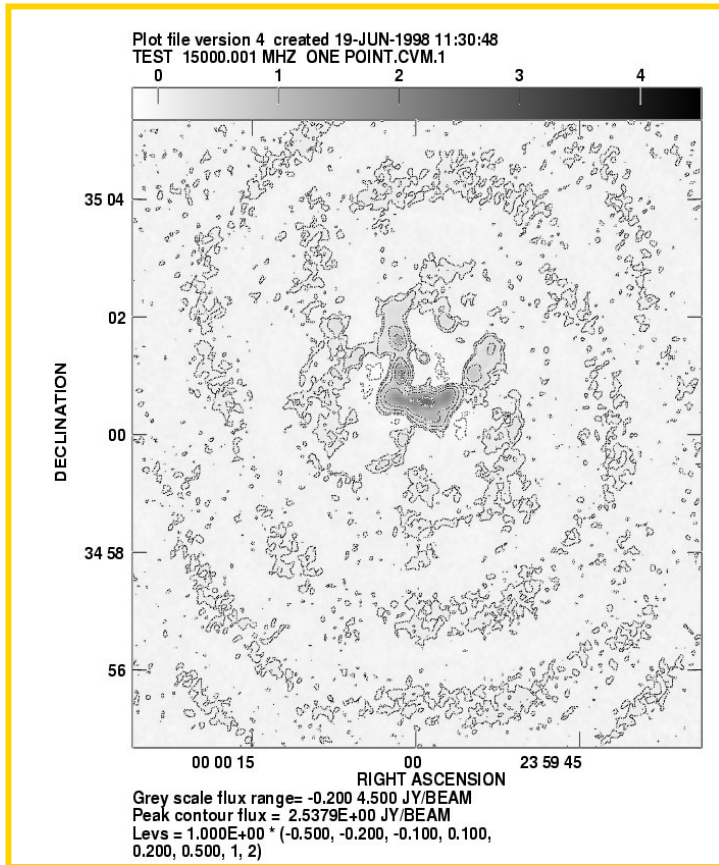
PB provides sensitivity pattern on sky



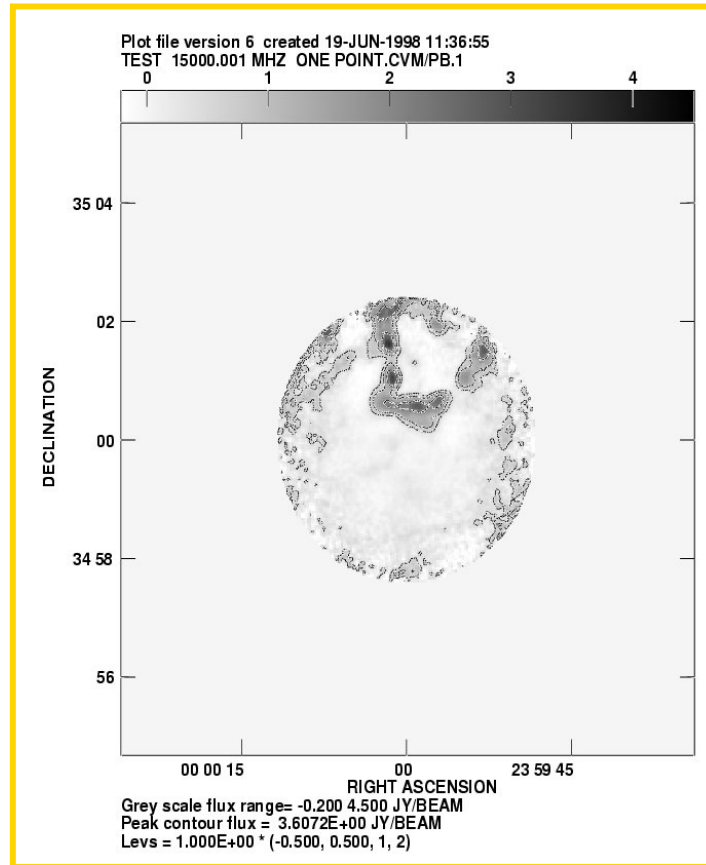
PB applied: sensitive to center only



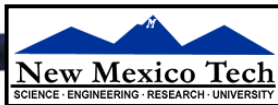
# The effect of the Primary Beam



Noise before PB correction



PB correction changes noise characteristics

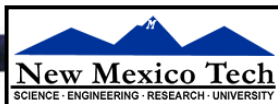




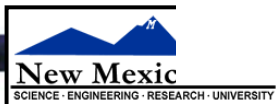
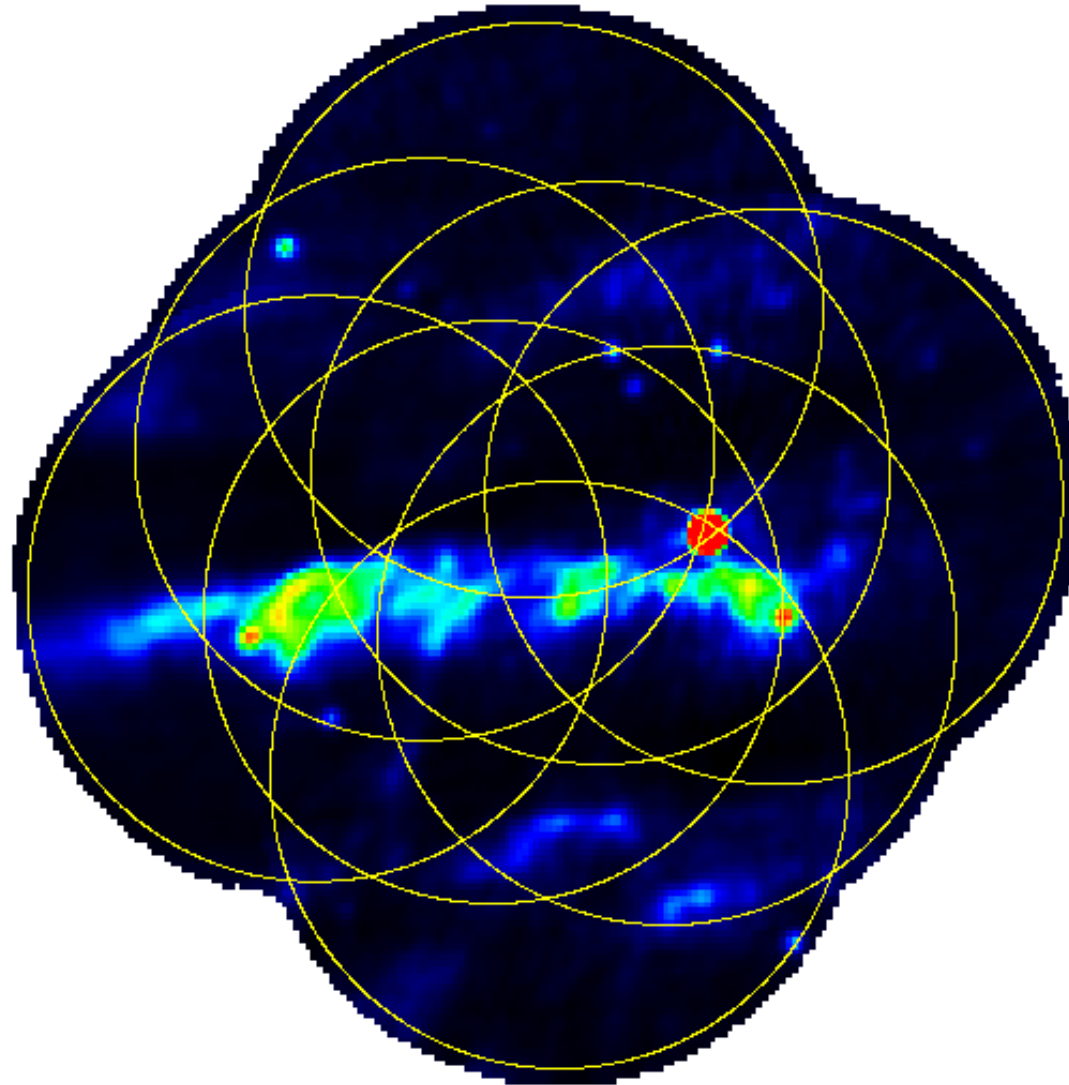
# Stitching the maps together: Image Reconstruction

Widely-used methods for mosaic image reconstruction:

- **Linear combination**  
*Map points individually → deconvolve individually → combine*
- **Joint deconvolution**  
*Map points individually → combine → deconvolve together*
- **Widefield Imaging by regridding of all visibilities before FFT into a single map**  
*Combine pointings in uv-space → single map → deconvolve*



# Mosaicing: Linear Combination of Images



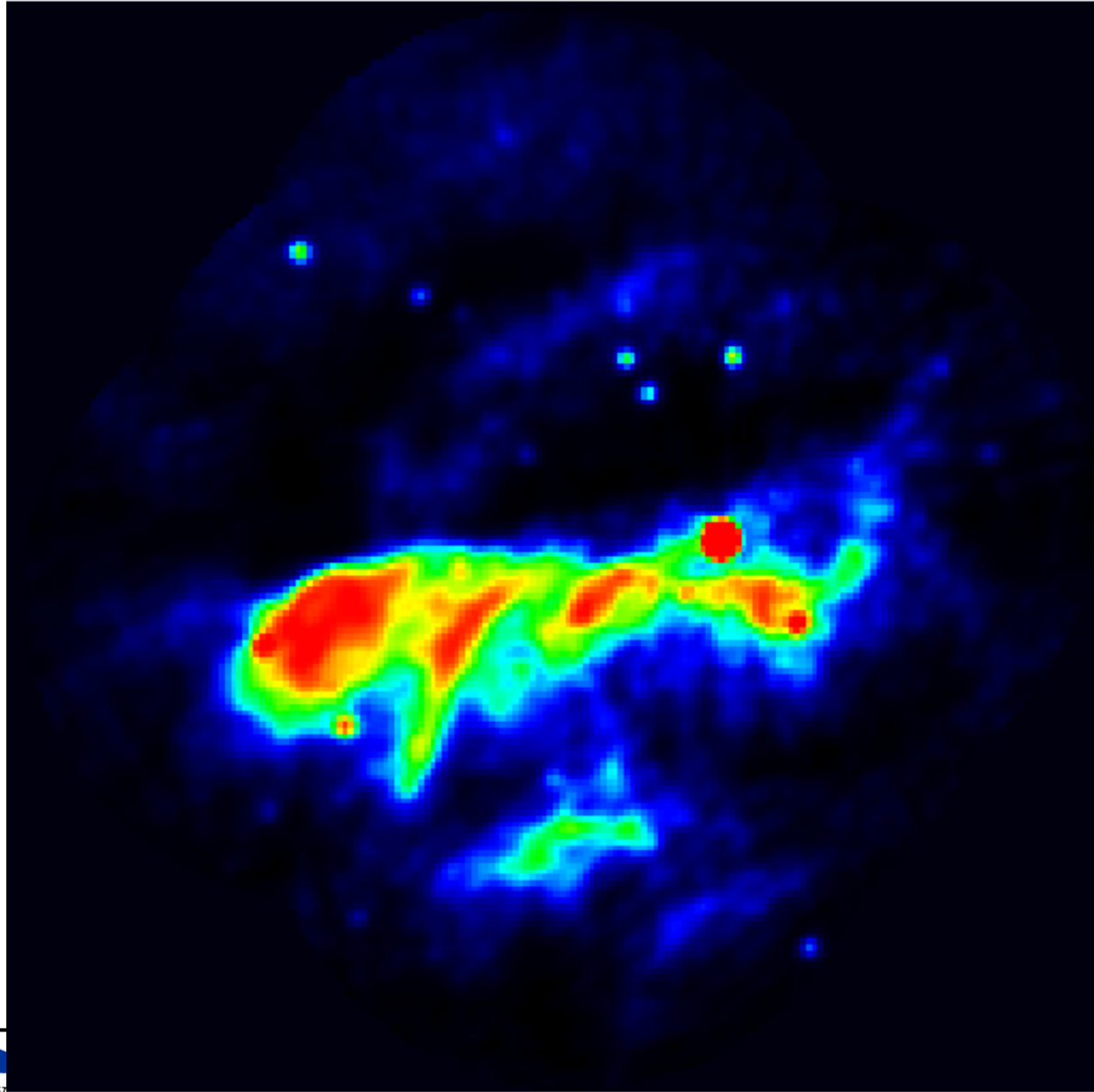


# The Individual Approach

- Treat each pointing separately
- Image each pointing
- Deconvolve each pointing
- Stitch together linearly with weights for primary beam

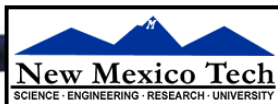
$$I(\mathbf{x}) = \frac{\sum_p A(\mathbf{x} - \mathbf{x}_p) I_p(\mathbf{x})}{\sum_p A^2(\mathbf{x} - \mathbf{x}_p)}$$

# Mosaicing: Linear Combination of Images



# Mosaicing: Linear Combination of Images

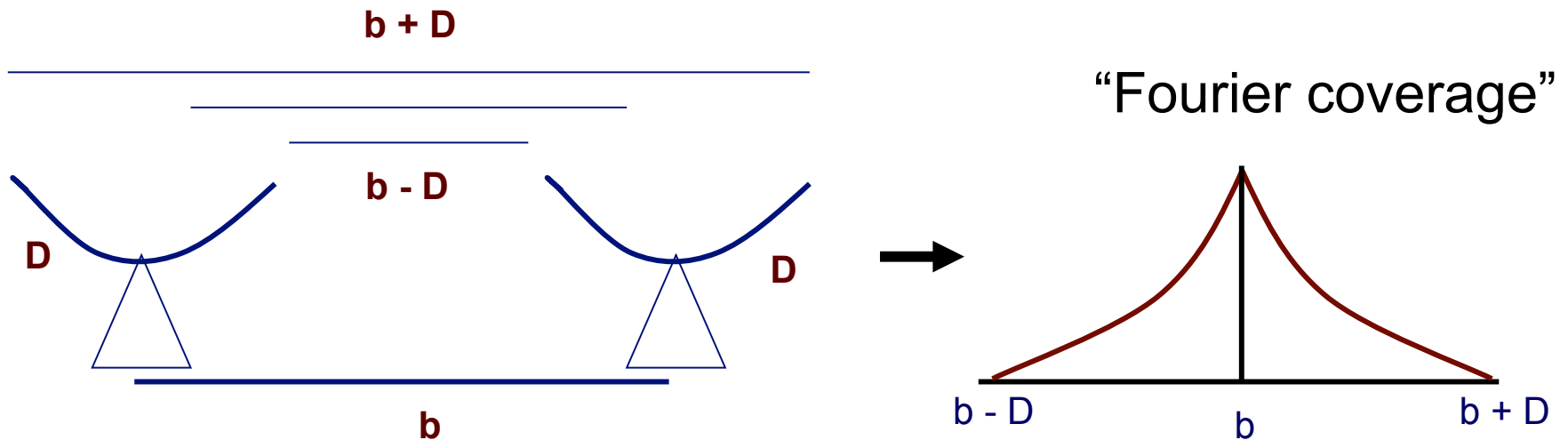
- Most straightforward method to create a mosaic map
- But deconvolution is **non-linear**
- Artifacts, in particular at edges may creep in
- Does not use the improved uv-coverage of overlapping regions (and does not take advantage of Ekers-Rots effect)
- Might be the best solution for high-dynamic range imaging
  - It is possible to manipulate every pointing extensively (e.g. solve for off-axis gains, like ‘peeling’; or different deconvolution parameters for different pointings)
  - Depends less on the exact knowledge of primary beam shape when massively oversampled





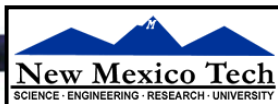
# Ekers & Rots Theorem

- An interferometer doesn't just measure angular scales  $\theta = \lambda / b$  it actually measures  $\lambda / (b - D) < \theta < \lambda / (b + D)$



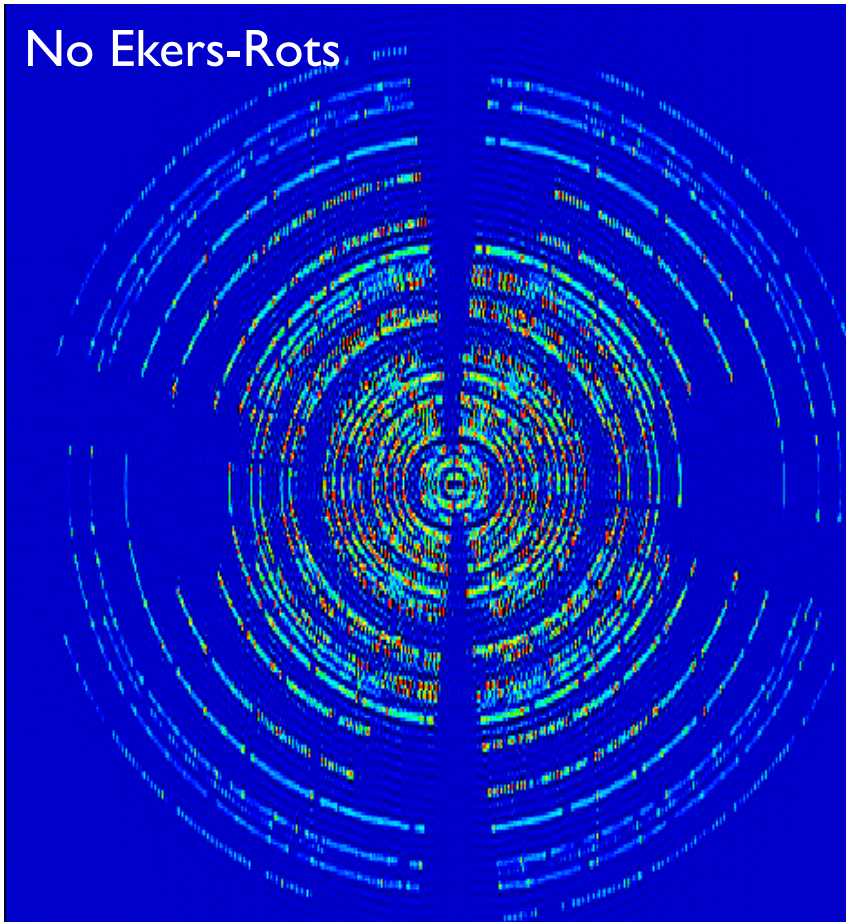
# Ekers & Rots Theorem

- Sounds great but you can't get all that extra info from a single visibility
- Interferometer measures a number per baseline and integration time, not a range
- Similar to a single dish, you have to scan to get the extra “spacings”
- Mosaicing is a way to perform this scanning and unlocks the extra information
- The sampling theorem states that the maximum gain is by sampling the sky with a regular, at least Nyquist spaced grid
- **Ekers-Rots is equivalent to a convolution of the FT of the primary beam with the interferometric visibilities in the uv plane for Nyquist sampled data**

