

# Wide Bandwidth Imaging

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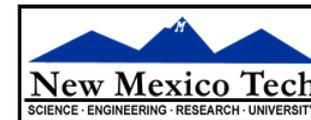


Thirteenth Synthesis Imaging Workshop

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National Radio Astronomy Observatory.



The University of New Mexico



# Outline

## (1) What is wide-band imaging ?

- Bandwidth and sensitivity
- Frequency-dependent Instrument and Sky
- Bandwidth smearing
- Multi-frequency synthesis

## (2) Imaging Algorithms

- Recap. of image-reconstruction methods
- Cube vs Continuum imaging (intensity and spectrum)

## (3) Examples of various effects/corrections/errors

## (4) Example of wide-band imaging trials on JVLA observations of a Galactic super-nova-remnant between 1-2 GHz.

# Wide-band Imaging + Sensitivity

	L-Band (1 –2 GHz)	C-Band (4 –8 GHz)	X-Band (8 –12 GHz)
Bandwidth : $\nu_{max} - \nu_{min}$	1 GHz	4 GHz *	4 GHz *
Bandwidth Ratio : $\nu_{max} : \nu_{min}$	2 : 1	2 : 1	1.5 : 1
Fractional Bandwidth : $(\nu_{max} - \nu_{min}) / \nu_{mid}$	66%	66%	40%

\* : Currently the max bandwidth is 2 GHz; it will increase with 3-bit samplers.

## (1) Broad-band receivers increase 'instantaneous' sensitivity

$$\text{Continuum sensitivity : } \sigma_{cont} \propto \frac{SEFD}{\sqrt{N_{ant}(N_{ant}-1)} \delta \tau \delta \nu}$$

(at field-center)

VLA → JVLA      50 MHz → 2 GHz      Sensitivity improvement :  $\sqrt{\frac{2 \text{ GHz}}{50 \text{ MHz}}} \approx 6$  times.

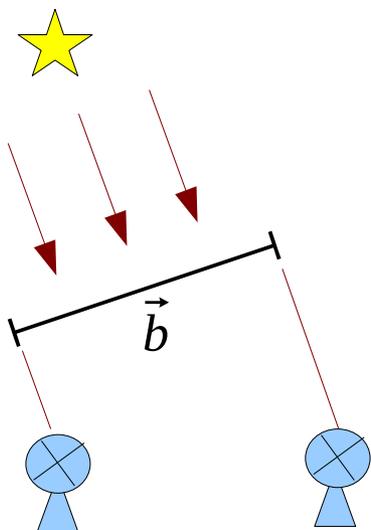
In practice, effective bandwidth for imaging depends on bandpass shape, data weights, and regions of the spectrum flagged due to RFI.

## (2) Imaging must account for the frequency-dependence of the sky and instrument.

UV-coverage ( imaging properties ), sky-brightness (EM-spectrum), primary-beam (field-of-view)

Fractional bandwidth controls the magnitude of frequency-dependent effects within the band.

# Frequency-dependent UV-coverage and PSFs



Spatial-frequency coverage changes with frequency

$$S(u, v)_\nu = \frac{\vec{b}}{\lambda} = \frac{\vec{b} \nu}{c}$$

The imaging properties of the interferometer change with frequency.

- Image angular-resolution (radians) :  $\frac{\lambda}{b_{max}}$
- Largest spatial scale (radians) :  $\frac{\lambda}{b_{min}}$

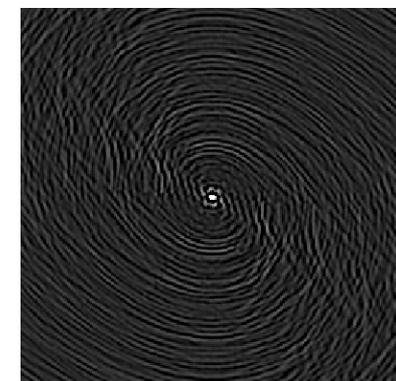
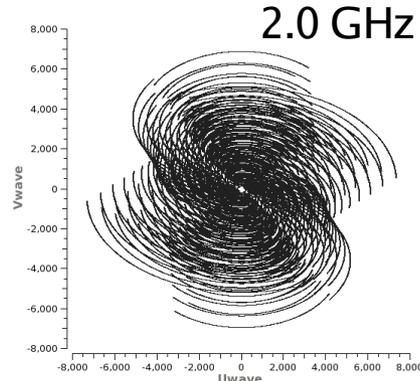
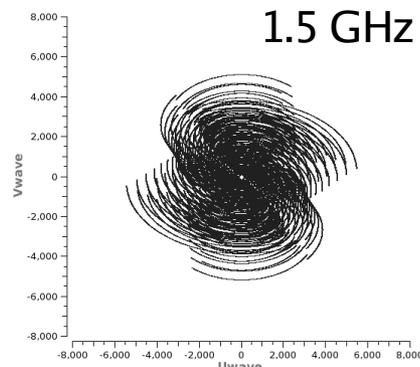
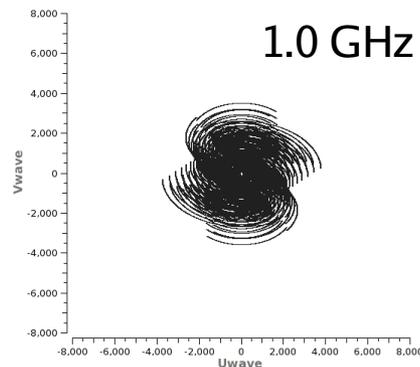
Broad-band signal → Channels :

Voltages measured by a broad-band receiver are split into several narrow-band channels ( FX or XF ), to measure visibilities at multiple frequencies, and to allow the correct uv-coverage to be used.

In the early days of wide-band receivers,  
this was not the case.....

$$S(u, v)_\nu$$

$$I_\nu^{psf} = [F^{-1}] S_\nu$$



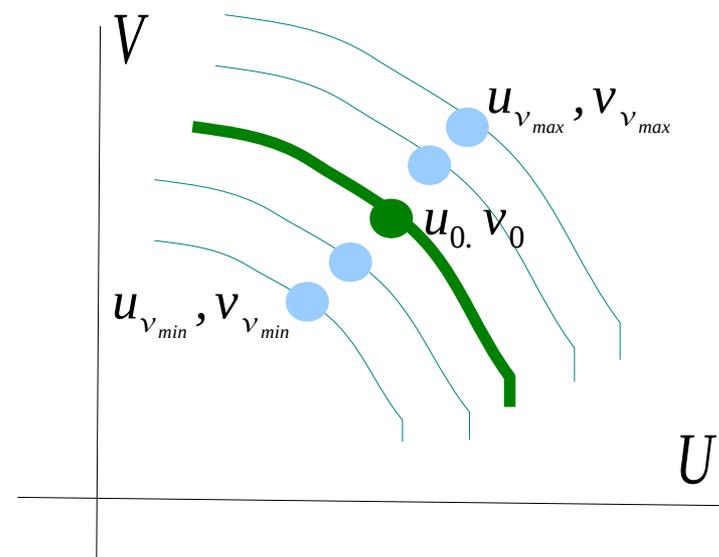
# Bandwidth smearing (chromatic aberration)

In the early days of continuum-observing, only one visibility was computed across the entire bandwidth of the receiver, and attributed to the reference (or middle) frequency  $\nu_0$ . Delay-tracking was also done only at  $\nu_0$ .

The visibility  $V(u_\nu)$  is mistakenly mapped to  $u_0 = \frac{b \nu_0}{c} = \frac{\nu_0}{\nu} u_\nu$

Similarity theorem of Fourier-transforms :

$$V\left(\frac{\nu_0}{\nu} u_\nu, \frac{\nu_0}{\nu} \nu_\nu\right) \longrightarrow \left(\frac{\nu}{\nu_0}\right)^2 I\left(\frac{\nu}{\nu_0} l, \frac{\nu}{\nu_0} m\right)$$



A radial shift in the source position, with frequency.

=> Radial smearing of the brightness-distribution.

The shape of the smearing is controlled by the bandshape ( See Chapter 18 by Bridle & Schwab )

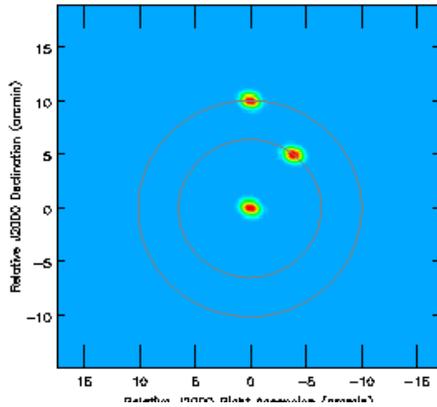
The measured visibility can be written as a weighted average along a radius in the UV-plane, where the 'weight-spectrum' is given by the bandpass shape and delay-tracking error. This is further written as a product of the visibility function and a 'delay function', which, in the image-domain becomes a position-dependent convolution with a radial 'distortion function'.

**Note :** Excessive channel-averaging during post-processing has a similar effect.

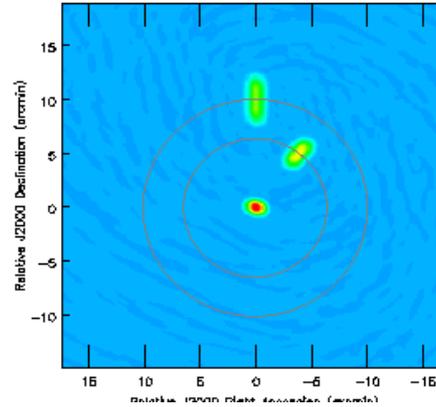
# Bandwidth smearing (chromatic aberration)

An (exaggerated) example of bandwidth-smearing with a 1-2 GHz signal.....

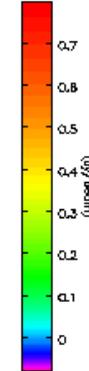
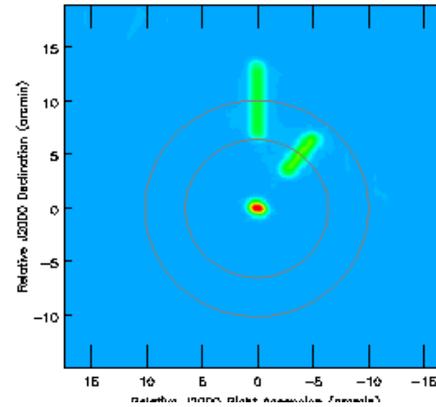
Bandwidth : 2 MHz



200 MHz



1.0 GHz



Contours represent 5 and 10 arcmin distances from the phase-center.

- (1) If the bandpass shape is known, it is possible to recover (partially) from bandwidth-smearing, but it is always best to avoid the problem altogether.
- (2) Construct visibilities for multiple narrow-band channels, each with its own delay-tracking.