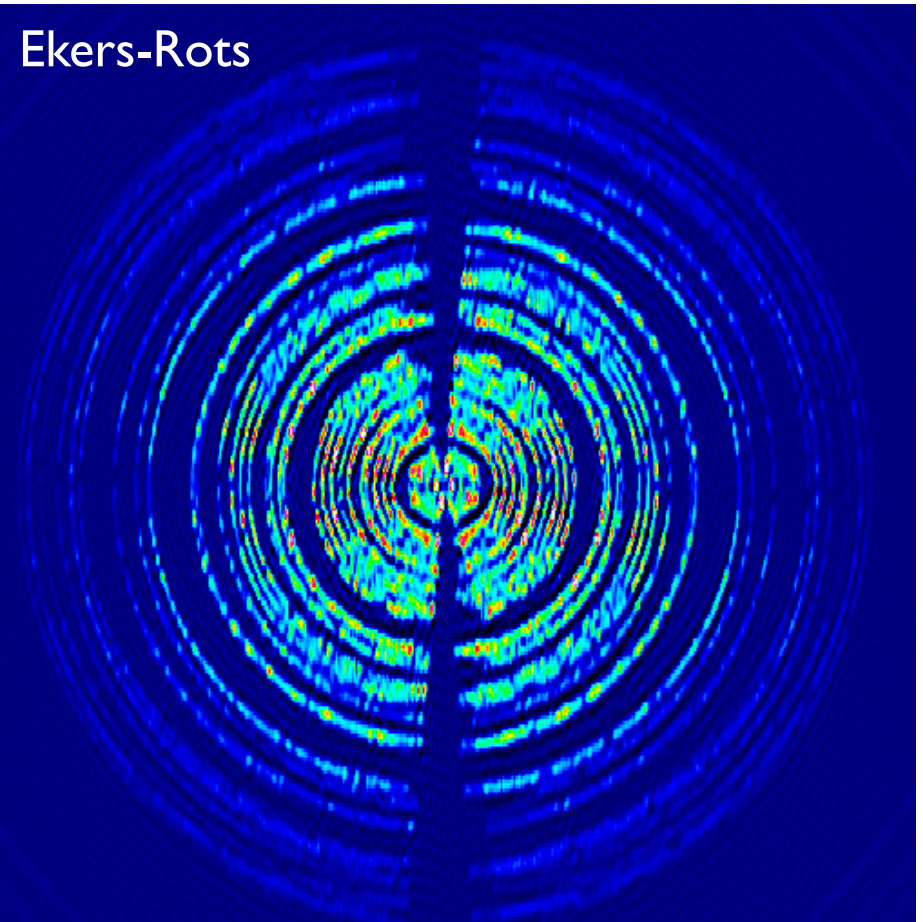


# Comparison of $u$ - $v$ coverage

No Ekers-Rots



Ekers-Rots





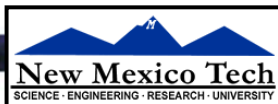
# Joint Deconvolution

- Form a linear combination of the individual pointings,  $p$  on

**DIRTY IMAGE:**

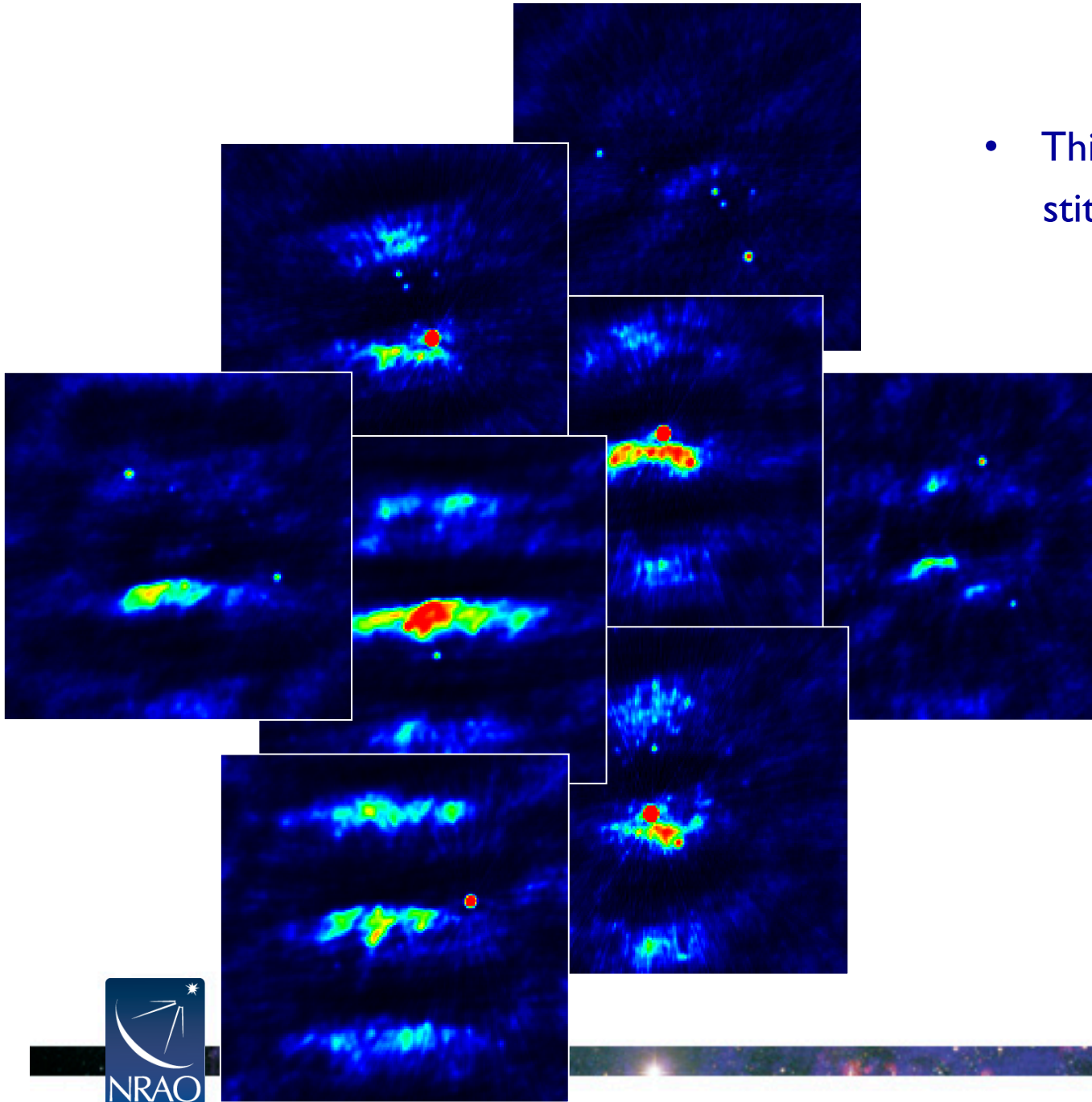
$$I(\mathbf{x}) = W(\mathbf{x}) \frac{\sum_p A(\mathbf{x} - \mathbf{x}_p) I_p(\mathbf{x}) / \sigma_p^2}{\sum_p A^2(\mathbf{x} - \mathbf{x}_p) / \sigma_p^2}$$

- Here  $\sigma_p$  is the noise variance of an individual pointing and  $A(\mathbf{x})$  is the primary response function of an antenna (primary beam)
- $W(\mathbf{x})$  is a weighting function that suppresses noise amplification at the edge of mosaic
- correction for W-projection effects is also required



Sault, Staveley-Smith, Brouw (1996)





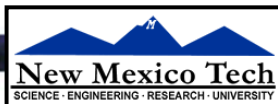
- This time: dirty images to be stitched together

# Mosaicing: Joint Approach

- Joint dirty beam depends on antenna primary beam, ie weight the dirty beam according to the position within the mosaiced primary beams:

$$B(\mathbf{x}; \mathbf{x}_0) = W(\mathbf{x}) \frac{\sum_p A(\mathbf{x}_0 - \mathbf{x}_p) B_p(\mathbf{x} - \mathbf{x}_0) / \sigma_p^2}{\sum_p A^2(\mathbf{x} - \mathbf{x}_p) / \sigma_p^2}$$

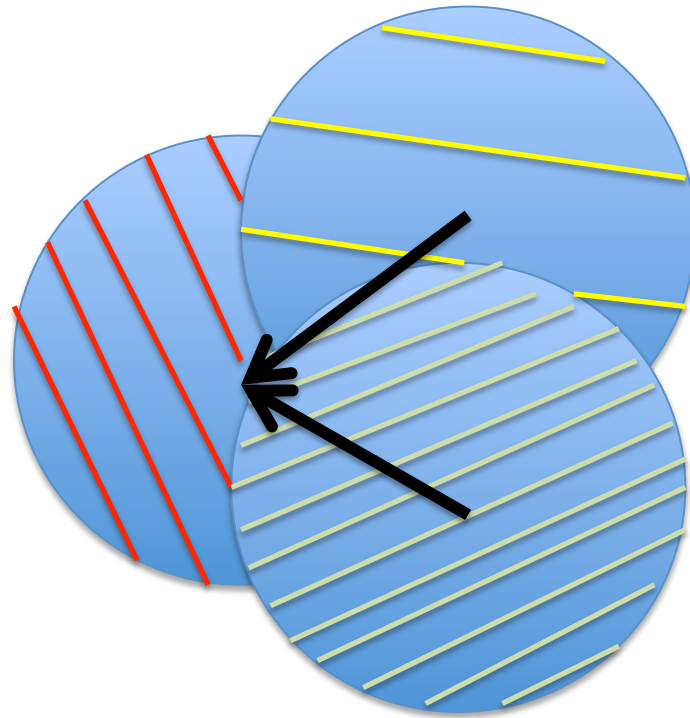
- Uses all *uv* data from all points for the beam simultaneously
  - Combined beam provides better deconvolution in overlap regions
  - Adds in Ekers & Rots spacings: more structure recovered, better beam
  - Overlapping pointings require good knowledge of PB shape further out than the half power point
  - Applies W-projection





# Widefield Imaging

- Take each uv data for each pointing and regrid to a common phase reference center



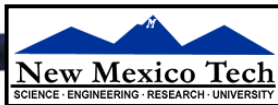
# Widefield Imaging

- Next Step: Perform weighting for primary beam(s)
- Multiplication in image domain = convolution in FT domain

$$I = \sum_p A_p I_p \quad (+ \text{ weighting terms})$$

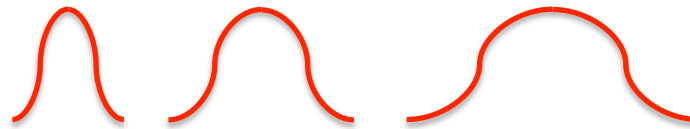
$$FT\{I\} = \sum_p FT\{A_p\} \otimes FT\{I_p\}$$


- The PBs for each pointing are identical but shifted
- FT of a shift is a phase gradient
- Sum of Phase gradient for each offset pointing \* single  $FT\{A\}$  is the weighting for each visibility to correct for primary beams
- FT to single image with a common synthesized “dirty beam”
- The widefield regridding method is also key when dealing with large number of pointings, e.g. in (future) on-the-fly interferometry

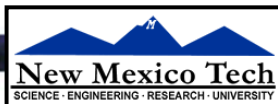


# Deconvolution

- Mosaics can be lots of point like sources but typically are performed for extended emission
- **CLEAN**: subtract dirty beam (point sources) from dirty image  
(Preferably Cotton-Schwab, with small gain; FFT of major cycle will reduce sidelobes)
- **Multiscale clean**: Use a number of kernel sizes for different scales



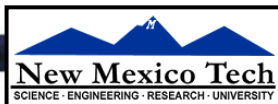
- **Maximum entropy**: iterate on minimizing  $\chi^2$  between data and a model, fit for maximum smoothness





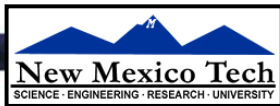
# Mosaicing in CASA

- Most of the tricky techniques are performed under the hood for your convenience
- Calibrate as you would do for a single pointing
- Use the **clean** task with your favorite parameters
- In *imagermode* use '*mosaic*'
- Use *ftmachine*='ft' for joint deconvolution, '*mosaic*' for the widefield imaging
- Use *psfmode*='clark' for Cotton-Schwab Algorithm
- Fill in '*multiscale*' parameters (scales) for MS Clean
- Maximum Entropy and linear mosaicing of cleaned images are only available from the CASA toolkit at this moment
- Contributed tasks for mosaicing setups – also check ALMA OT/JVLA OPT



# Practical Considerations

- What grids to use?
- How often to come back to a individual pointing
- Slew time of Antennas
- Change of atmospheric conditions



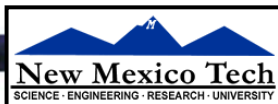
# Practical Consideration: Sensitivity/Primary Beam/Pointing

- Pointings overlap which increases the sensitivity per position. For a fixed time observation the total noise is

$$\sigma_t \sim \sigma_p \sqrt{n} / 1.4$$

where n is the number of pointings

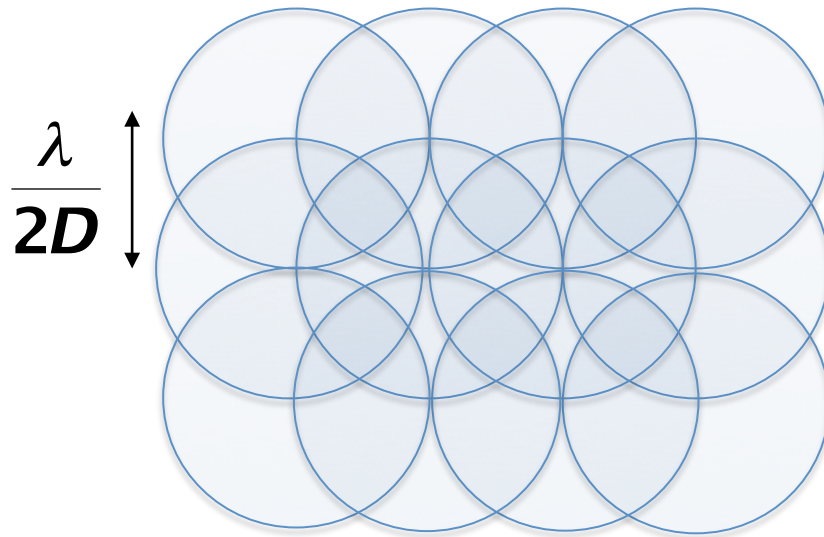
- Mosaicing requires a good model of the primary beam in particular for less-dense packings
- For wide band mosaicking best to use the highest frequency for your pointing positions but some compromise is possible; for less dense packings W-projection becomes more important
- Pointing errors are **first order in mosaics** (only second order in single pointing observations of sources smaller than primary beam)



# Practical Consideration: Choice of Grid

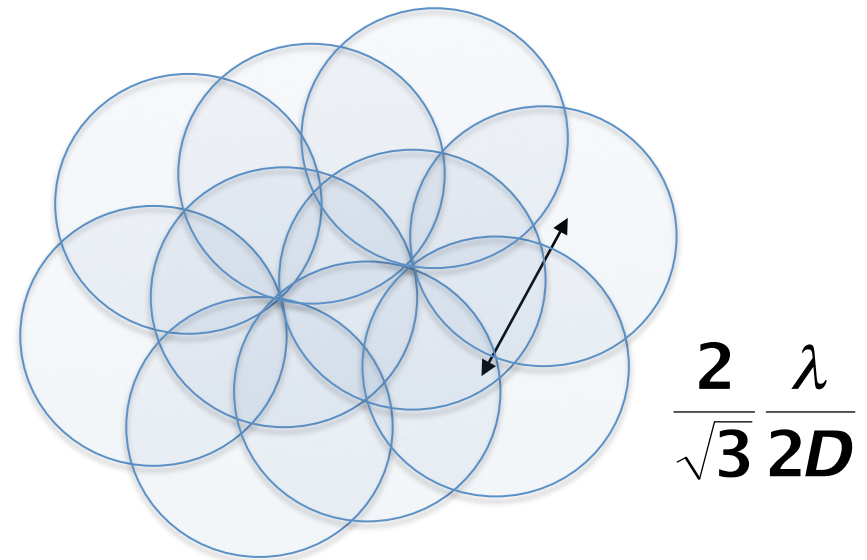
- Different ways to layout the grid on the sky:
- Nyquist sampling:

## Rectangular grid



Minimum Nyquist for structure information recovery

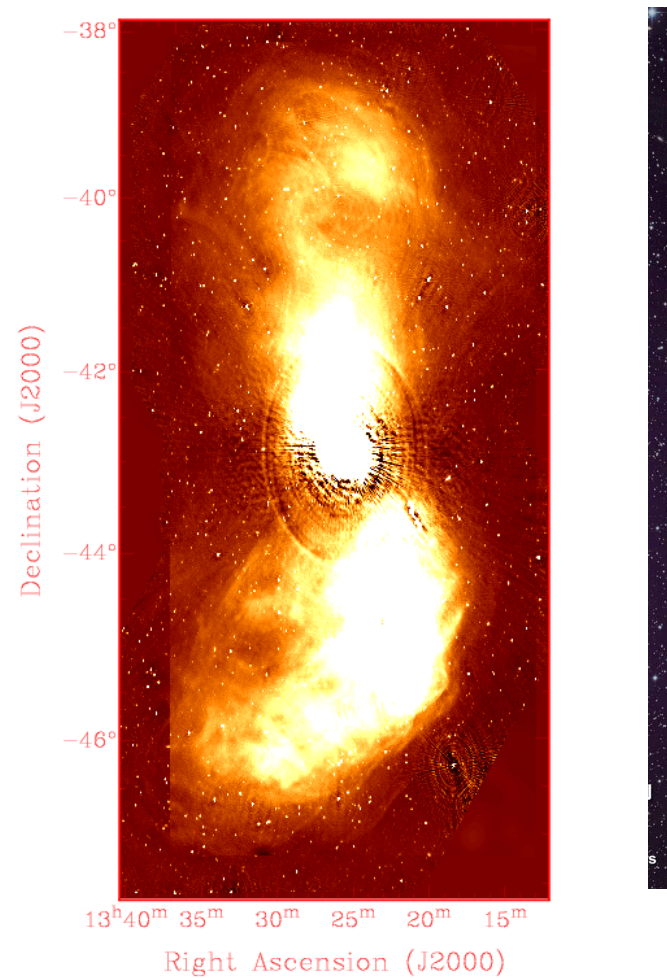
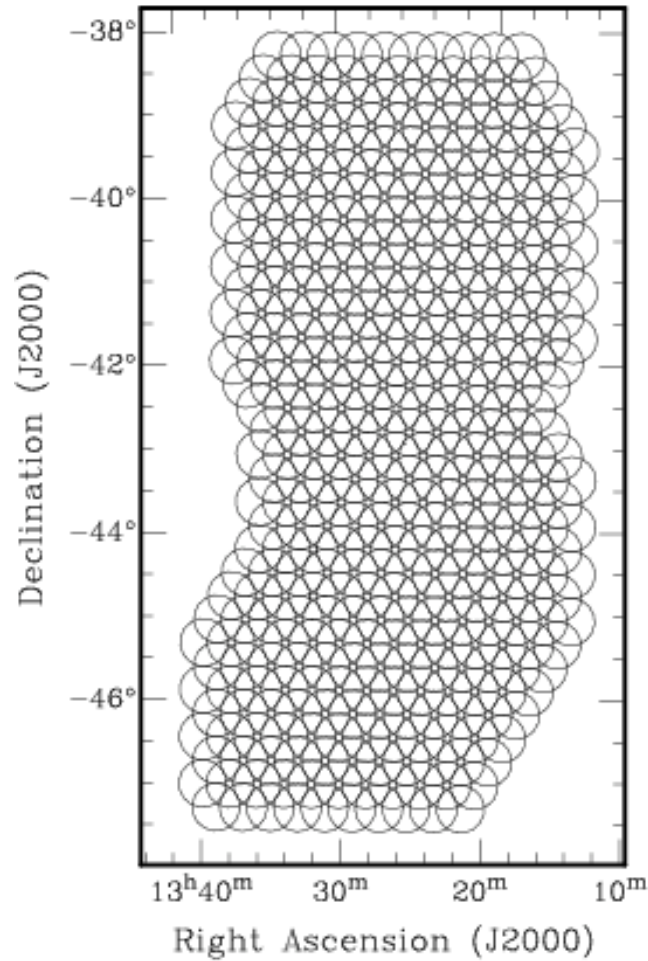
## Hexagonal grid



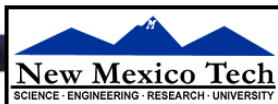
Oversampled but every position at least covered three times, best for uniform noise, but many pointings are needed



# Centaurus A: 406 pointings



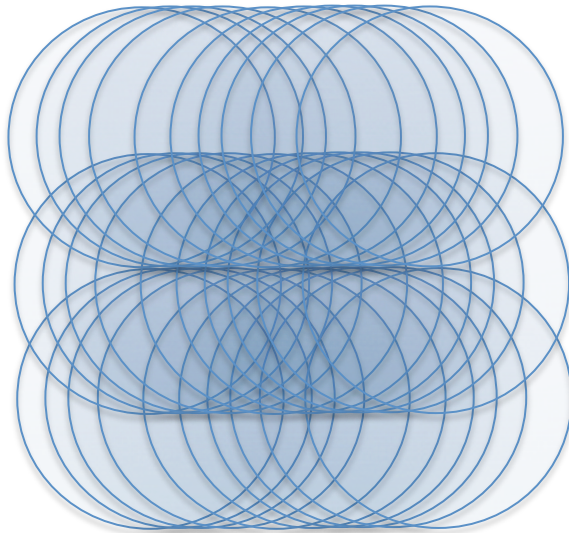
Feain et al. 2011



# Practical Consideration: Choice of Grid

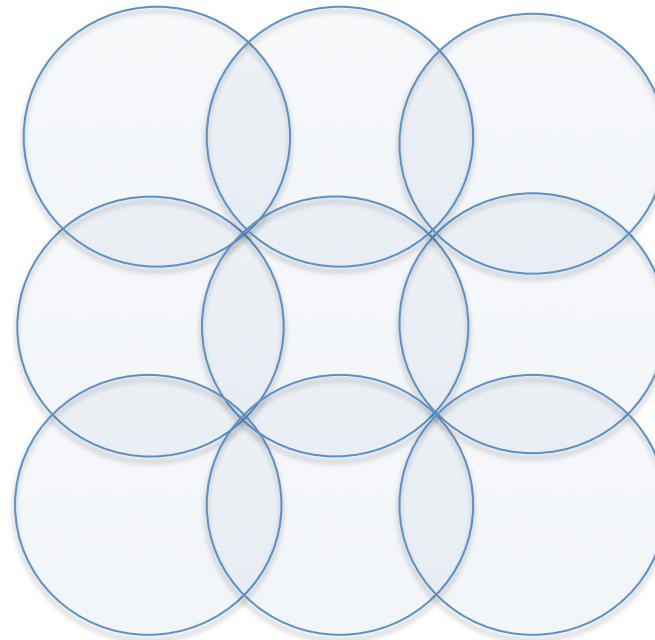
- On-The-Fly Interferometry
- Non-Nyquist sampling

OTF



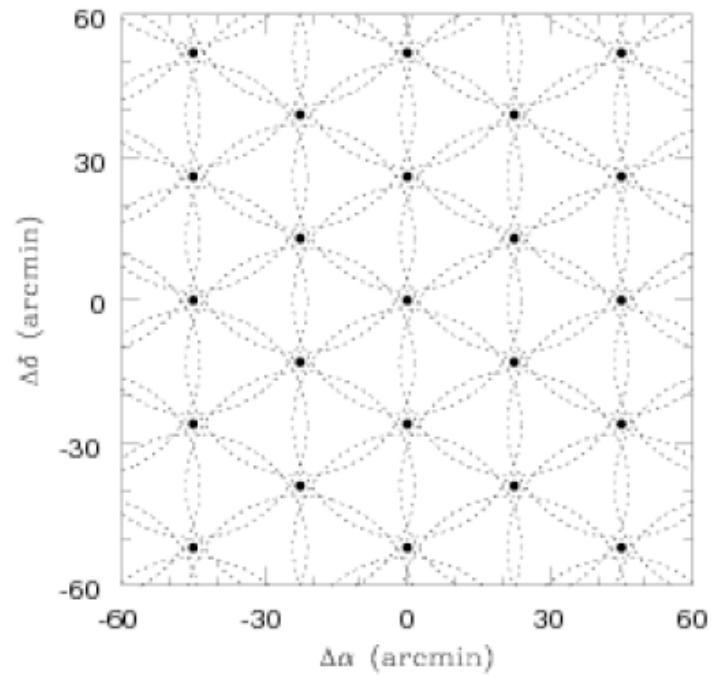
Scan does not stop, fast dumping of data, influences the primary beam shape, produces lots of data but reduces overhead

Non-Nyquist

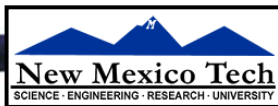
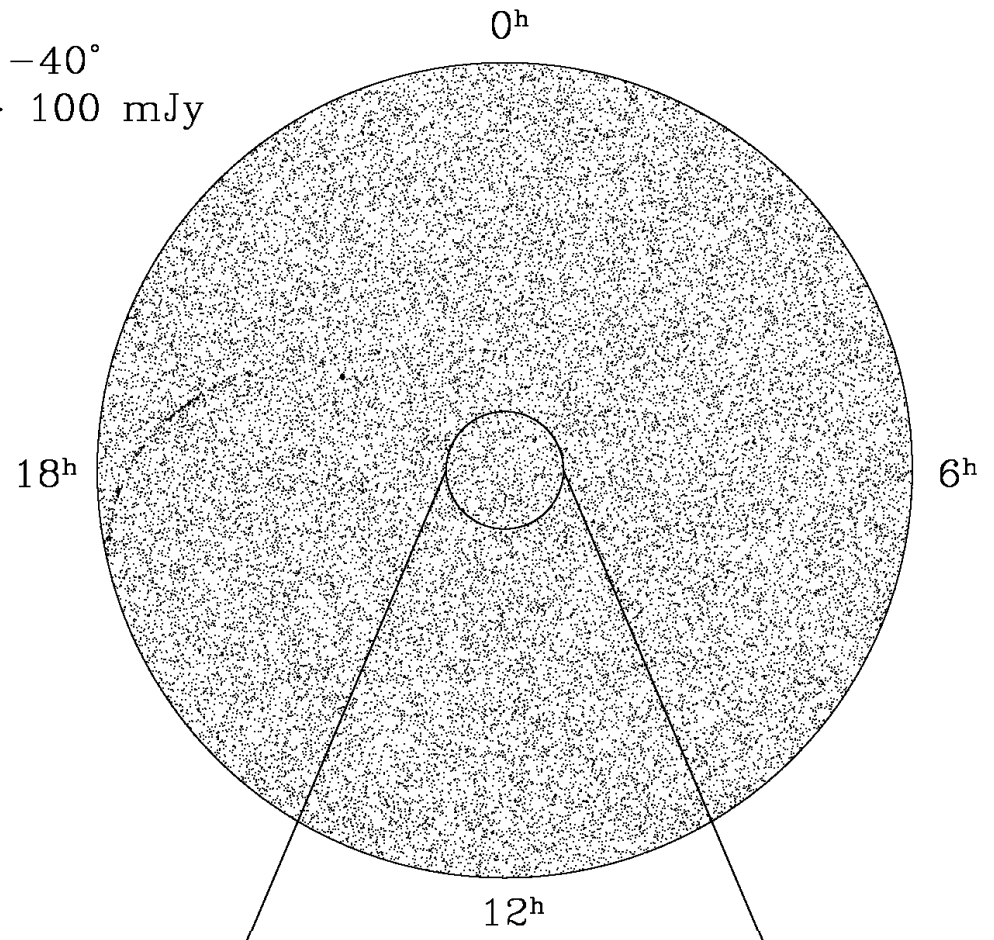


Basic, fast sky coverage

# NVSS: 217,446 pointings

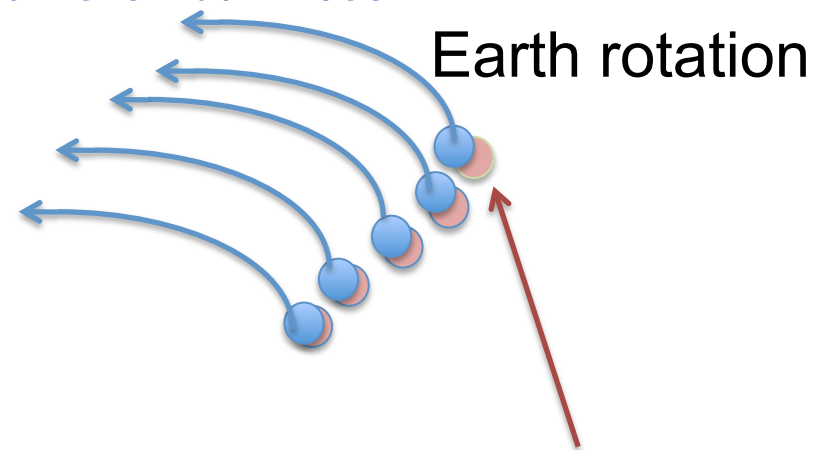
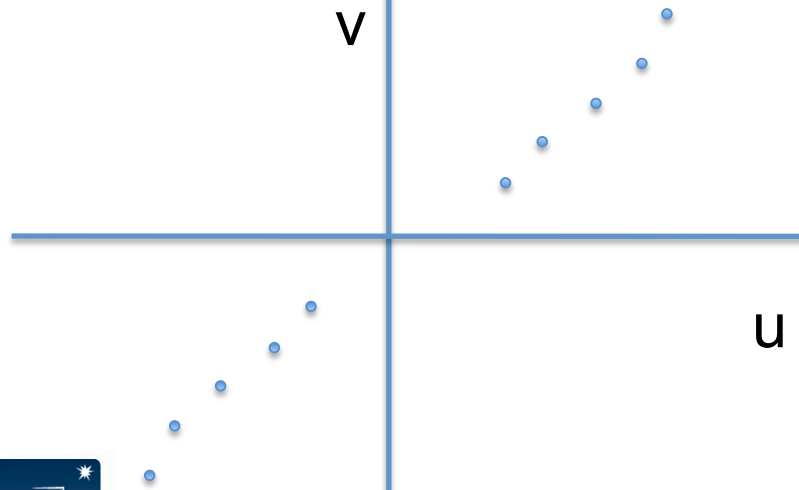


$\delta > -40^\circ$   
 $S > 100 \text{ mJy}$

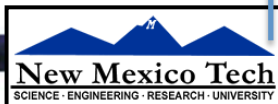


# Practical Considerations: Nyquist $uv$ structure sampling

- How often to visit a pointing?
- One baseline measures region in  $uv$  plane with size  $2D$
- Want adjacent samples to be completely independent
- At transit, the time between independent points is  $\tau = (86400 / 2\pi)(2D / L)$  sec, where  $D$  = antenna diameter,  $L$  = longest baseline
- Nyquist sampling for  $N$  pointings: dwell time is  $\tau/2N$  sec

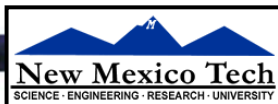
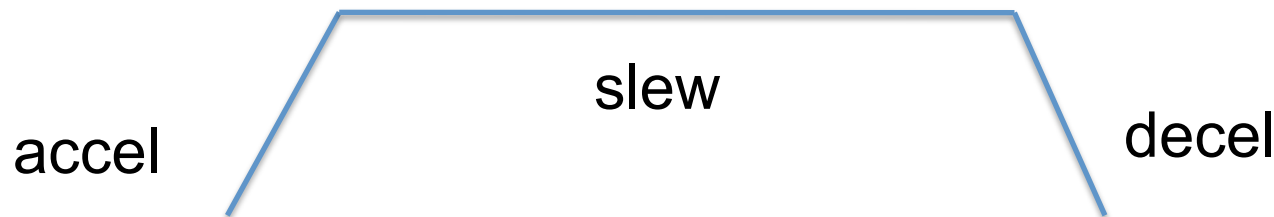


Nyquist sample



# Practical Consideration: Slew Time

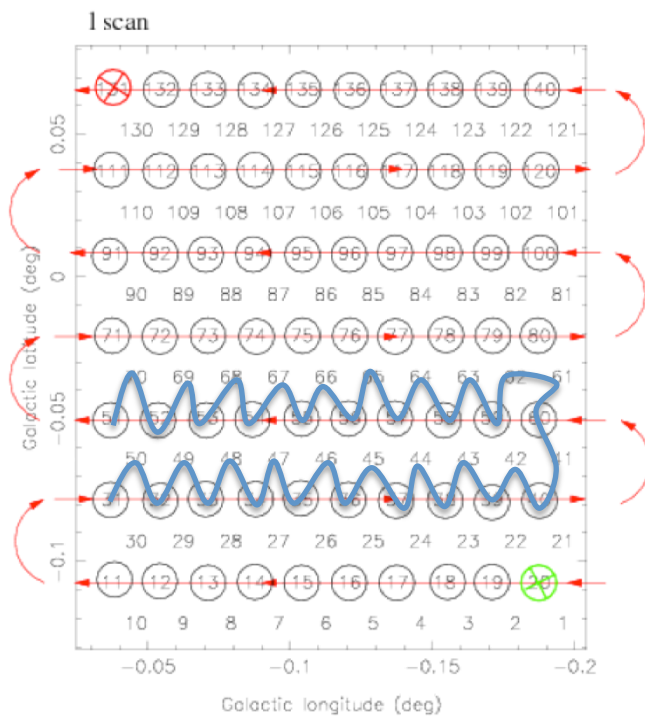
- Telescope slew times are calculated by:
- Acceleration
- Constant Slew velocity
- Deceleration
- Settling time
- Some telescopes may have variations in Az and El
- JVL A: acceleration:  $2.2 \text{ deg s}^{-2}$ , slew rate:  $20 \text{ deg min}^{-1}$  in El, 40 in Az
- Settling time:  $\sim 1\text{-}3\text{s}$  shorter in El, longer in Az
- ALMA: acceleration:  $24 \text{ deg s}^{-2}$ , slew rate  $180 \text{ deg min}^{-1}$  in El, 360 in Az



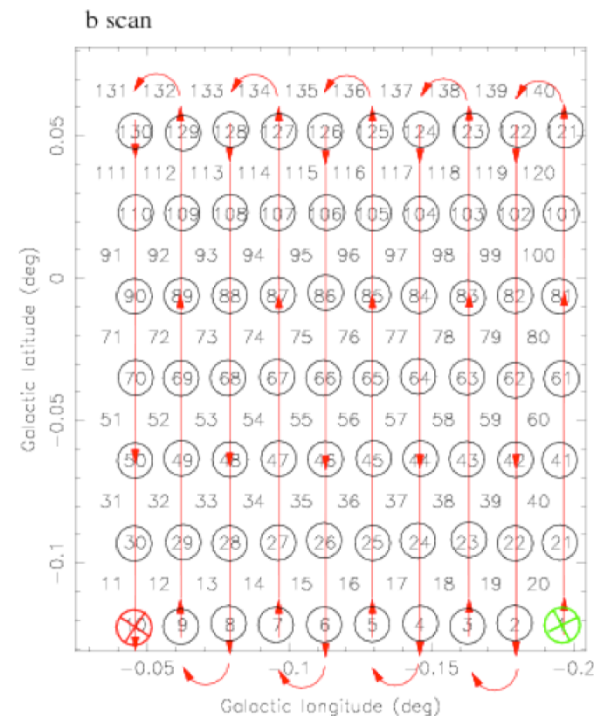


# Practical Considerations: Slew time vs uv-coverage

ATCA Galactic Center NH<sub>3</sub> survey



70 Pointings a 30sec total time 35min

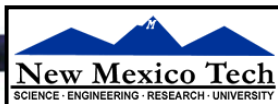


70 Pointings a 30sec total time 35min

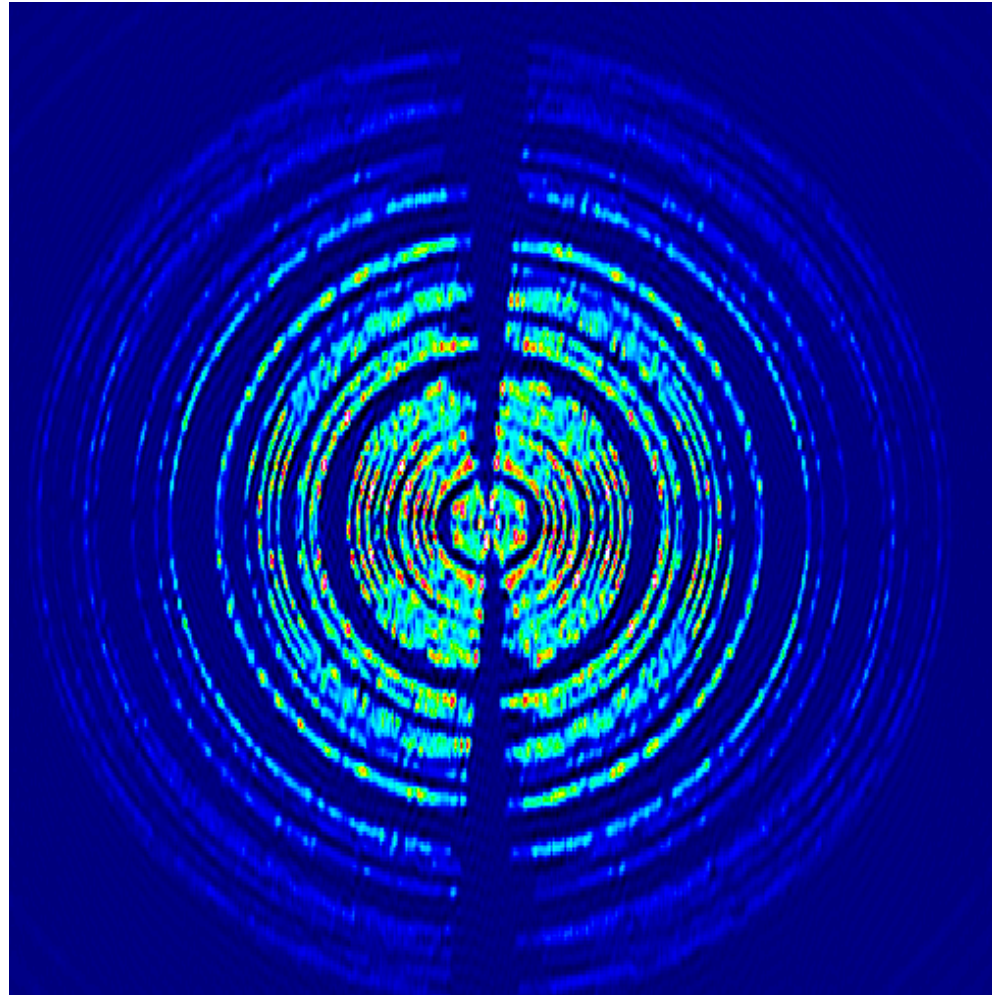


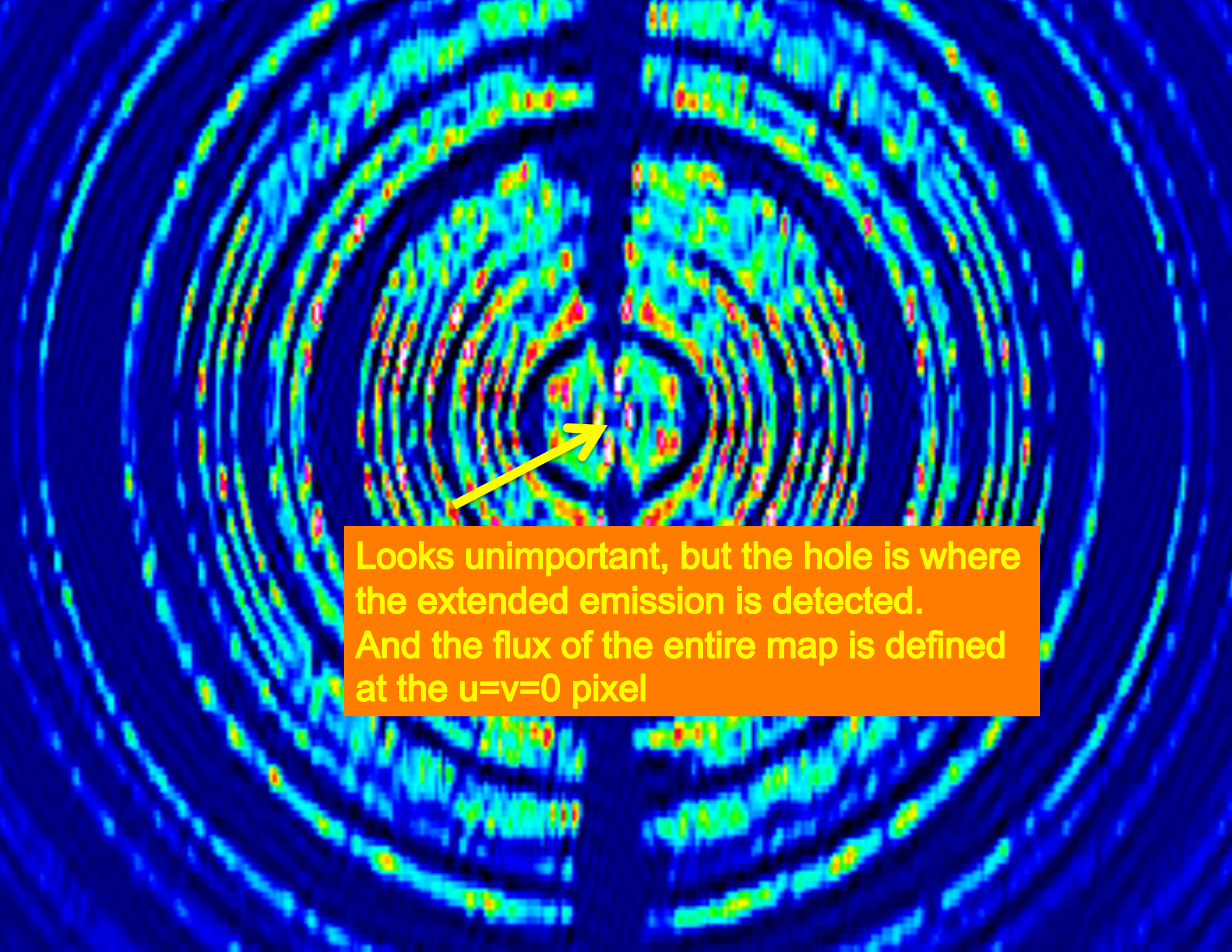
# Practical Consideration: Changing Atmosphere (Ionosphere)

- The water vapor content of the atmosphere can change on small timescales
  - In particular there can be large variations in individual cells
    - Changing sky brightness
    - Changing opacity
    - Increased phase noise
  - Delay variations due to ionosphere are possible at low frequencies
- Try to cover the full mosaic fast but more frequently  
This will make the map more uniform, but it increases your overhead



# Short and Zero Spacing Correction

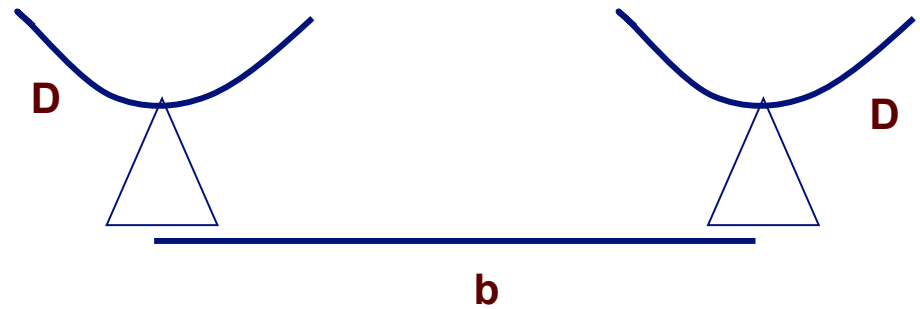




Looks unimportant, but the hole is where the extended emission is detected.  
And the flux of the entire map is defined at the  $u=v=0$  pixel

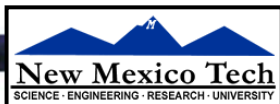


# uv-coverage



- What's the problem with the hole?
- It's the **short baselines**
- They define the largest spatial frequencies, or the largest angular scales that an interferometer is sensitive to
- The field of view is given by the beam of a single antenna
- The largest angular scale is given by the shortest distance between 2 antennas  $\theta < 2\lambda/d_{\min}$
- Single antenna diameter  $<$  shortest distance
- Field of view  $>$  largest sensitive scale
- Extreme: full flux in field of view is given by the central pixel in the uv-coverage

**Short spacings & zero spacings problem**





# JVLA

## largest angular scale

- Primary beam / field of view:  
45'/ $\nu$  (GHz)

Largest angular scale < field of view

Table 5: Configuration Properties

Configuration	A	B	C	D
$B_{\max}$ (km <sup>1</sup> )	36.4	11.1	3.4	1.03
$B_{\min}$ (km <sup>1</sup> )	0.68	0.21	0.035 <sup>5</sup>	0.035
Synthesized Beamwidth $\theta_{\text{HPBW}}$ (arcsec) <sup>1,2,3</sup>				
74 MHz (4 band)	24	80	260	850
1.5 GHz (L)	1.3	4.3	14	46
3.0 GHz (S) <sup>6</sup>	0.65	2.1	7.0	23
6.0 GHz (C)	0.33	1.0	3.5	12
8.5 GHz (X) <sup>7</sup>	0.23	0.73	2.5	8.1
15 GHz (Ku) <sup>6</sup>	0.13	0.42	1.4	4.6
22 GHz (K)	0.089	0.28	0.95	3.1
33 GHz (Ka)	0.059	0.19	0.63	2.1
45 GHz (Q)	0.043	0.14	0.47	1.5
Largest Angular Scale $\theta_{\text{LAS}}$ (arcsec) <sup>1,4</sup>				
74 MHz (4 band)	800	2200	20000	20000
1.5 GHz (L)	36	120	970	970
3.0 GHz (S) <sup>6</sup>	18	58	490	490
6.0 GHz (C)	8.9	29	240	240
8.5 GHz (X) <sup>7</sup>	6.3	20	170	170
15 GHz (Ku) <sup>6</sup>	3.6	12	97	97
22 GHz (K)	2.4	7.9	66	66
33 GHz (Ka)	1.6	5.3	44	44
45 GHz (Q)	1.2	3.9	32	32

36500

1800

900

450

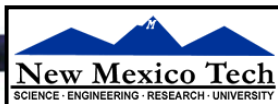
320

180

120

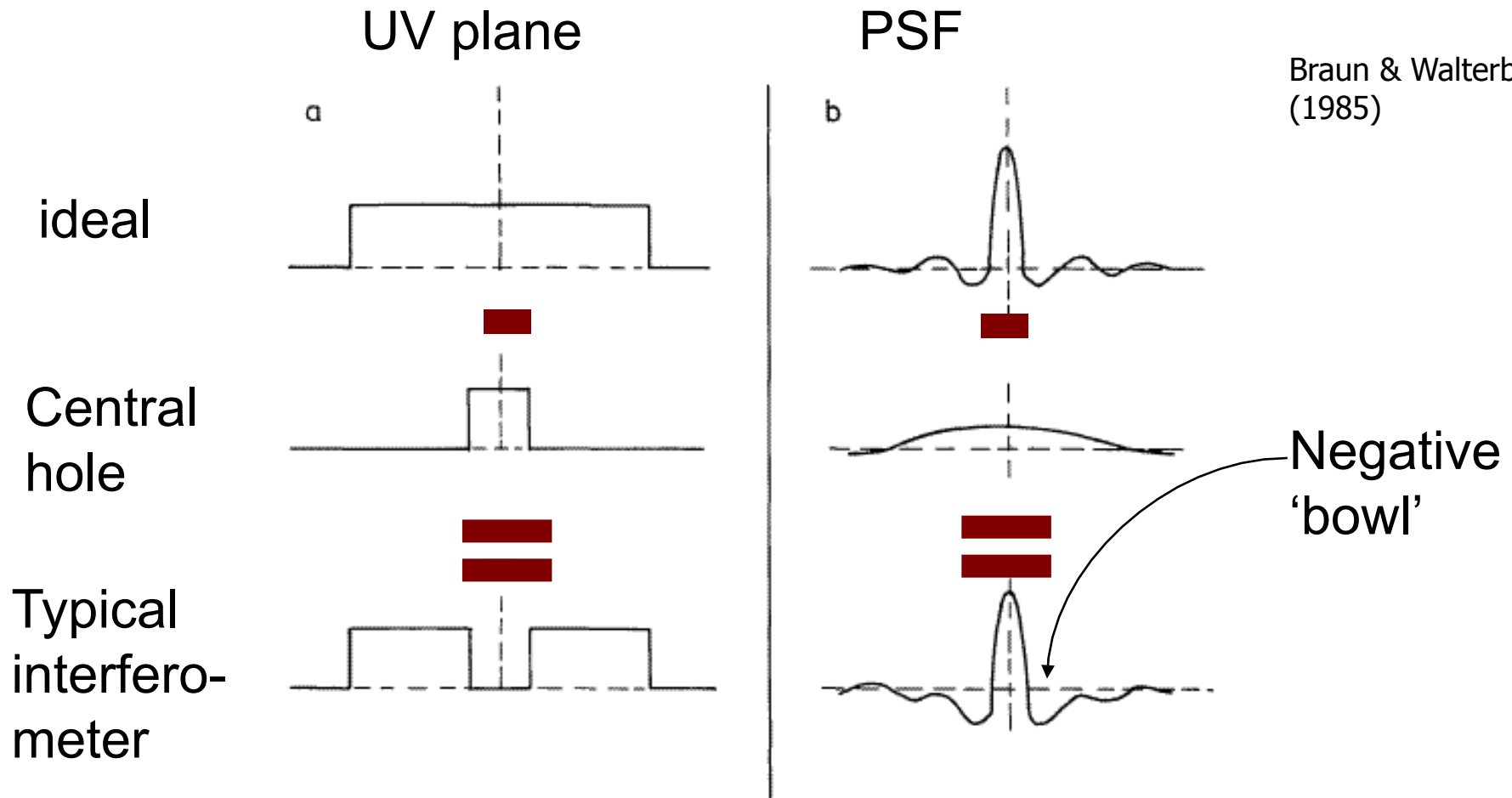
80

60



# The short(zero)-spacing problem

Braun & Walterbos  
(1985)