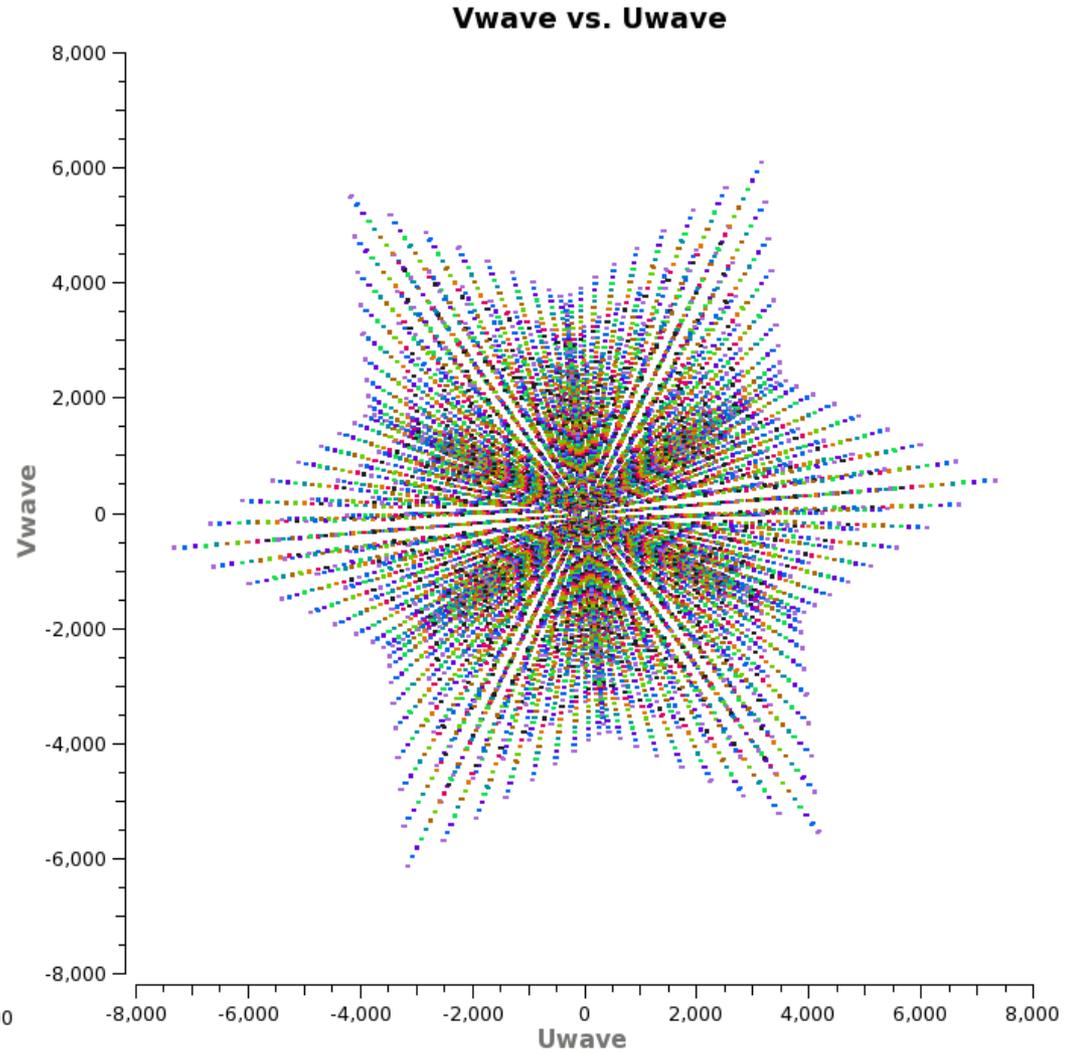
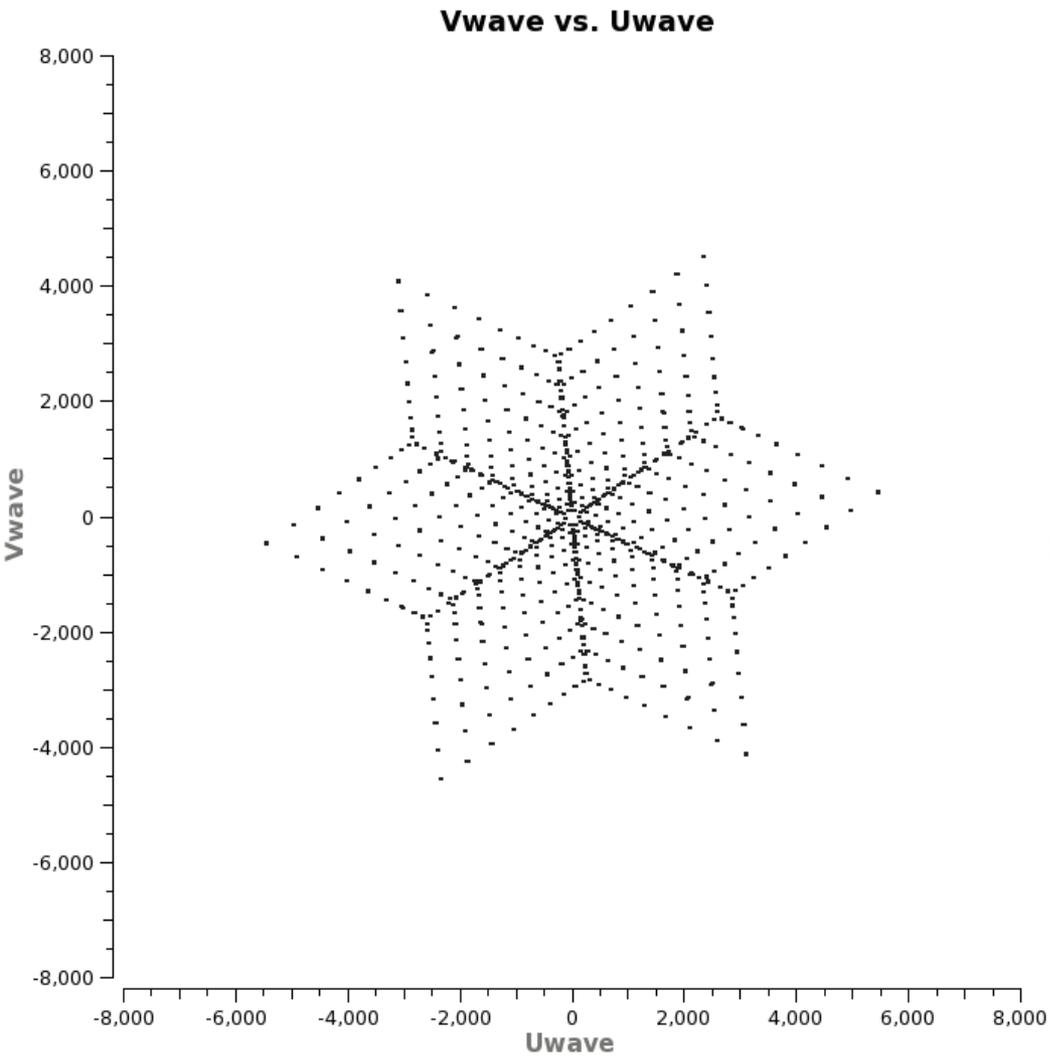
Bandwidth Smearing Limit ( maximum channel-width ) :  $\delta \nu < \nu_0 \frac{D}{b_{max}}$

=> Place  $V(u_\nu)$  at the correct location on the UV-plane.

=> UV-range spanned by  $\delta \nu$  is smaller than a uv-grid cell (  $1 / f\text{-o-v}$  )

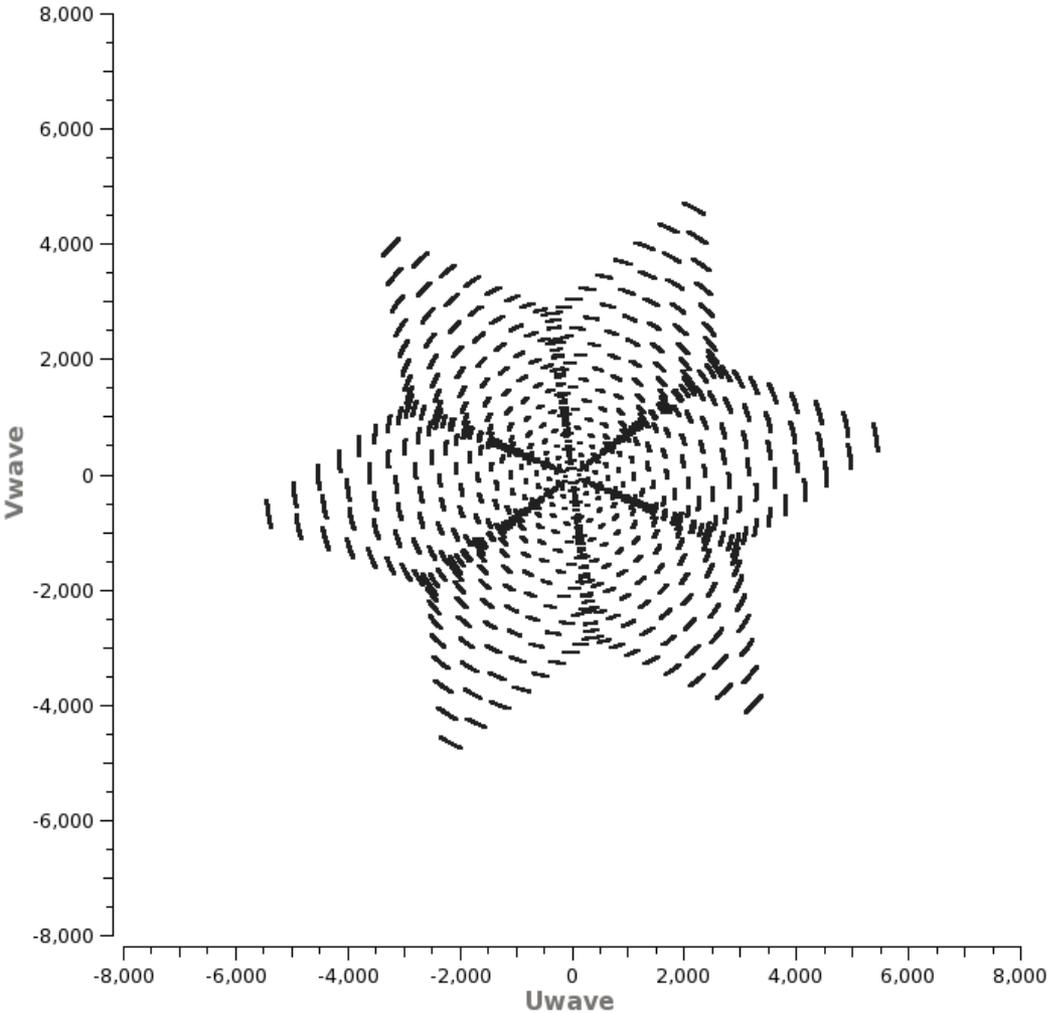
For example, at 1.4 GHz,  
 33 MHz (D-config),  
 10 MHz (C-config),  
 3 MHz (B-config),  
 1 MHz (A-config)