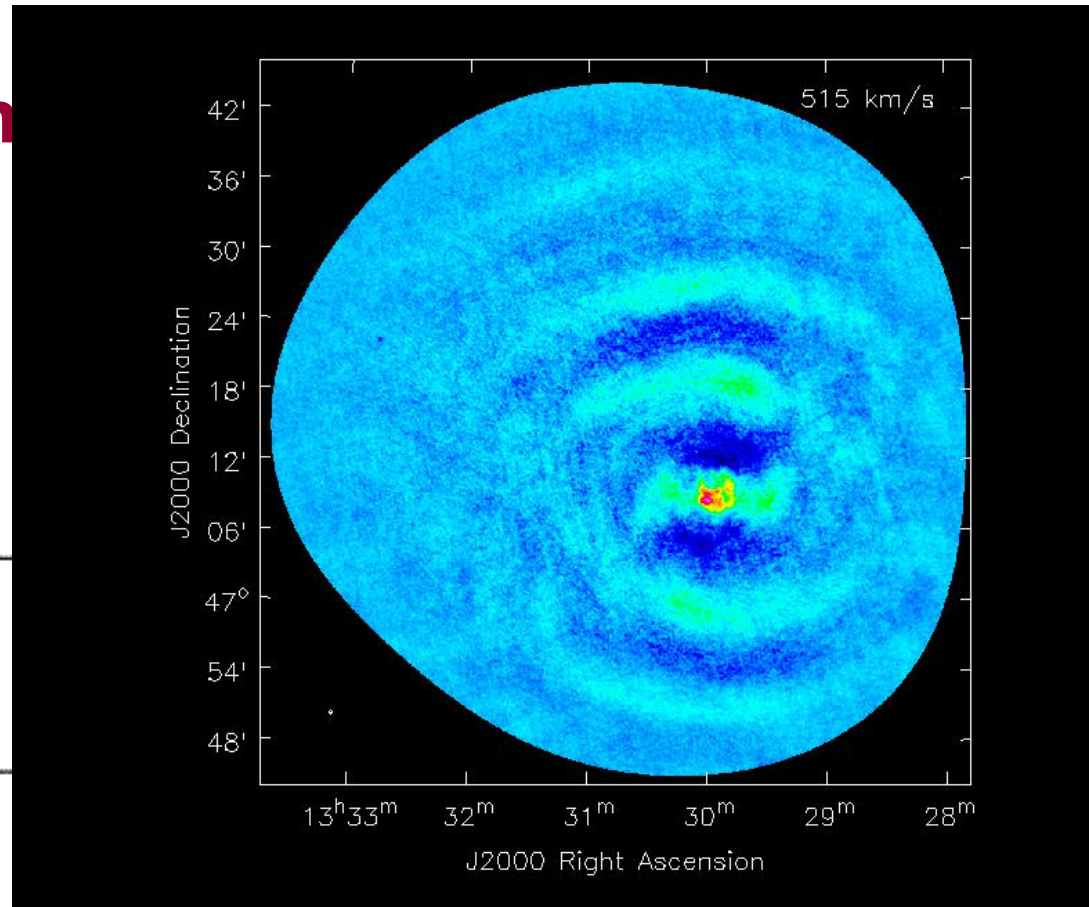


The sh

ideal

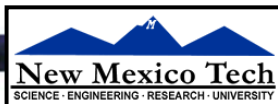
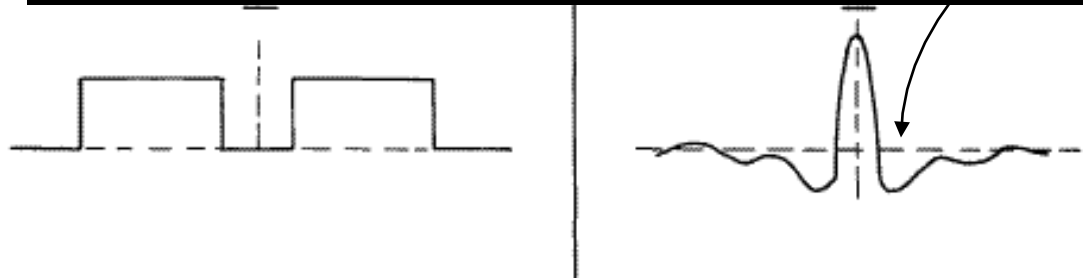
Central  
hole

Typical  
interfero-  
meter



Braun & Walterbos  
(1985)

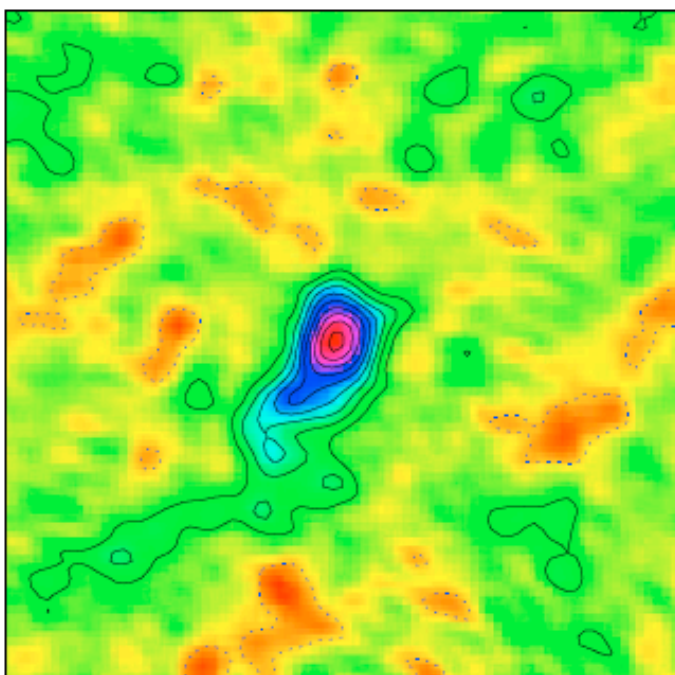
Negative  
'bowl'



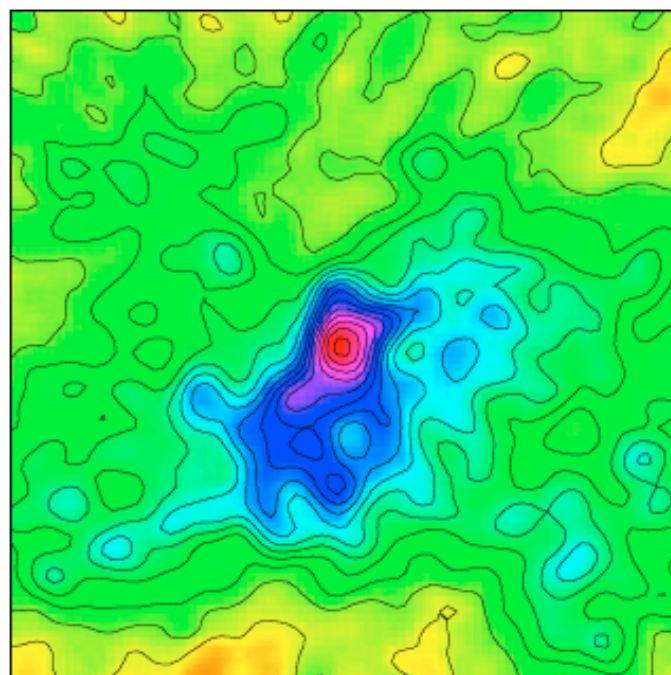


## Short Spacings Example

Without short spacings



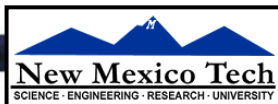
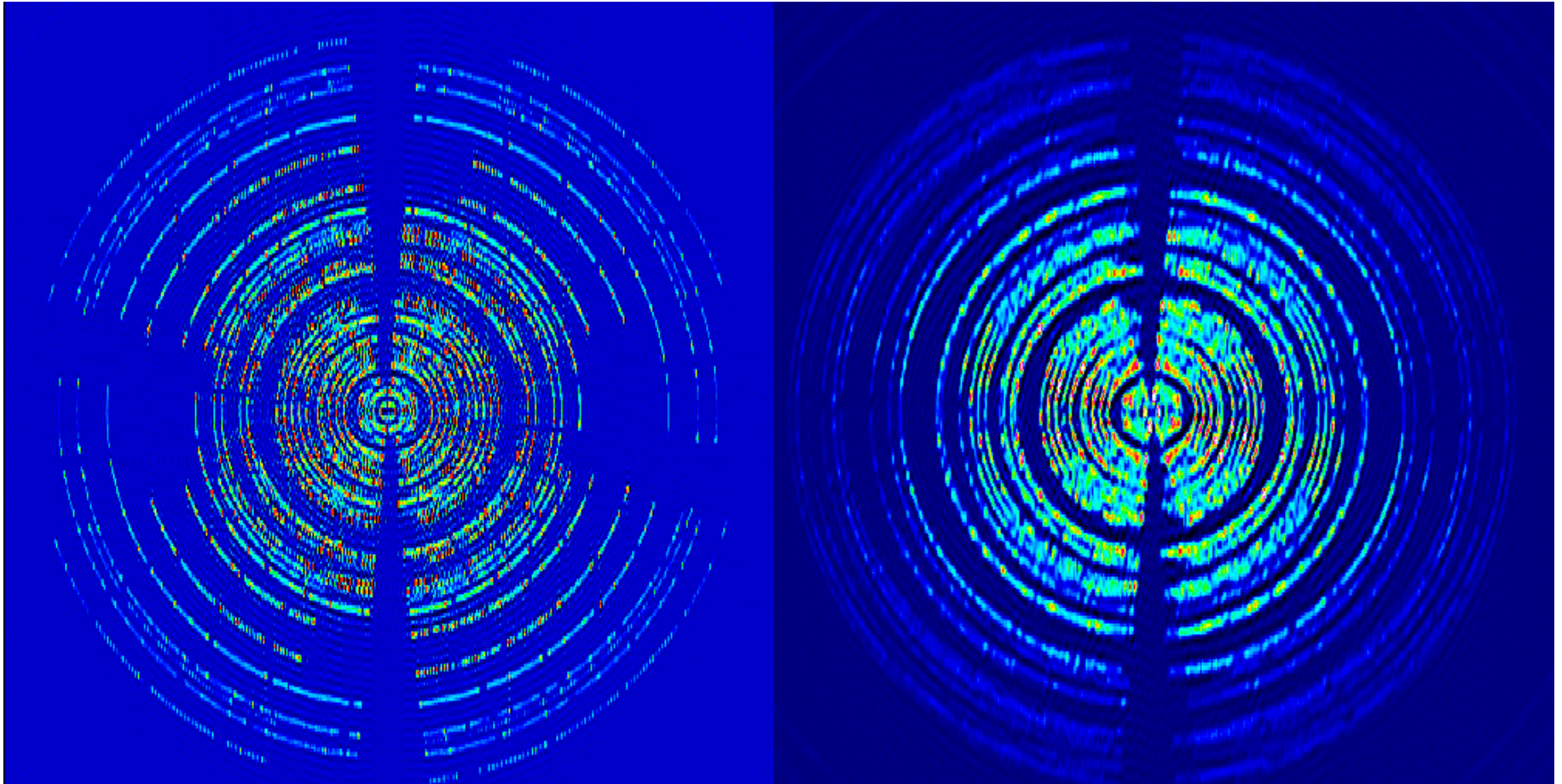
With short spacings



$^{13}\text{CO}$  (1–0) in the L1157 protostar (Gueth et al. 1997)



# Ekers-Rots helps



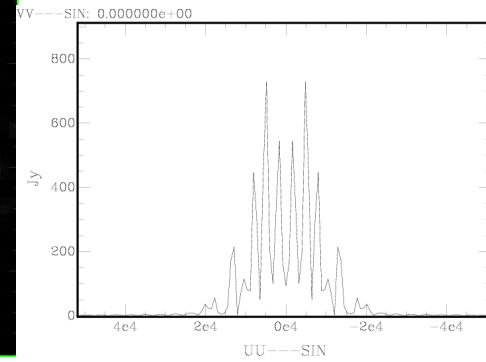
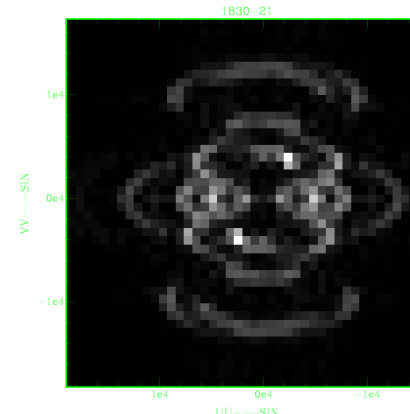
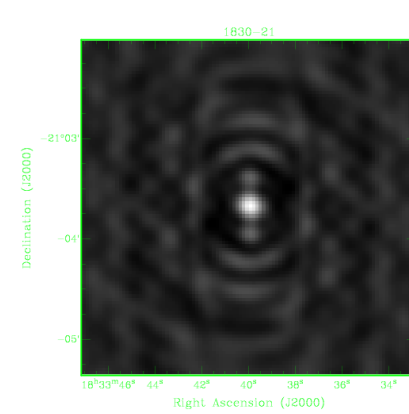


# CLEAN extrapolates short spacings

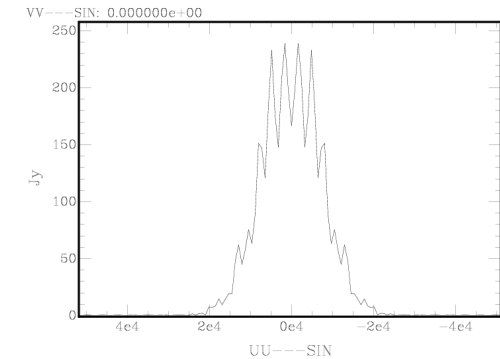
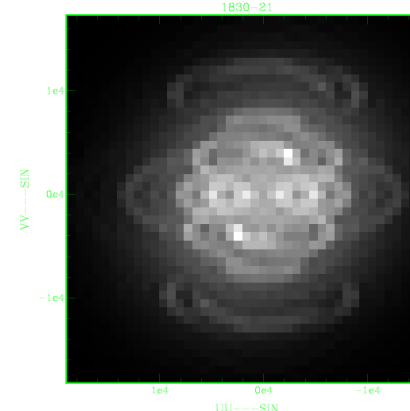
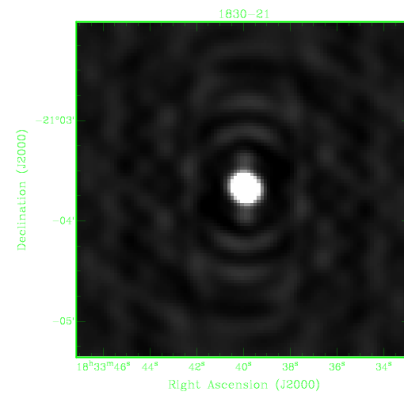
FFT

FFT-slice

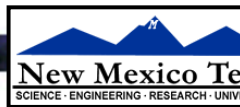
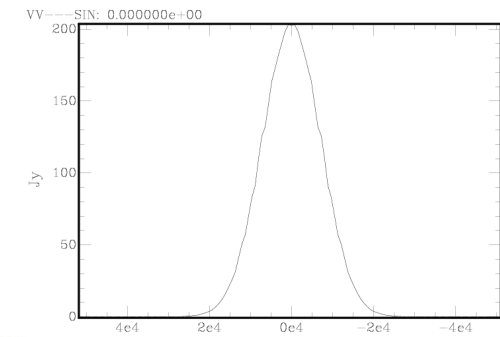
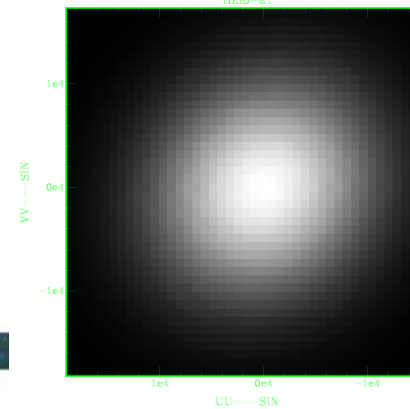
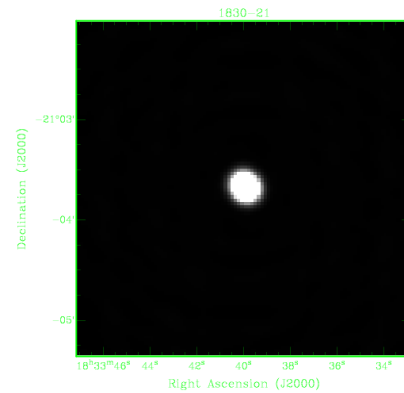
dirty