# Multi-Frequency-Synthesis

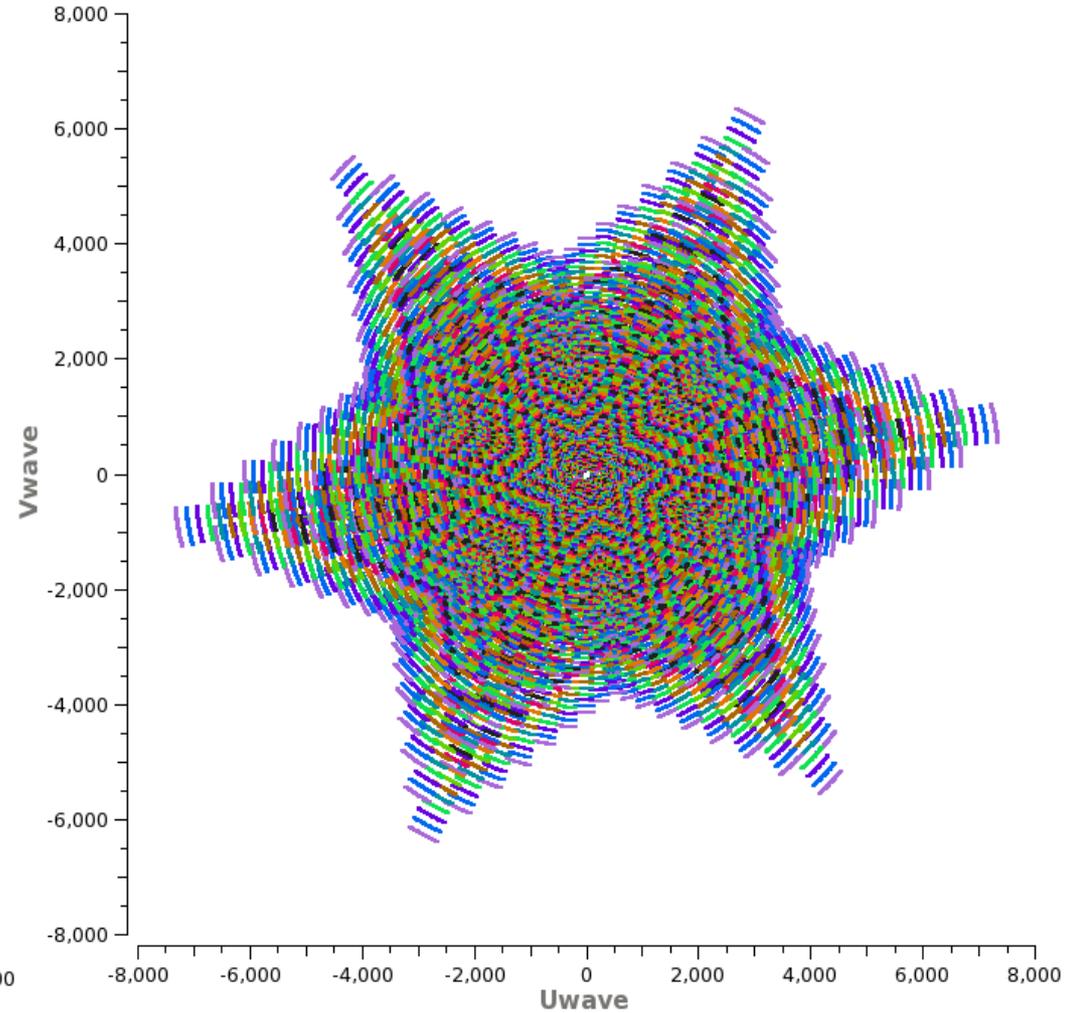


# Multi-Frequency Synthesis

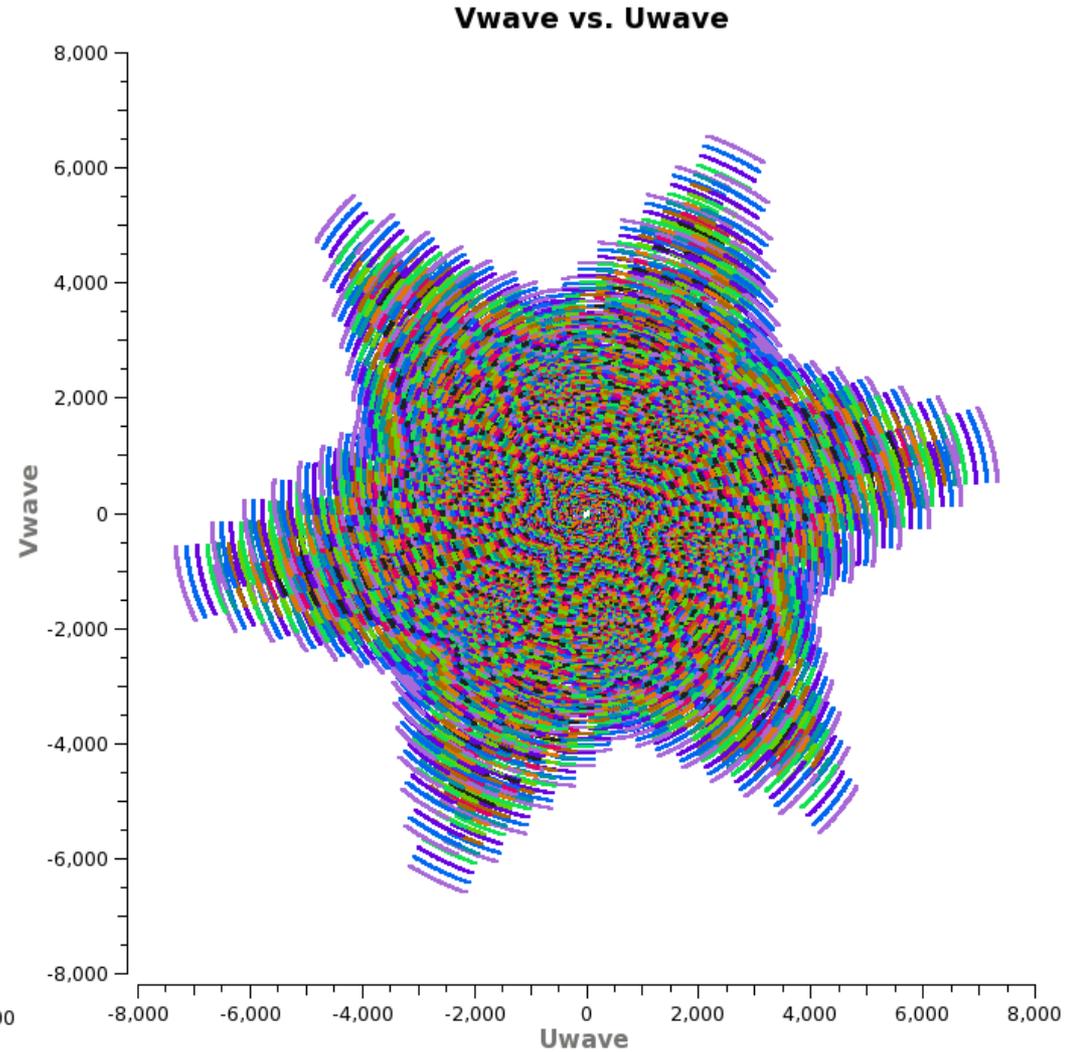
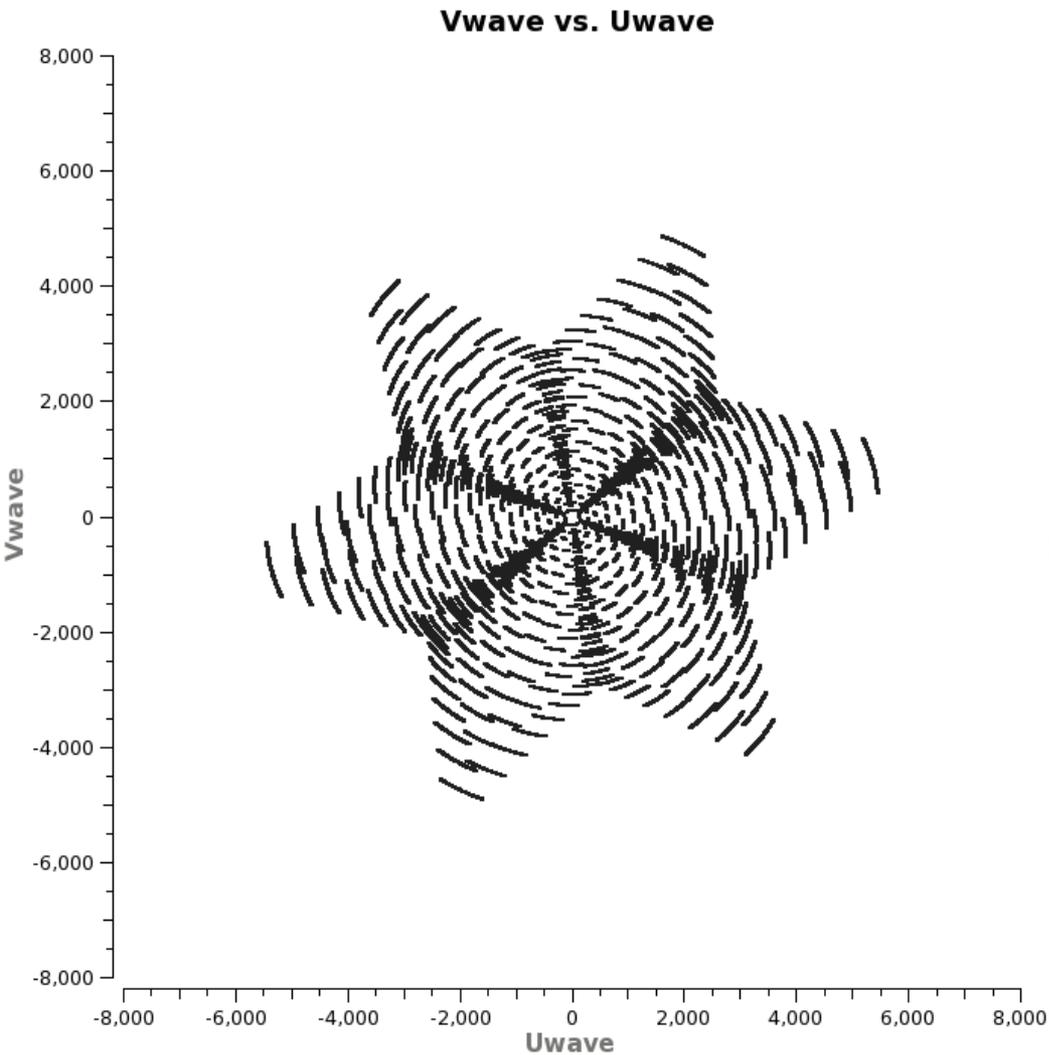
Vwave vs. Uwave



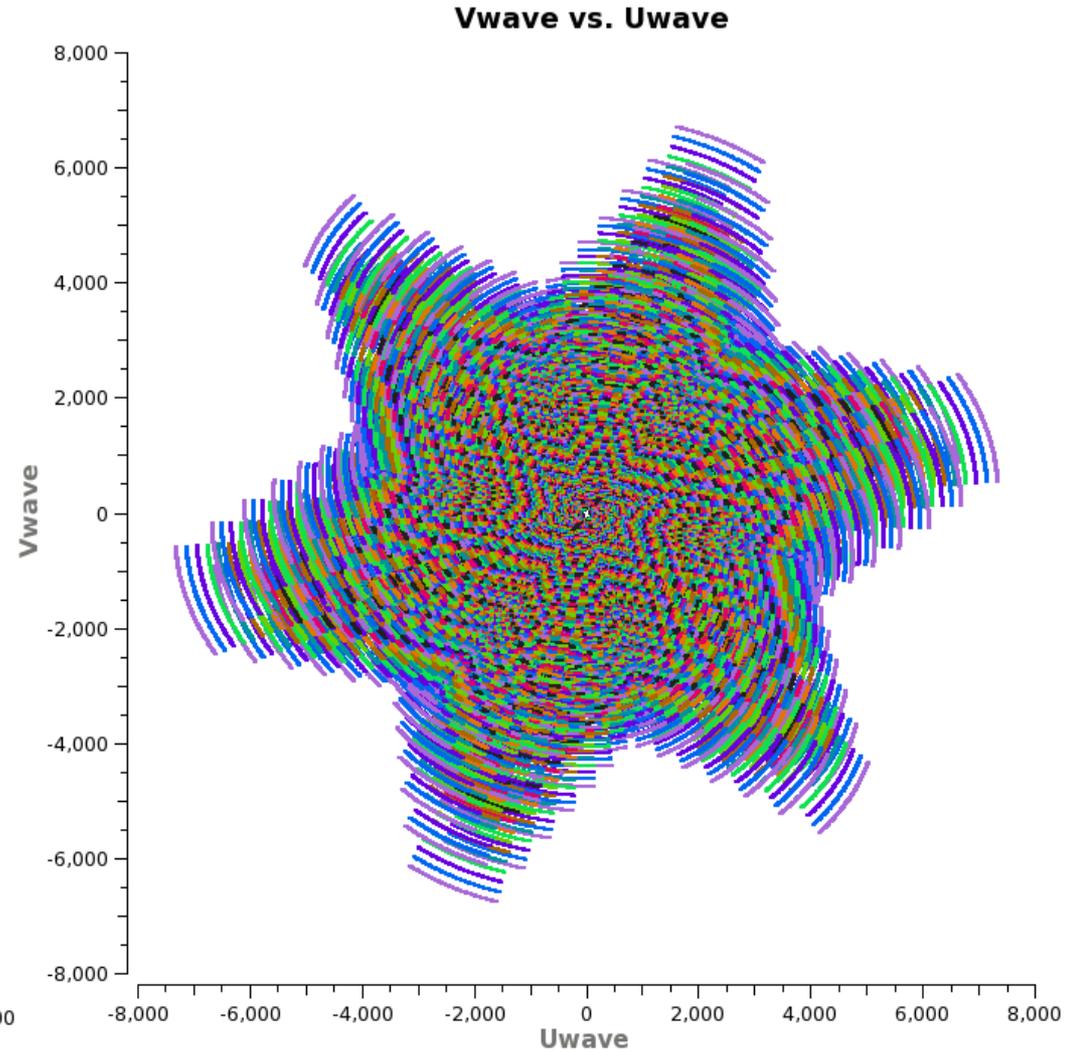
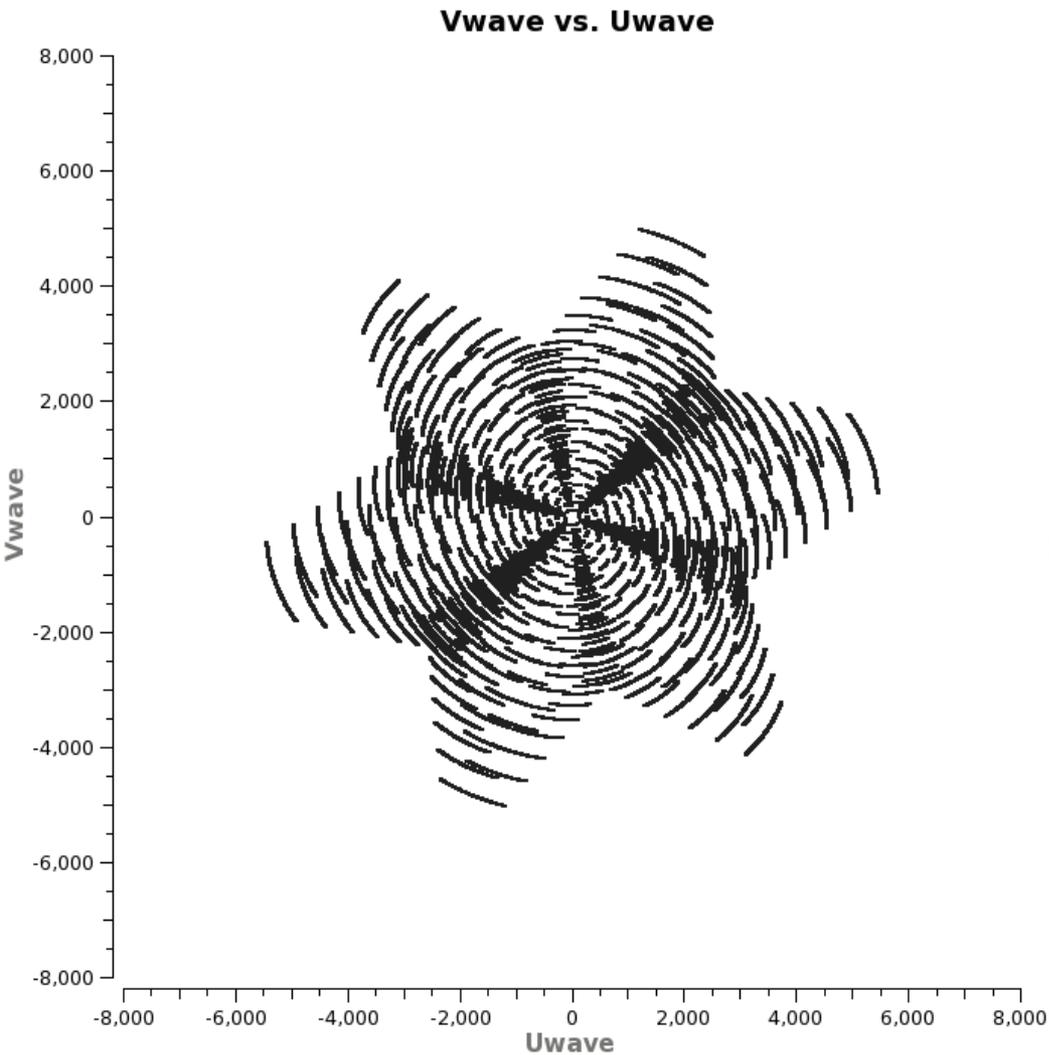
Vwave vs. Uwave



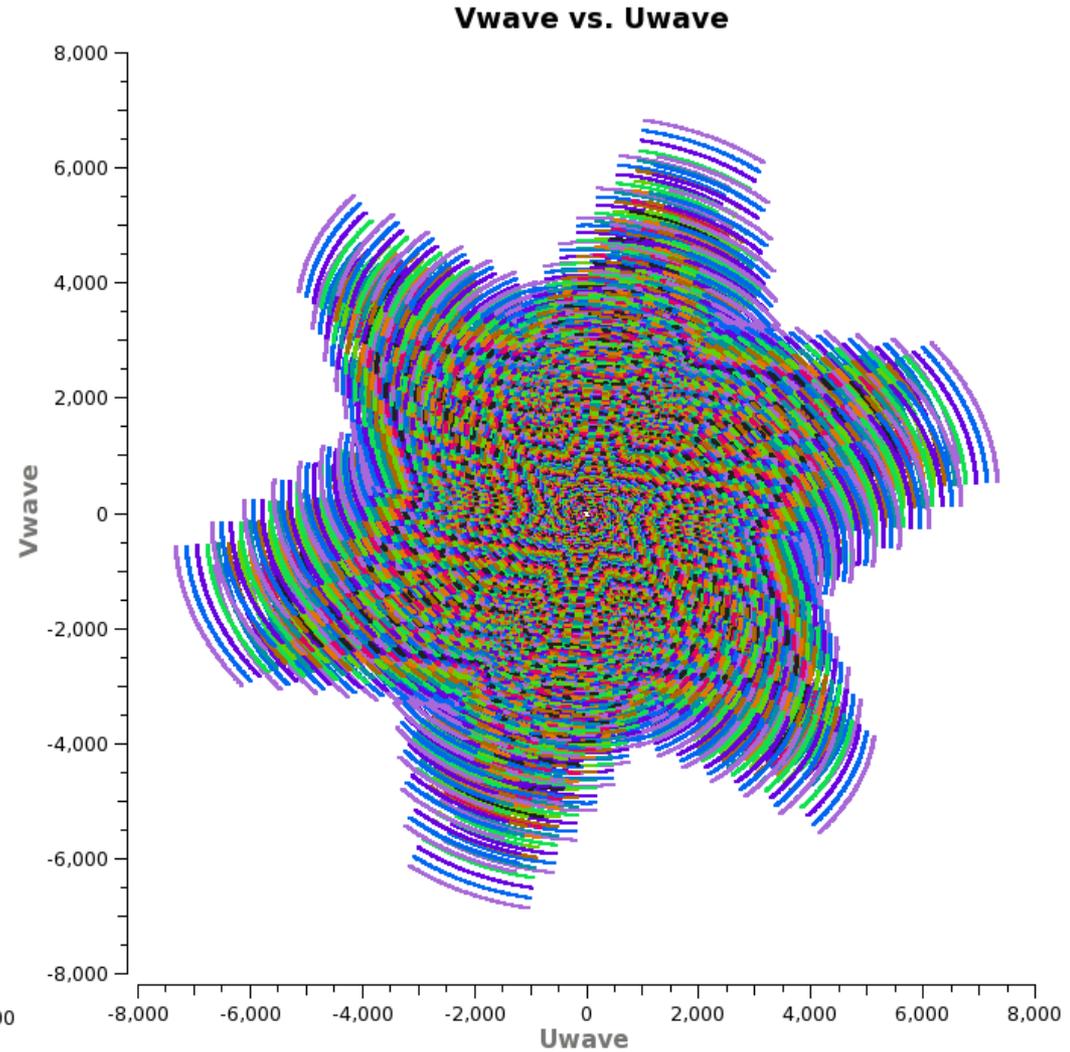
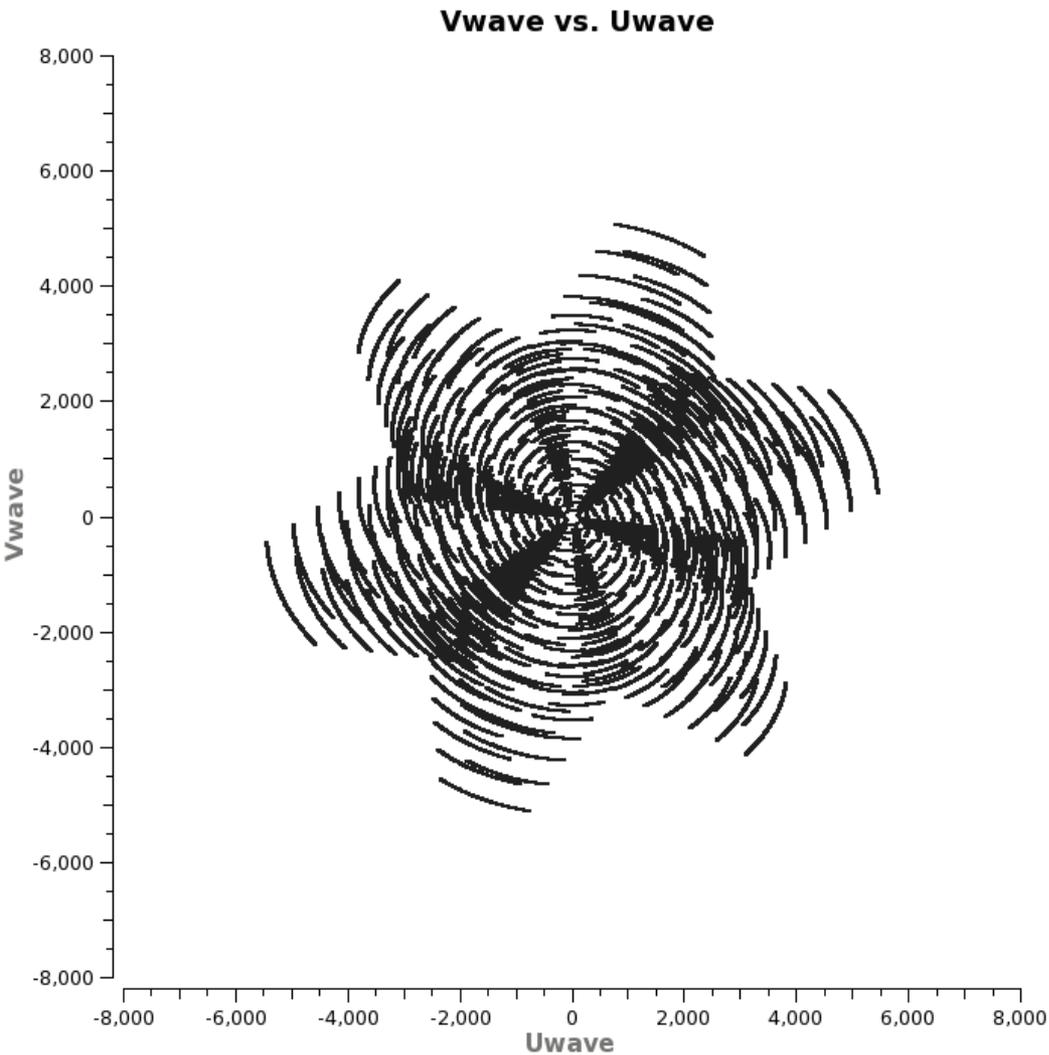
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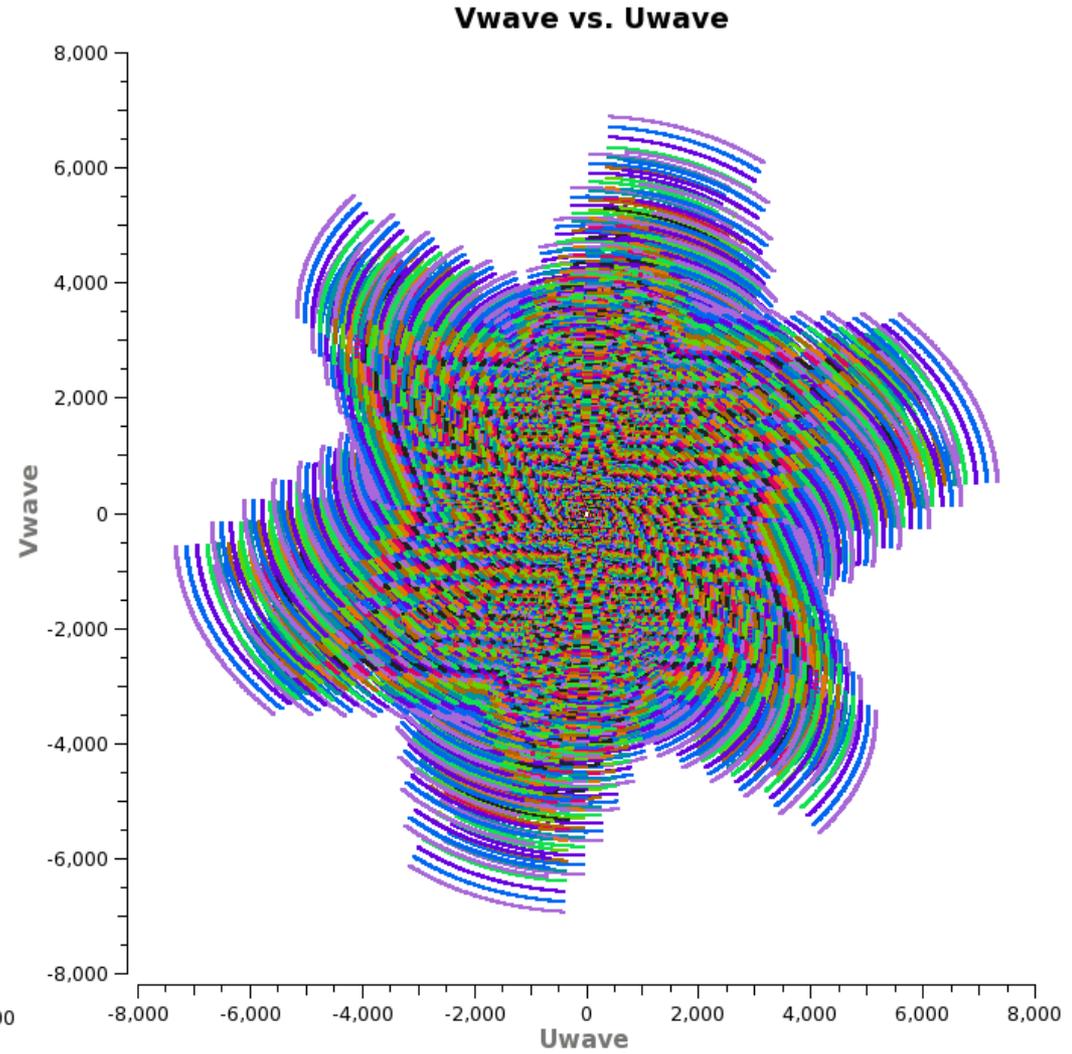
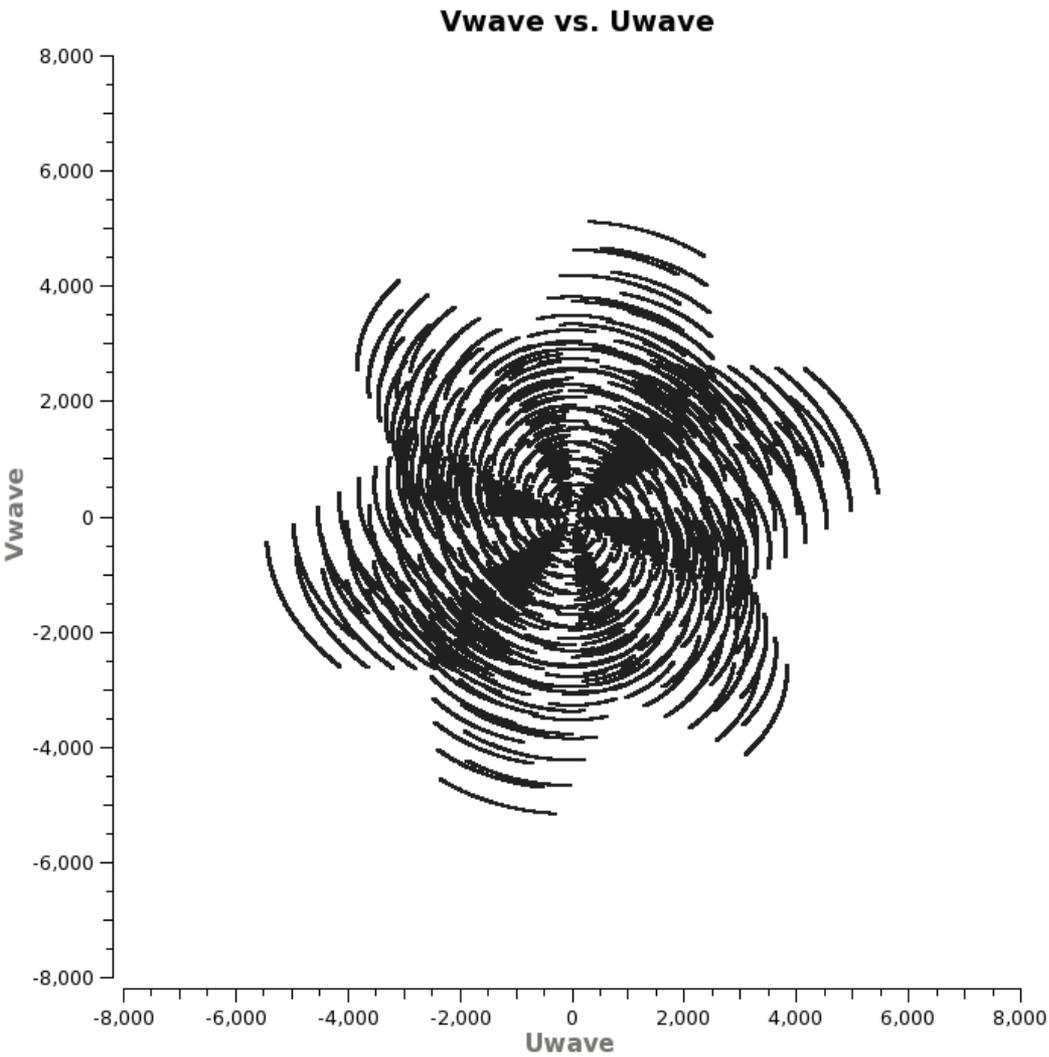
# Multi-Frequency Synthesis