Few iterations

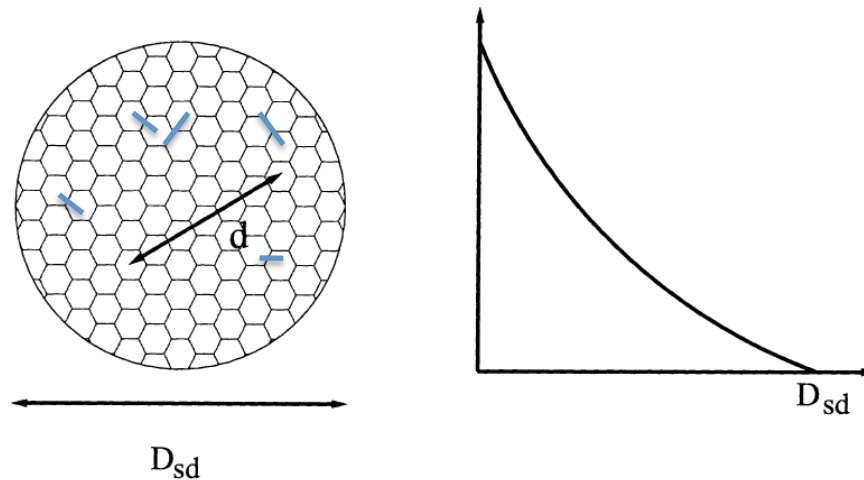


more iterations



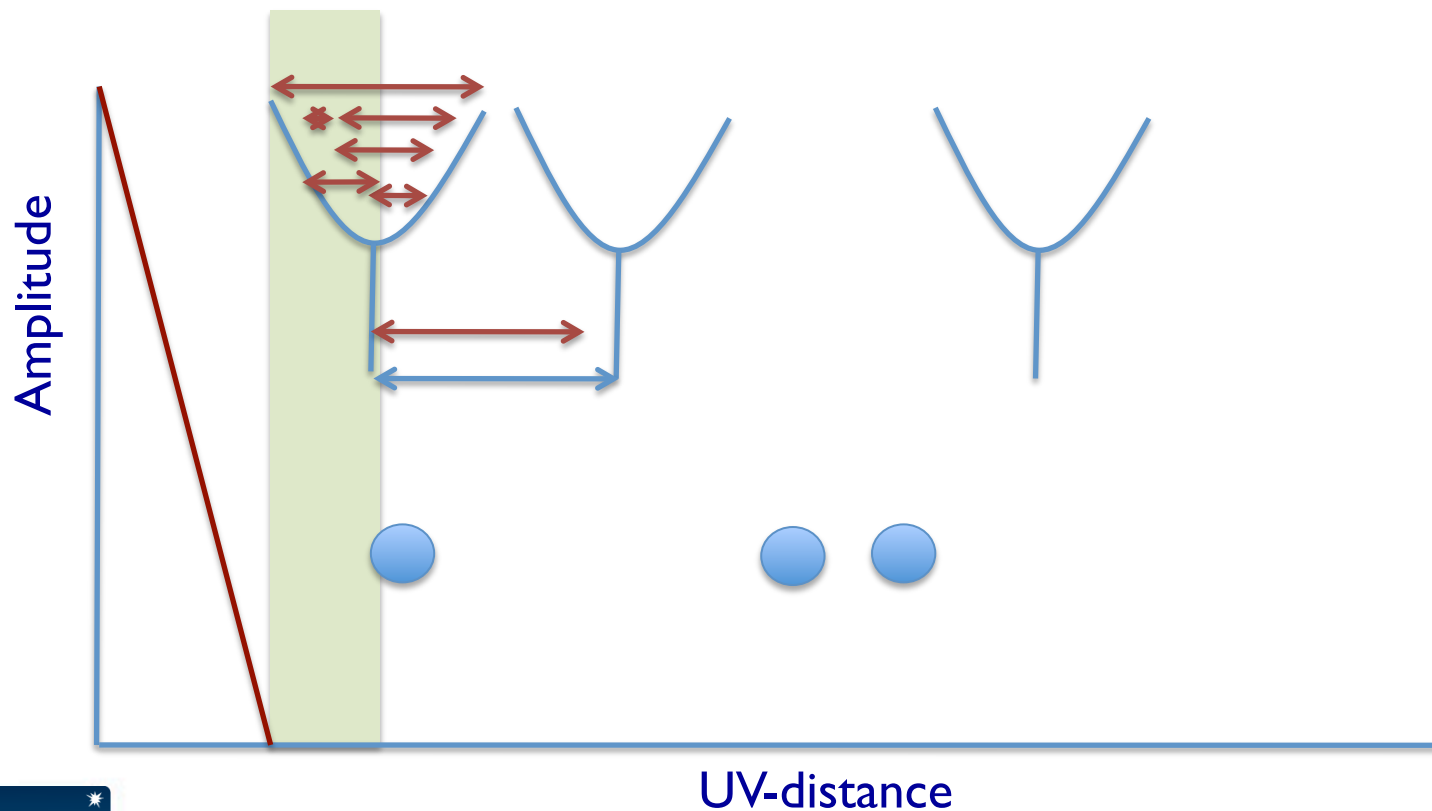
# uv-coverage

- CLEAN **EXTRAPOLATES** to the central short and zero spacings
- But we would like to measure those; can we do that?
- Yes! Use the Fourier magic of a Single Dish



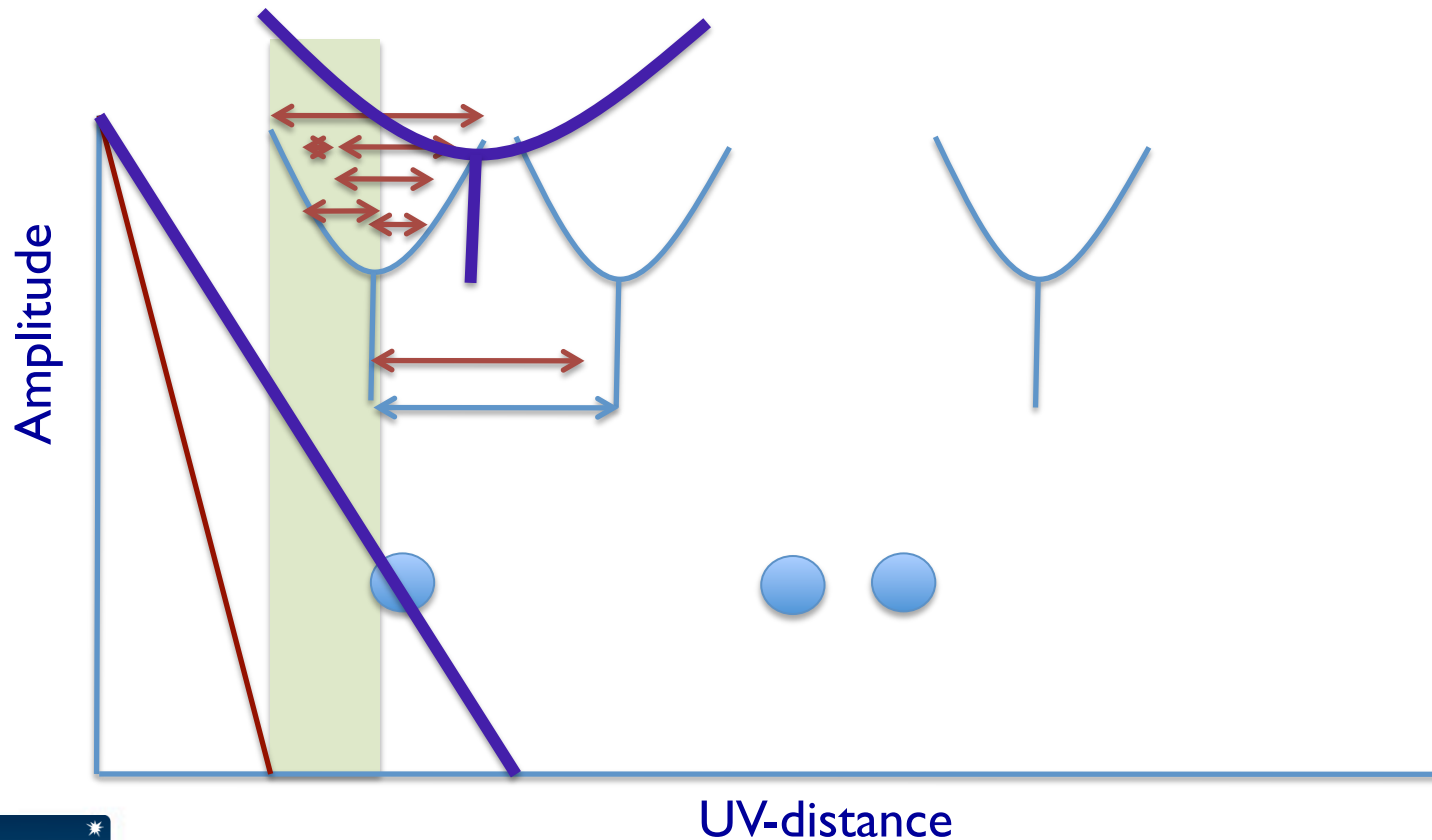
# Zero spacing correction

- Get an interferometric observation
- Go to a single dish and map the same region, use a SD with a diameter larger than the shortest baseline of your interferometric map



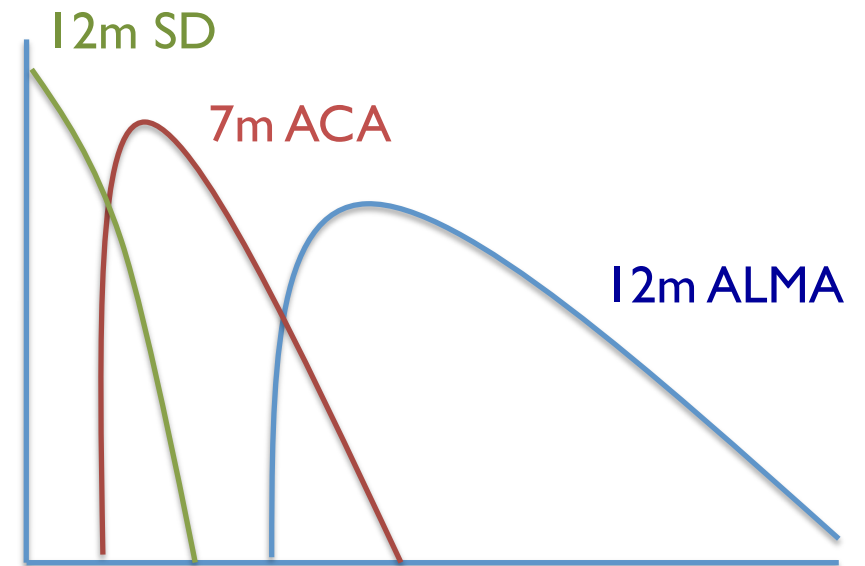
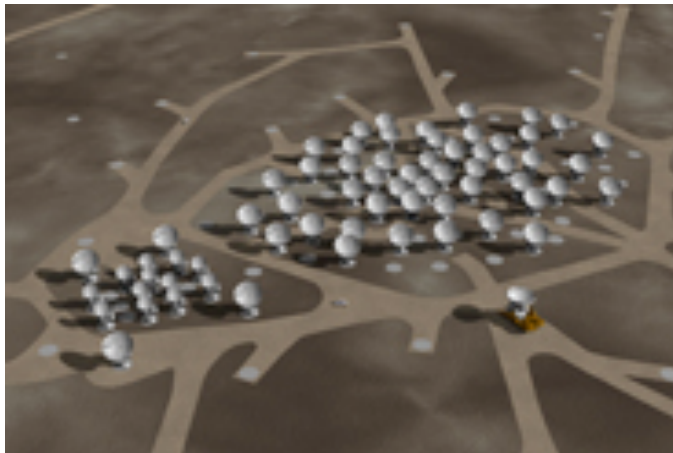
# Zero spacing correction

- Get an interferometric observation
- Go to a single dish and map the same region, use a SD with a diameter larger than the shortest baseline of your interferometric map



# Zero/Short Spacings @ ALMA

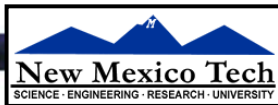
- ALMA approach:
- 12m antennas + 7m antennas +
- 12m antennas that operate as SD



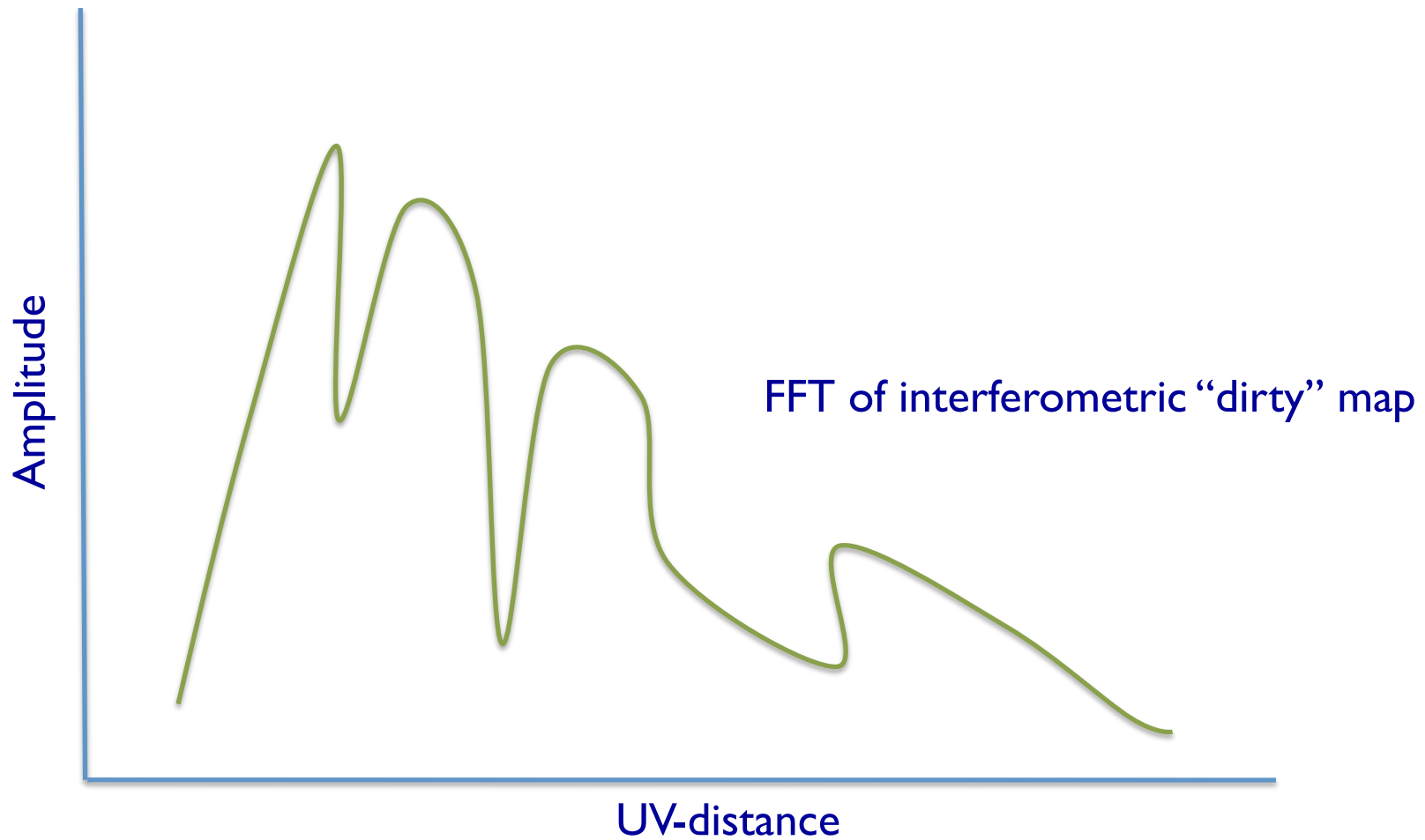


# Zero spacing correction

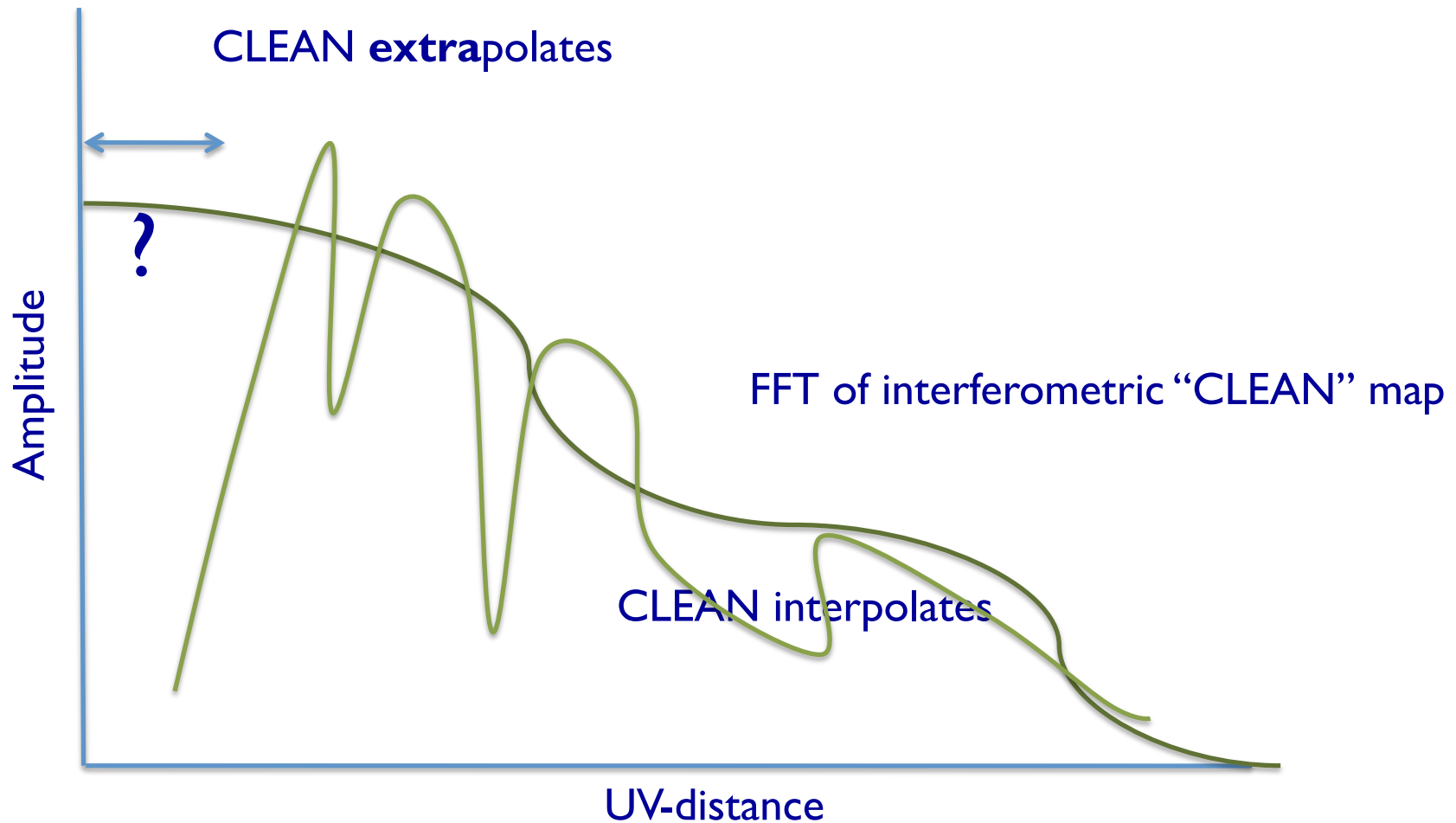
- Get an interferometric observation
  - Go to a single dish and map the same region, use a SD with a diameter larger than the shortest baseline of your interferometric map
  - Aim for same surface brightness sensitivity at shortest BL and SD
  - Calibrate, calibrate, calibrate!
- 
- **Feathering:** FT SD map → FT cleaned, interferometric map → combine both with weighting in uv-space → FT back to combined image
  - Use the SD map as a **model for deconvolution** with (multi-scale-)clean
  - **Minimize Maximum Entropy  $\chi^2$**  for both the SD and the interferometric map **simultaneously**
  - Linear Combination in **image domain**