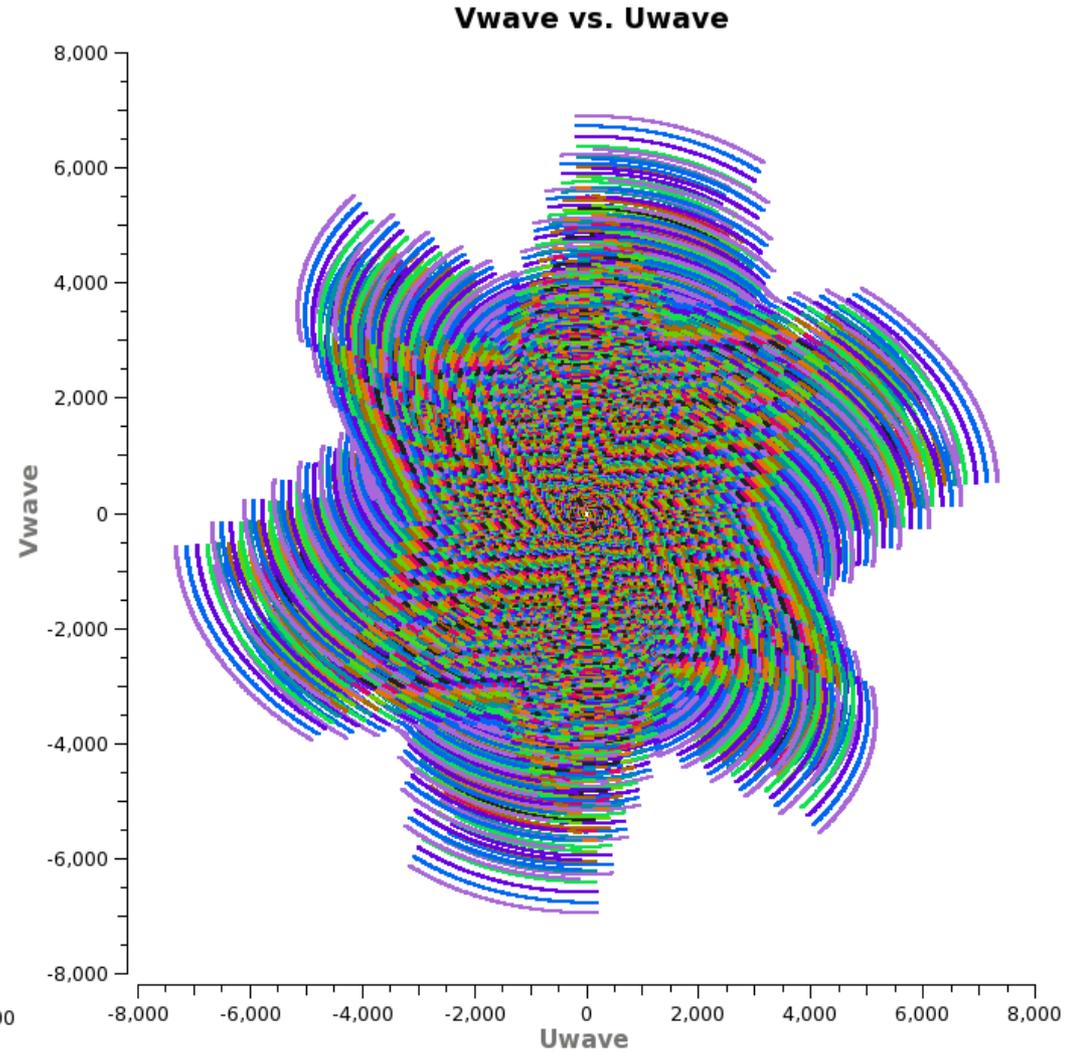
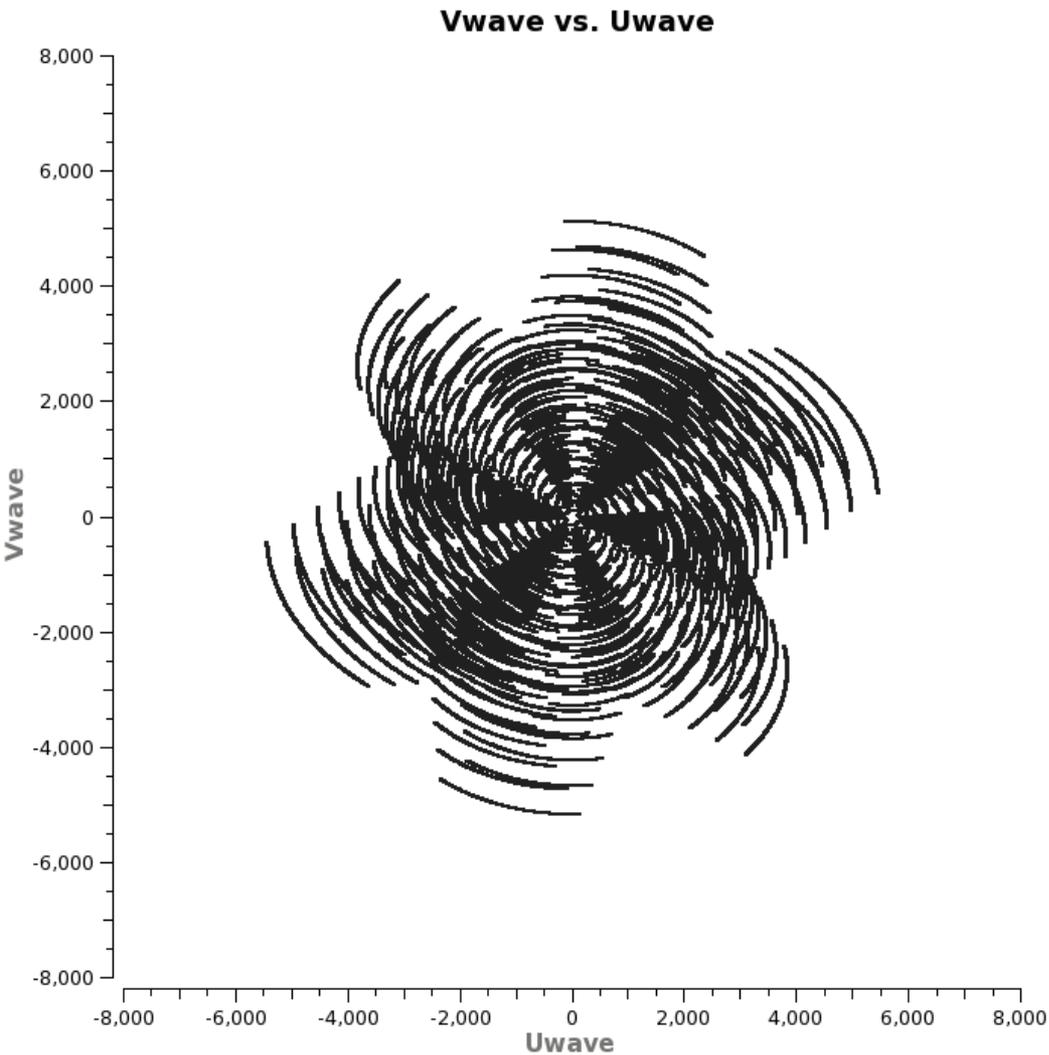
# Multi-Frequency Synthesis