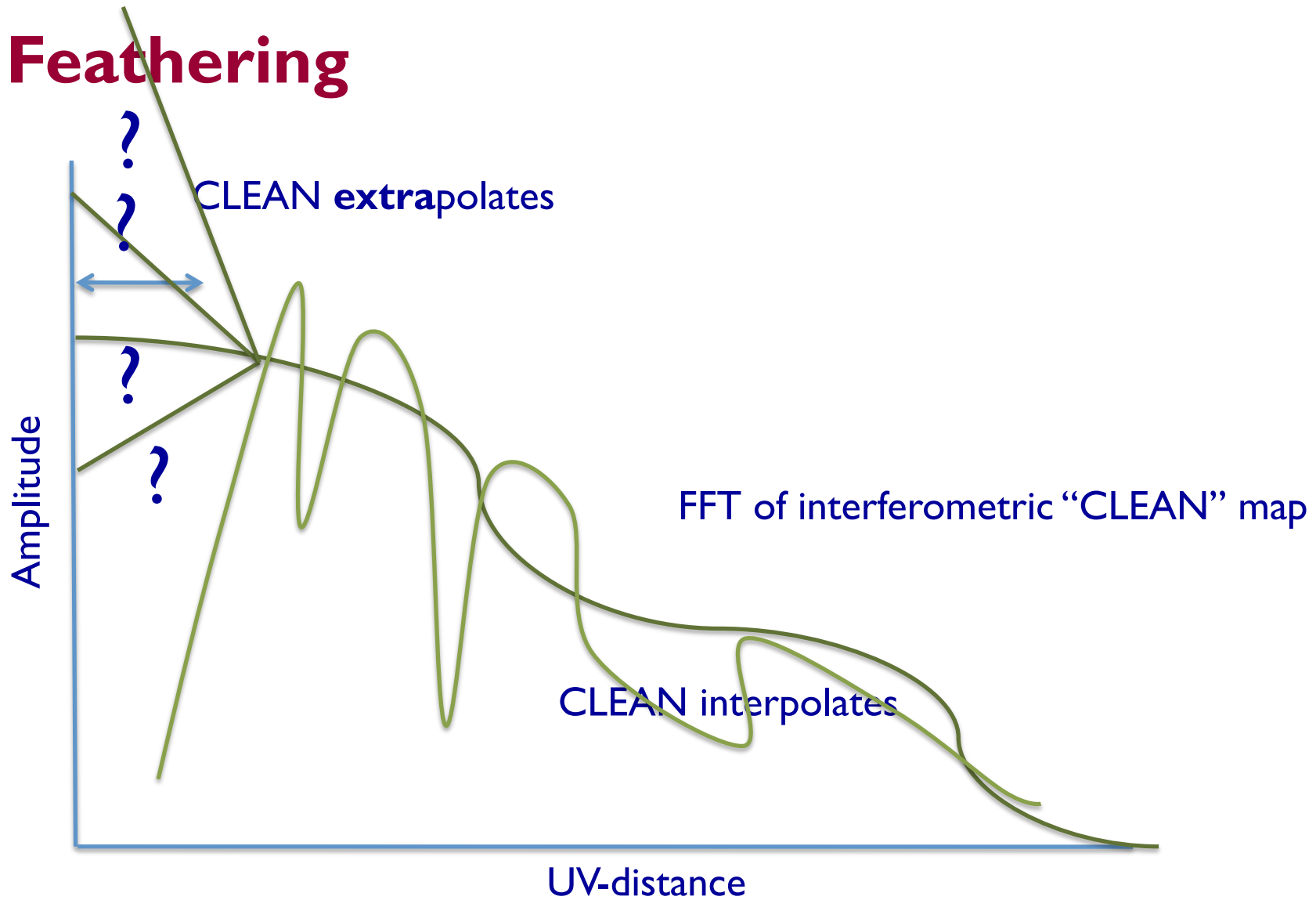
# Feathering



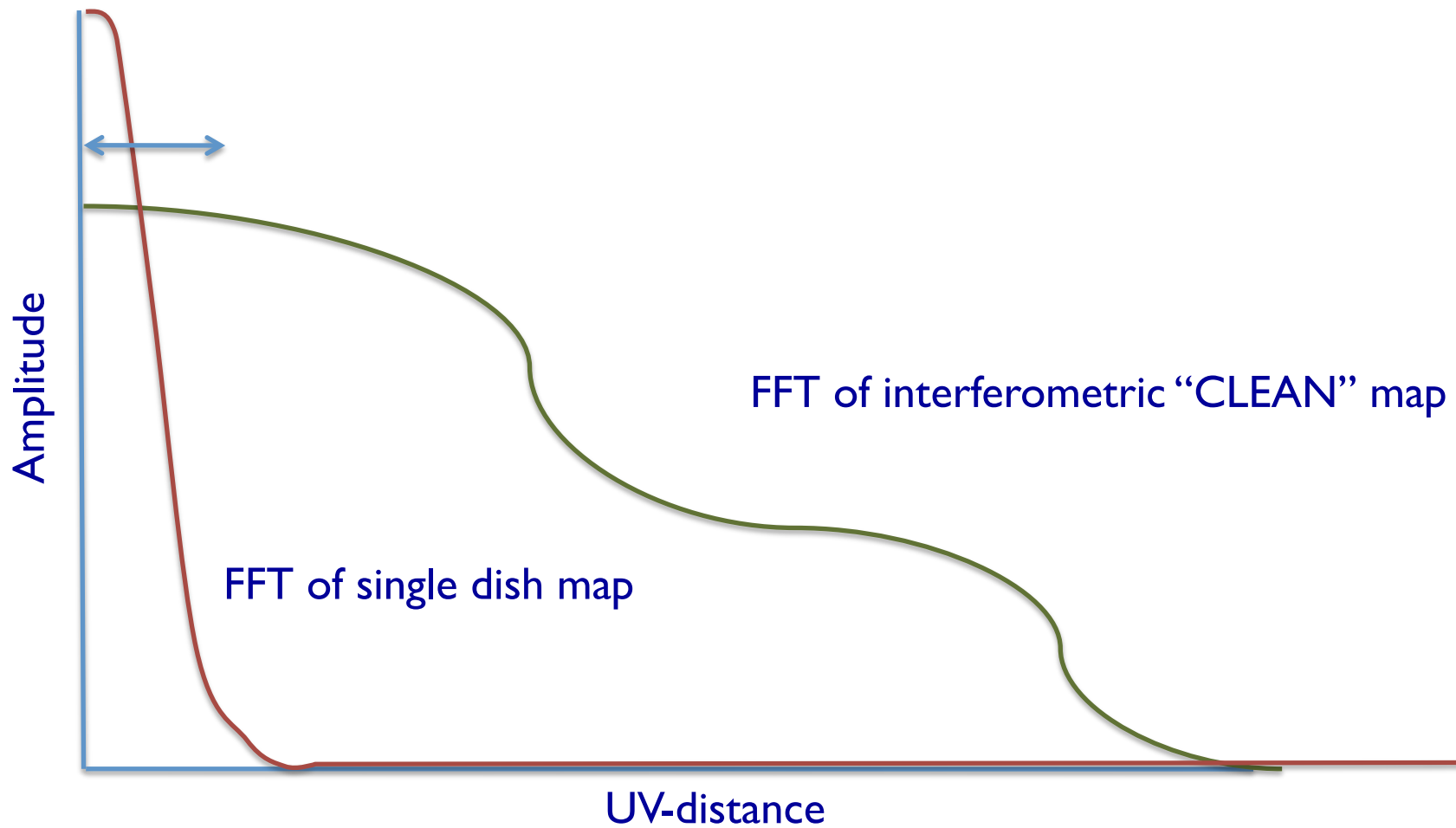
# Feathering



# Feathering

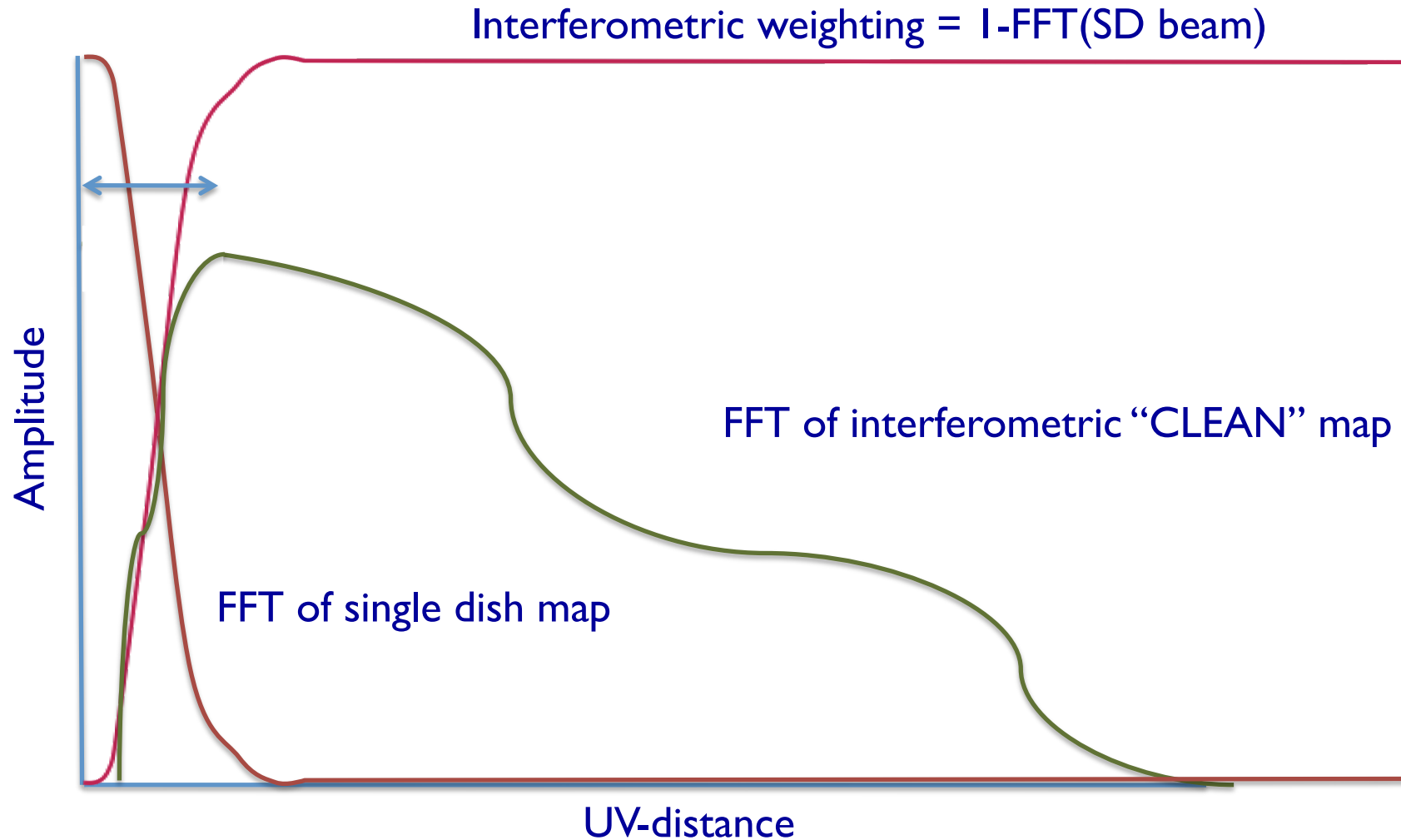


# Feathering

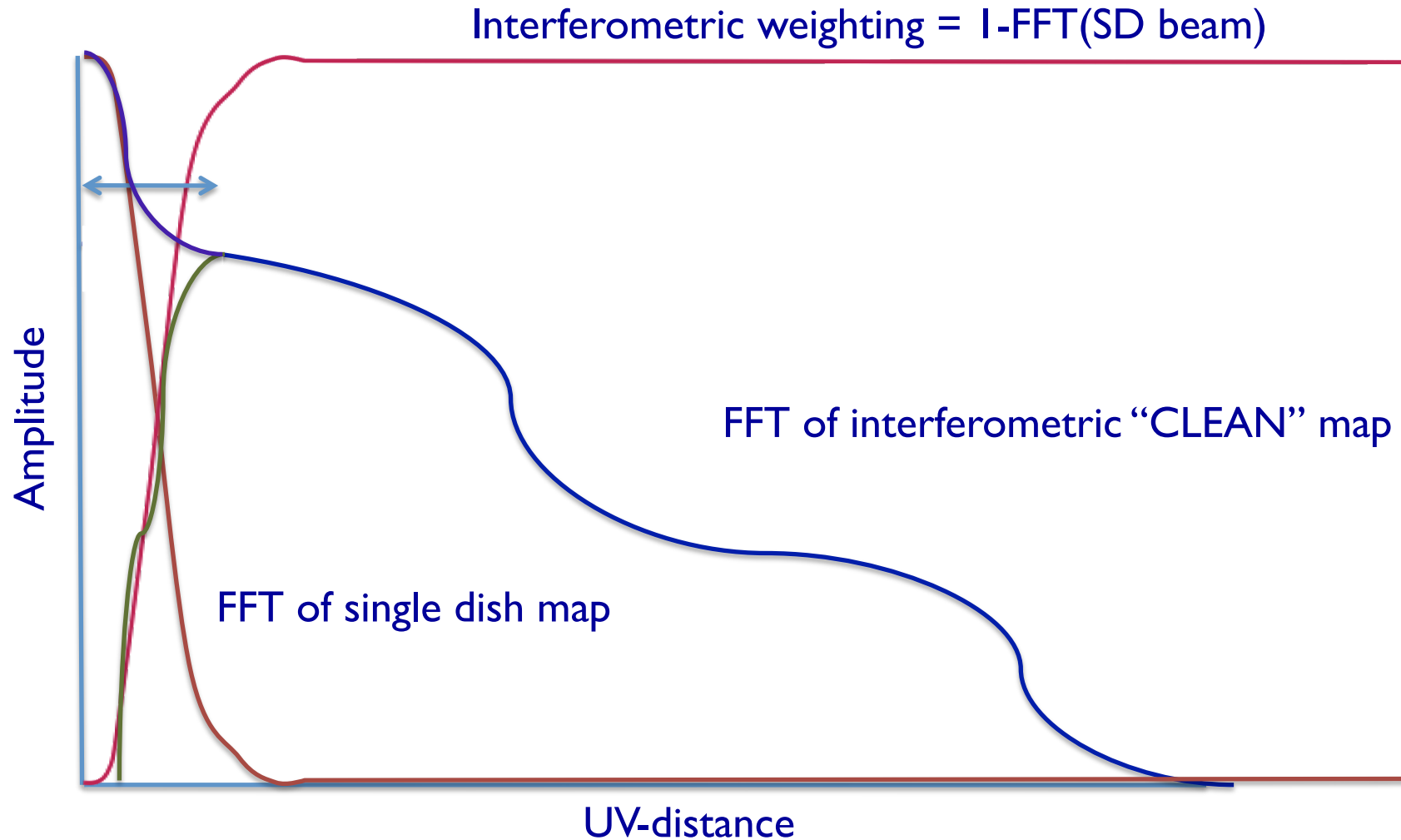




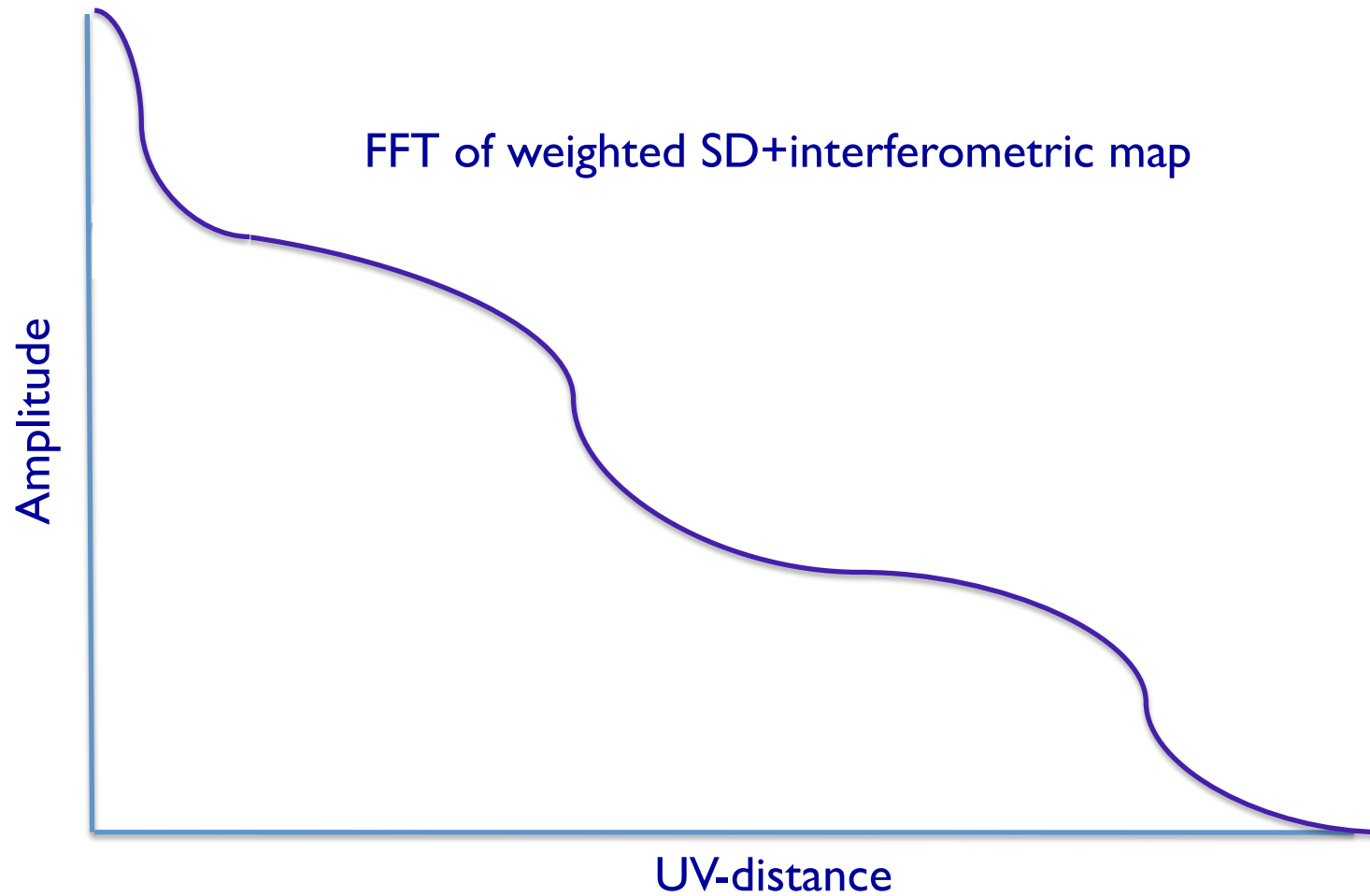
# Feathering

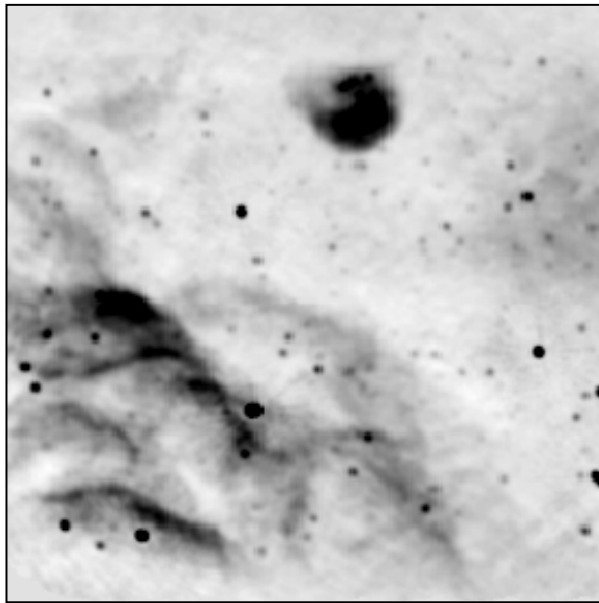


# Feathering

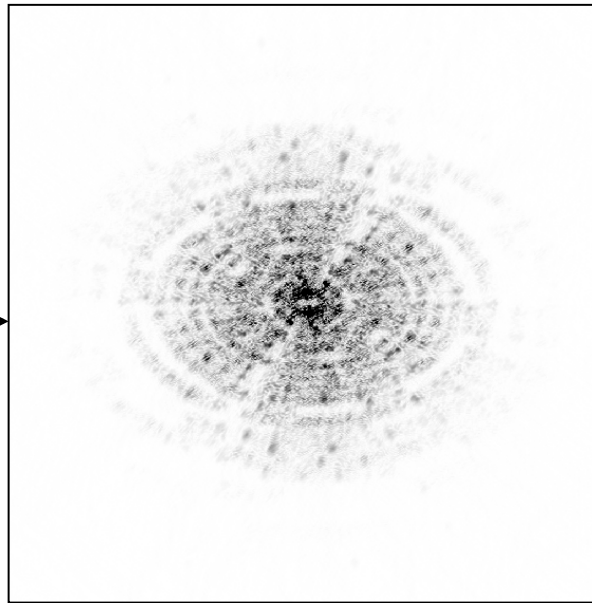


# Feathering



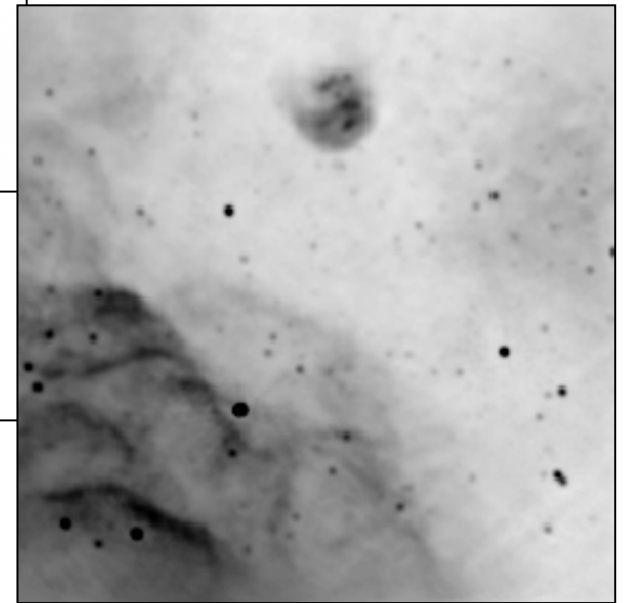


**FT**  
→

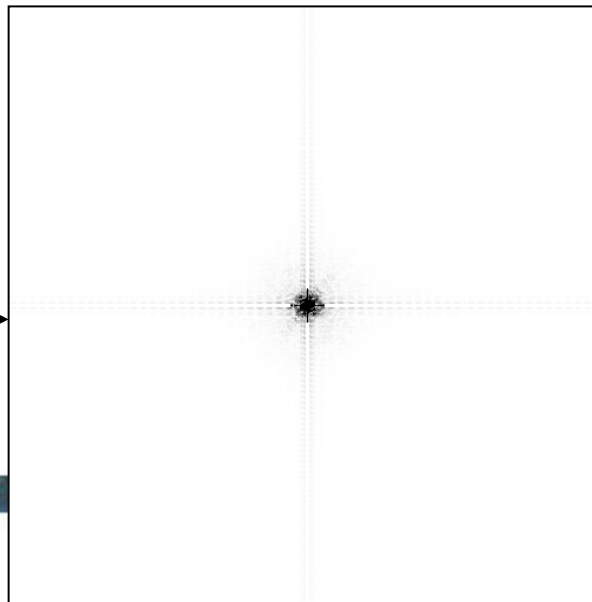


$+ f_{cal}$

**FT<sup>-1</sup>**=



**FT**  
→



Example of Fourier  
plane combination:  
McClure-Griffiths et al.

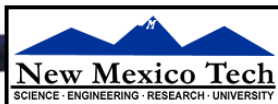
# Methods – Joint Deconvolution with Maximum Entropy

- Deconvolve both images simultaneously, with 2 conditions for improving the quality (entropy)

$$\aleph = - \sum_i I_i \ln \left( \frac{I_i}{M_i e} \right)$$

Subject to (1) 
$$\sum_i \left\{ I_{\text{int}}^D - B_{\text{int}} * I \right\}_i^2 < N \sigma_{\text{int}}^2$$

(2) 
$$\sum_i \left\{ I_{sd}^D - \frac{B_{sd} * I}{f_{sd}} \right\}_i^2 < M \sigma_{sd}^2$$





# Methods – ‘Linear’ Combination in Image Domain

Combined image:

$$I_{\text{tot}} = w_{\text{int}} I_{\text{int}} + w_{\text{sd}} f_{\text{sd}} I_{\text{sd}}$$

Weights:

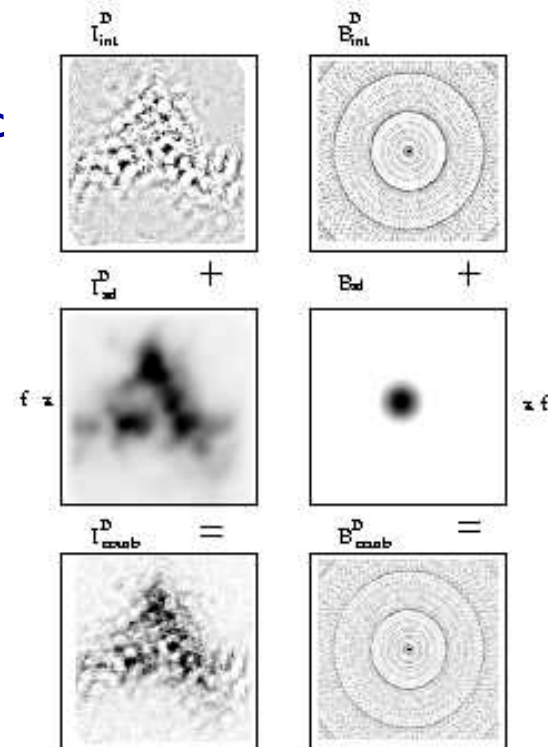
$$w_{\text{int}} = \frac{\Omega_{\text{sd}}}{\Omega_{\text{int}} + \Omega_{\text{sd}}}$$