# Multi-Frequency Synthesis

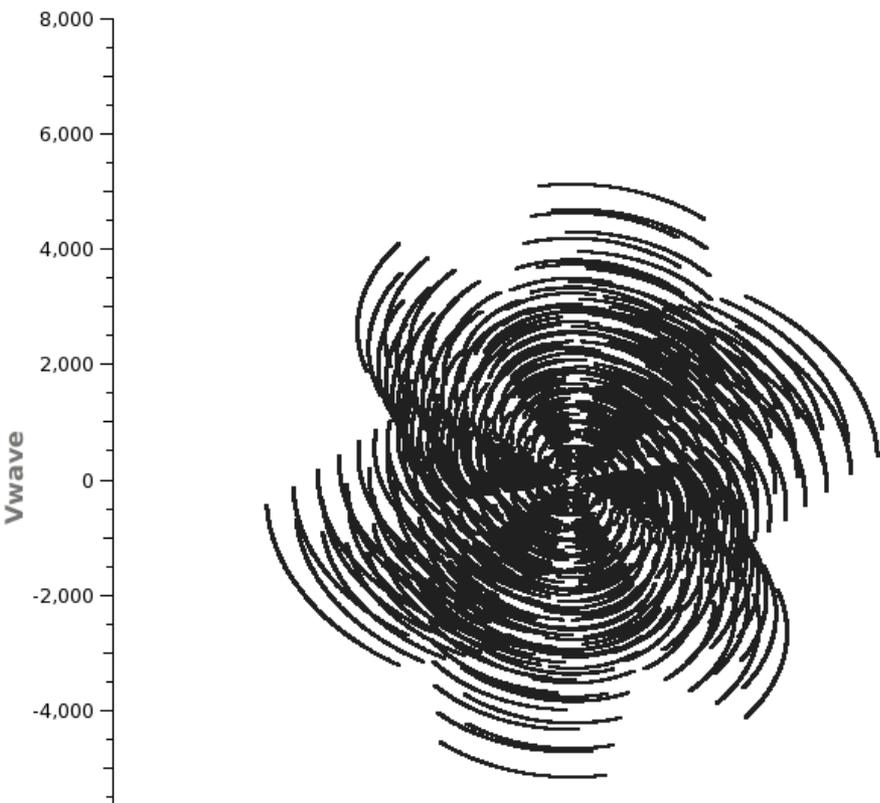


# Multi-Frequency Synthesis

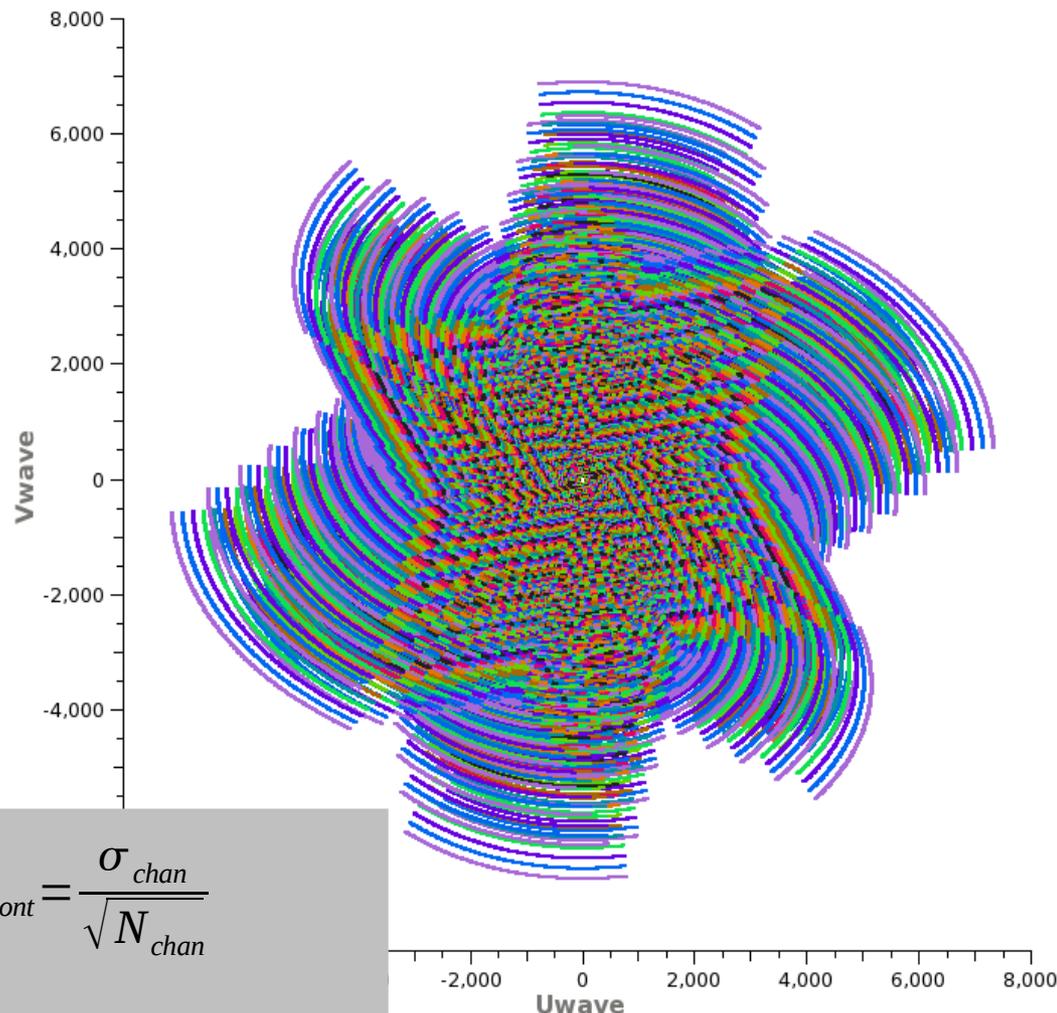


# Multi-Frequency Synthesis

Vwave vs. Uwave



Vwave vs. Uwave

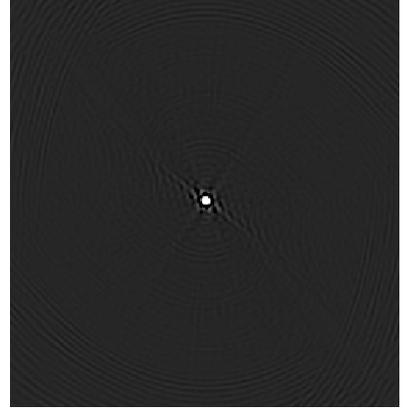
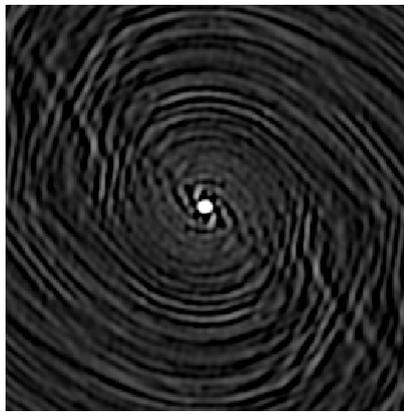
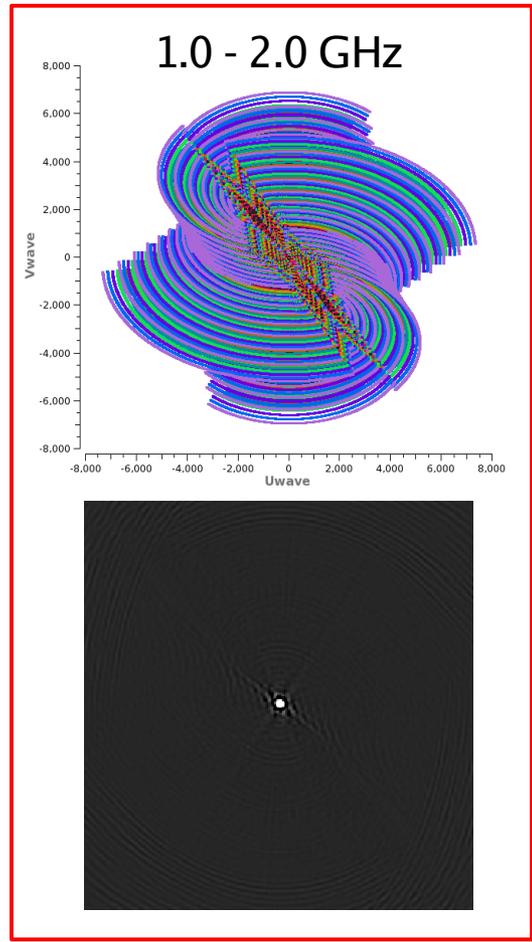
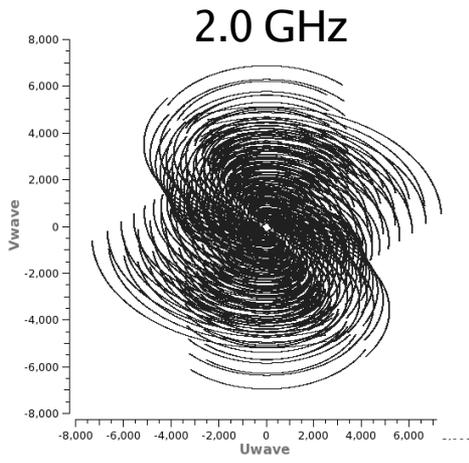
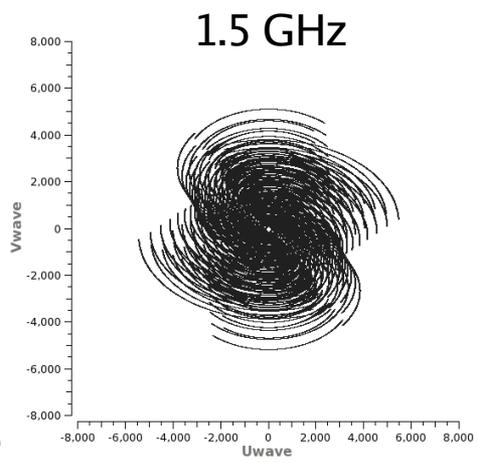
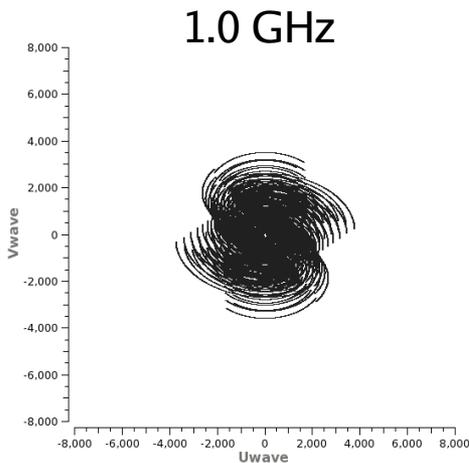


– Overlapping UV-coverage => better sensitivity  $\sigma_{cont} = \frac{\sigma_{chan}}{\sqrt{N_{chan}}}$

– Increased UV-filling => better imaging-fidelity

– Larger spatial-frequency range => better angular-resolution  $\frac{\lambda}{b_{max}}$

# Point Spread Functions : Single vs Multi Frequency



JVLA D-config, 6 hour synthesis : Robust-weighted PSFs.

For a flat-spectrum sky-brightness, channels contain multiple measurements of the same visibility function

$$V(u_v, v_v) = \int \int I(l, m) e^{2\pi i(u_v l + v_v m)} dl dm \quad \Rightarrow \text{Standard Imaging and Deconvolution applies}$$

# Frequency-dependent Sky Brightness

When the source intensity varies with frequency, different channels measure the visibility function of different sky-brightness distributions

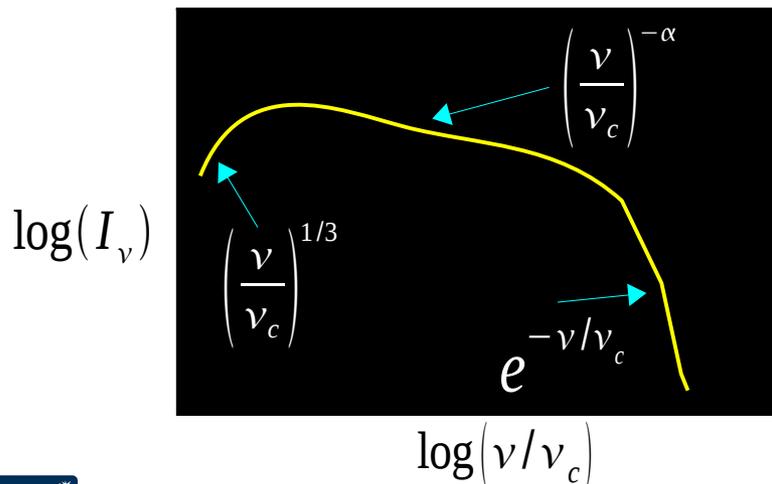
$$V(u_\nu, v_\nu) = \int \int I(l, m, \nu) e^{2\pi i(u_\nu l + v_\nu m)} dl dm$$

=> Cannot apply standard imaging techniques  
To the combined visibilities.

(1) Each point on the source has an intrinsic spectrum :

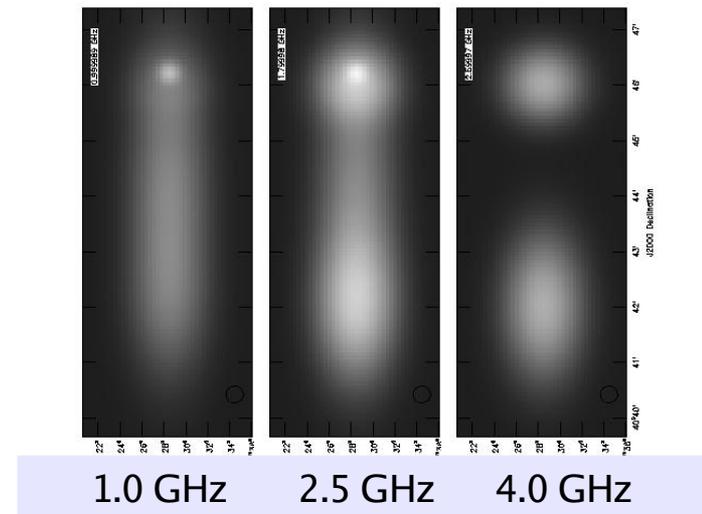
- The radio synchrotron spectrum is often a power law with varying spectral-index ( spectral curvature )

$$I_\nu = I_{\nu_0} \left( \frac{\nu}{\nu_0} \right)^{\alpha + \beta \log(\nu/\nu_0)}$$

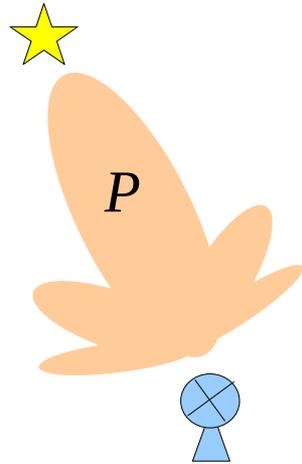


(2) Frequency probes source structure :

- Spectrum traces velocity structure (doppler-shifted line emission)
- Frequency probes depth in a 3D volume (solar flares/loops)



# Frequency Dependent Antenna response (Primary-Beam)



Primary-beam scales with frequency

$$HPBW_{\nu} = \frac{\lambda}{D} = \frac{c}{\nu D}$$

Bandpass calibration does **not** correct for off-axis gains or their frequency-dependence.

The average effect in the image-domain is a multiplication by an artificial PB-spectrum

=> Away from the pointing center, the Primary Beam introduces an artificial 'spectral index' on the measured sky :  $\alpha_{observed} = \alpha_{sky} + \alpha_{PB}$

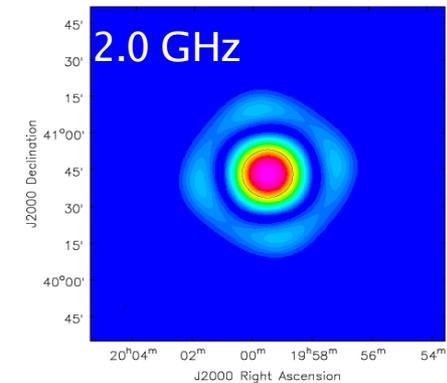
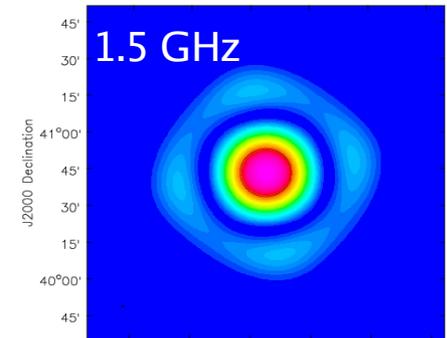
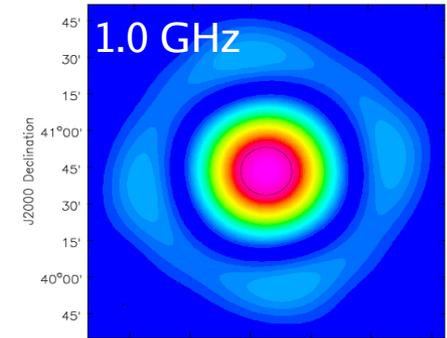
About -0.4 at the PB=0.8 ( 6 arcmin from the center at L-Band )

About -1.4 at the HPBW ( 15 arcmin from the center at L-Band )

Wide-field sensitivity depends on frequency.

Continuum sensitivity to a source with with a non-flat spectrum  $\propto \frac{\sum_{\nu} w_{\nu} \cdot P_{\nu} \cdot I_{\nu}}{\sum_{\nu} I_{\nu}}$

EVLA Primary Beams



# What is wide-band Imaging ?

- Use broad-band receivers to increase instantaneous continuum sensitivity
- Measure visibilities in many narrow-band channels to avoid bandwidth-smearing
- Use multi-frequency-synthesis
  - to increase the uv-coverage used in deconvolution and image-fidelity
  - to make images at the angular-resolution allowed by the highest frequency
- Account for the sky spectrum
  - by modeling and reconstructing the spectrum as well as the intensity
  - by flattening it out (bandpass self-calibration)
- Account for the frequency-dependent off-axis gains of the antennas
  - by including the PB-spectrum in the sky-spectrum model
  - by applying wide-field imaging techniques to eliminate the effect during imaging.

# Outline

## (1) What is wide-band imaging ?

- Bandwidth and sensitivity
- Frequency-dependent Instrument and Sky
- Bandwidth smearing
- Multi-frequency synthesis

## (2) Imaging Algorithms

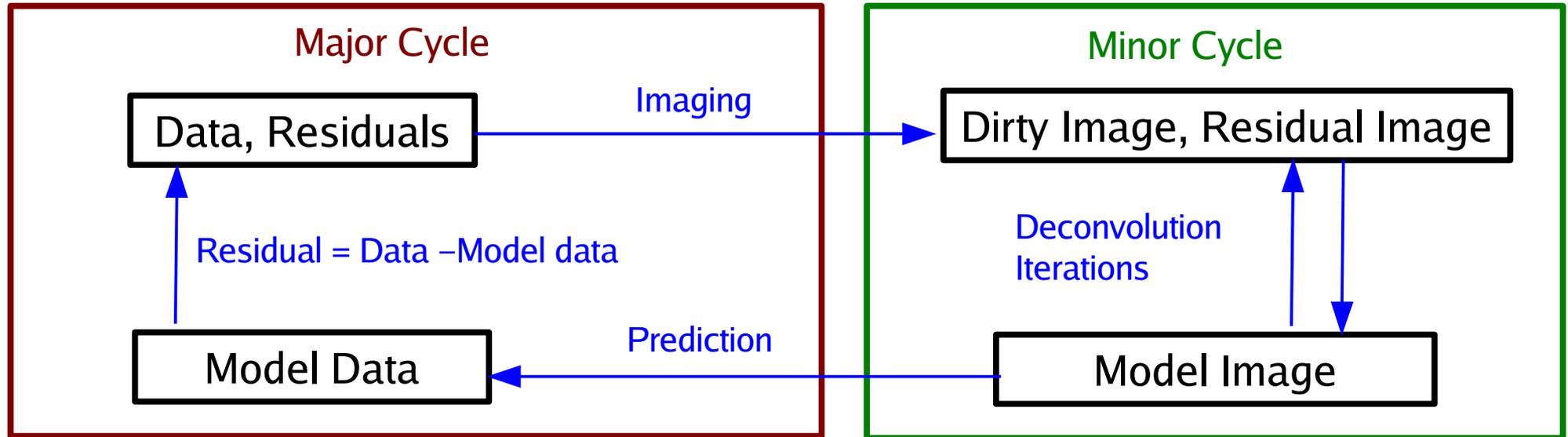
- Recap. of image-reconstruction methods
- Cube vs Continuum imaging (intensity and spectrum)

## (3) Examples of various effects/corrections/errors

## (4) Example of wide-band imaging trials on JVLA observations of a Galactic super-nova-remnant between 1-2 GHz.

# Basic Imaging and Deconvolution (recap.)

Image Reconstruction : Iteratively fit a sky-model to the observed visibilities.