$$w_{\text{sd}} = \frac{\Omega_{\text{int}}}{\Omega_{\text{int}} + \Omega_{\text{sd}}}$$

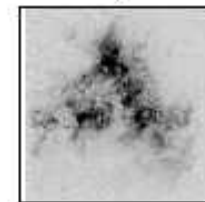
Interferometric  
Dirty image  
and beam

SD image  
and beam

Combination

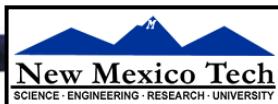


DECONVOLVE



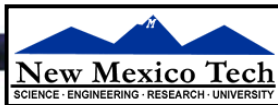
deconvolve

Stanimirovic et al.



# Summary

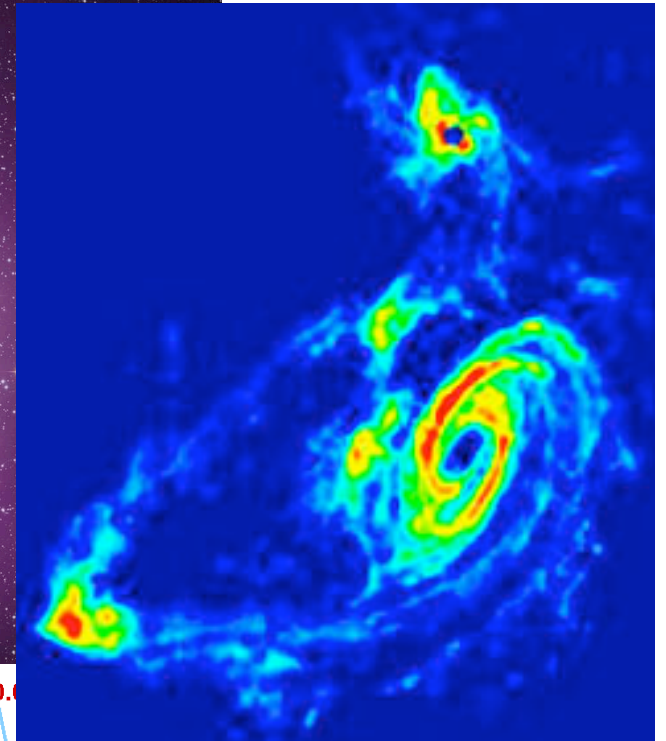
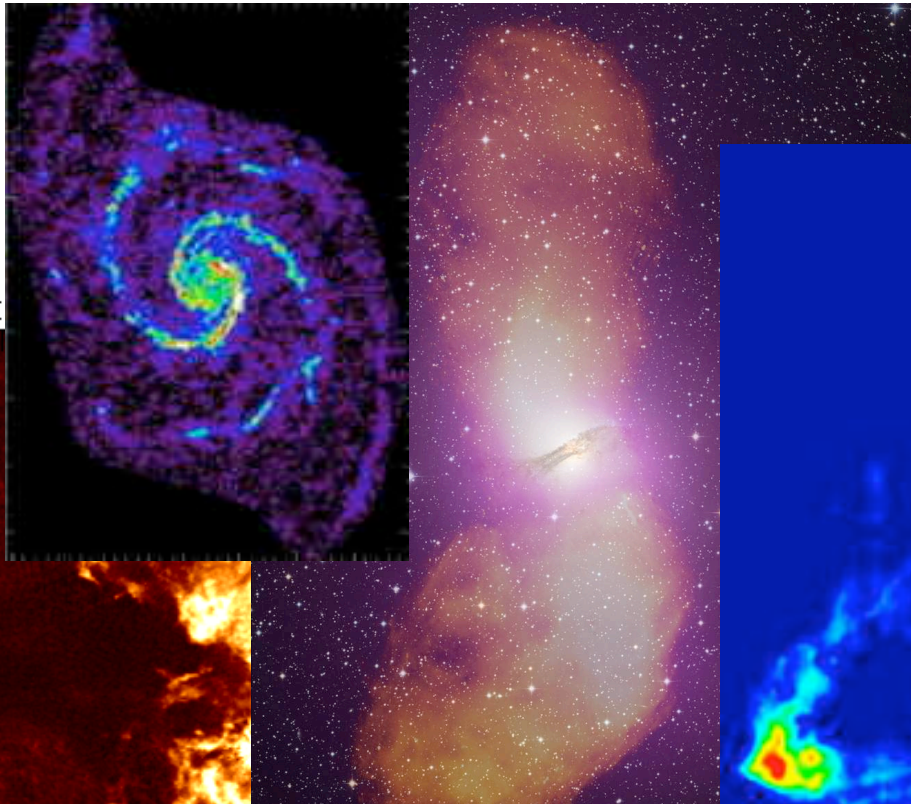
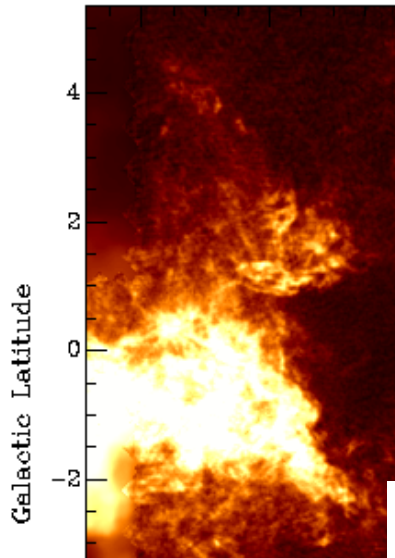
- Mosaicing is a technique to image objects much larger than the primary beam
- Unlocks additional uv spacings by using dish extends for additional uv-coverage (convolution of visibilities with FT[PB])
- Needs a bit of care and thought to setup
- Mosaicing techniques will be used very commonly in the future:
  - ALMA features a small PB from 1' @3mm to 10'' @600GHz
  - SKA/pathfinders sport large beam but aim for large (all-sky) sky coverage
- Zero/short spacing reconstruction may be required
  - Use a large SD telescope and carefully apply calibration
- Choose the best mosaicing and zero/short spacing correction method for your problem
- Fun to reduce and beautiful images!



# Summary

Velocity: 36.28 km/s

GSH

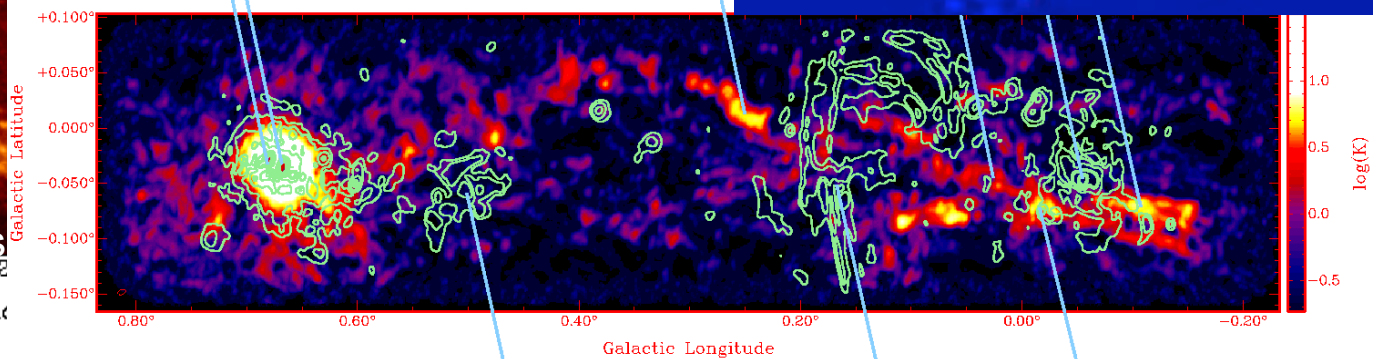


25 pointings

Galac

Sgr B2 (N) (M)

M0.25+0.0



Sgr B1

Pistol

M-0.02-0.07