Measurement Equation :  $[A] I^m = V^{obs}$

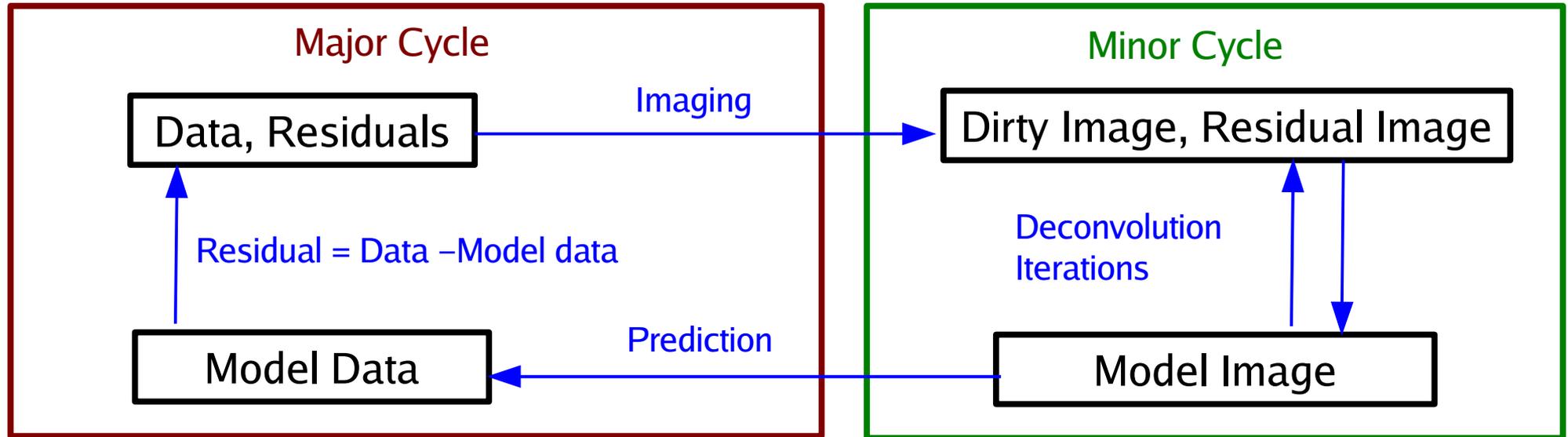
- The operator  $[A] = [S][F]$  includes the UV-coverage, Instrumental-gains, data-weights.
- The vector  $I^m$  is the sky model ( e.g. image-pixels, Gaussian set )

Fit the parameters of  $I^m$  via a weighted least-squares optimization :

- Minimize  $\chi^2 = [V^{obs} - A I^m]^T W [V^{obs} - A I^m] \implies \frac{\delta \chi^2}{\delta I^m} = 0$

# Basic Imaging and Deconvolution (recap.)

Image Reconstruction : Iteratively fit a sky-model to the observed visibilities.



Normal Equations :  $[A^T W A] I^m = [A^T W] V^{obs}$

- This describes an image-domain convolution  $I^{psf} * I^m = I^{dirty}$

Iterative Solution :  $I_{i+1}^m = I_i^m + g [A^T W A]^+ (A^T W (V^{obs} - A I_i^m))$

Diagrammatic breakdown of the iterative solution equation:

- Deconvolution:** Indicated by a green arrow pointing to the  $[A^T W A]^+$  term.
- Imaging (Gridding + iFT):** Indicated by a red arrow pointing to the  $A^T W$  term.
- Prediction (FT + de-Gridding):** Indicated by a red arrow pointing to the  $(V^{obs} - A I_i^m)$  term.

# Deconvolution Algorithms (recap)

Clean (Hogbom, Clark, Cotton-Schwab) :  $I^{sky} = \sum_x a_x \delta(x)$

Chapters 7 and 8

Maximum Entropy :  $I^{sky} = \sum_x a_x \delta(x)$  with a smoothness constraint

- Minimizing  $\chi^2$  is the same as maximizing likelihood  $e^{-\frac{1}{2} \chi^2}$  (Bayesian idea)

Multi-Scale Clean :  $I^{sky} = \sum_s [I_s^{shp} * I_s]$

Solve for components of different sizes  
(similarly, multi-resolution clean)

Cornwell, 2008  
Greisen, 2008

Adaptive-Scale-Pixel Clean :  $I^{sky} = \sum_c a_x e^{-\frac{(x-x_c)^2}{\sigma^2}}$

Solve for parameters of a Gaussian set

Bhatnagar, Cornwell 2004

Multi-Frequency Clean :

Conway et al 1991, Sault & Wieringa 1994

$$I_\nu^{sky} = \sum_t I_t \left( \frac{\nu - \nu_0}{\nu_0} \right)^t$$

Model the sky spectrum with polynomials, solve for Taylor-coefficient images.

Multi-Scale Multi-Frequency Clean :  $I_\nu^{sky} = \sum_t I_t \left( \frac{\nu - \nu_0}{\nu_0} \right)^t$  where  $I_t = \sum_s [I_s^{shp} * I_{s,t}]$

Rau, Cornwell, 2011

# Cube (Spectral-Line) Imaging (See D.Meier's lecture)

- (1) Image and deconvolve each channel separately (add them to form a continuum image).
  - Pre-average channels up to the bandwidth-smearing limit to reduce data size.
- (2) During image-restoration, convolve model images from all channels with a common 'restoring beam' derived from the angular-resolution allowed by the lowest-frequency. Smooth residual images to match the same target resolution.
- (3) Source spectra can be derived from the smoothed restored images (at low angular resolution)
- (4) Imaging-fidelity is limited to the single-frequency UV-coverage
  - Reconstructions may not be consistent across frequency
- (5) Imaging sensitivity is limited to the single-channel sensitivity  $\sigma_{chan} = \sigma_{continuum} \sqrt{N_{chan}}$ 
  - Will not deconvolve sources that are below  $\sigma_{chan}$  but above  $\sigma_{continuum}$

Cube (Spectral-Line) Imaging is the simplest form of wide-band imaging, and good for a quick-look to assess data-quality. It can handle arbitrary spectra and has no spectral-model dependence. For telescopes like JVLA and ALMA, it may suffice for many science-goals.

..... but you can often do better.

# Continuum Imaging : multi-scale multi-frequency-synthesis

(2011A&A...532A..71R, arXiv:1106.2745)

Sky Model : Collection of multi-scale flux components whose amplitudes follow a polynomial in frequency

$$I_{\nu}^{sky} = \sum_t I_t \left( \frac{\nu - \nu_0}{\nu_0} \right)^t \quad \text{where } I_t = \sum_s [I_s^{shp} * I_{s,t}]$$

Instrument Response to a Taylor-polynomial spectrum :  $I_t^{psf} = \sum_{\nu} \left( \frac{\nu - \nu_0}{\nu_0} \right)^t I_{\nu}^{psf}$

Algorithm : Linear least squares + deconvolution

Data Products : Taylor-Coefficient images  $I_0^m, I_1^m, I_2^m, \dots$  that represent the sky spectrum

- Interpret in terms of a power-law ( spectral index and curvature )  $I_{\nu} = I_{\nu_0} \left( \frac{\nu}{\nu_0} \right)^{\alpha + \beta \log(\nu/\nu_0)}$

$$I_0^m = I_{\nu_0} \quad I_1^m = I_{\nu_0} \alpha \quad I_2^m = I_{\nu_0} \left( \frac{\alpha(\alpha-1)}{2} + \beta \right)$$

- PB-correction : Model the average PB-spectrum with a Taylor-polynomial, and do a post-deconvolution Polynomial-Division

$$\frac{(I_0^m, I_1^m, I_2^m, \dots)}{(P_0, P_1, P_2, \dots)} = (I_0^{sky}, I_1^{sky}, I_2^{sky}, \dots)$$

New algorithms.....  
Still learning usage  
patterns and errors

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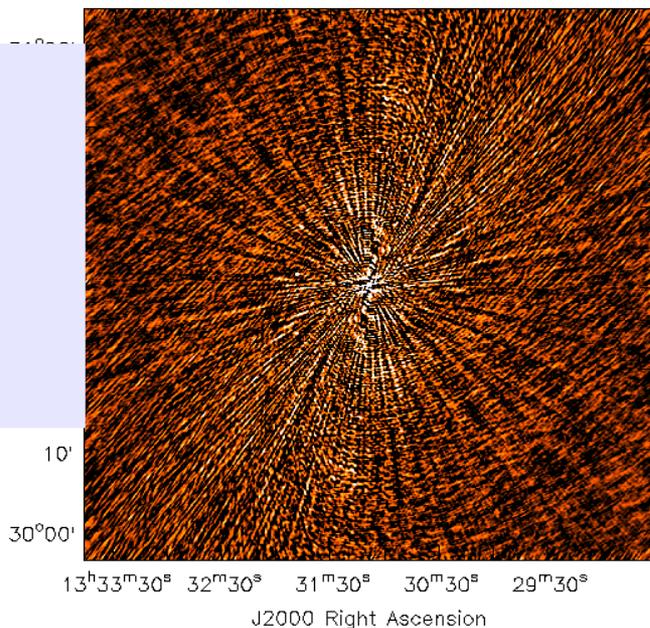
## (4) Example of wide-band imaging trials on JVLA observations of a Galactic super-nova-remnant between 1-2 GHz.

# Dynamic-range with MS-MFS : 3C286 example : Nt=1,2,3,4

**NTERMS = 1**

Rms :  
9 mJy -- 1 mJy

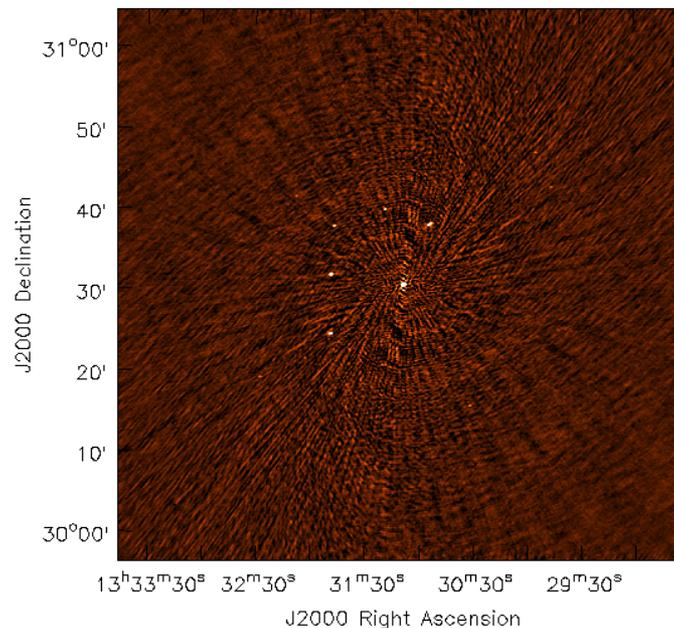
DR :  
1600 -- 13000



**NTERMS = 2**

Rms :  
1 mJy -- 0.2 mJy

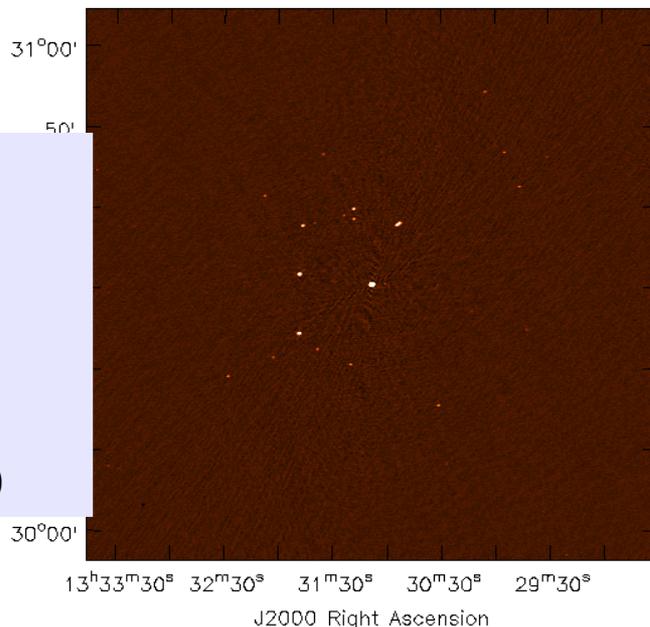
DR :  
10,000 -- 17,000



**NTERMS = 3**

Rms :  
0.2 mJy -- 85 uJy

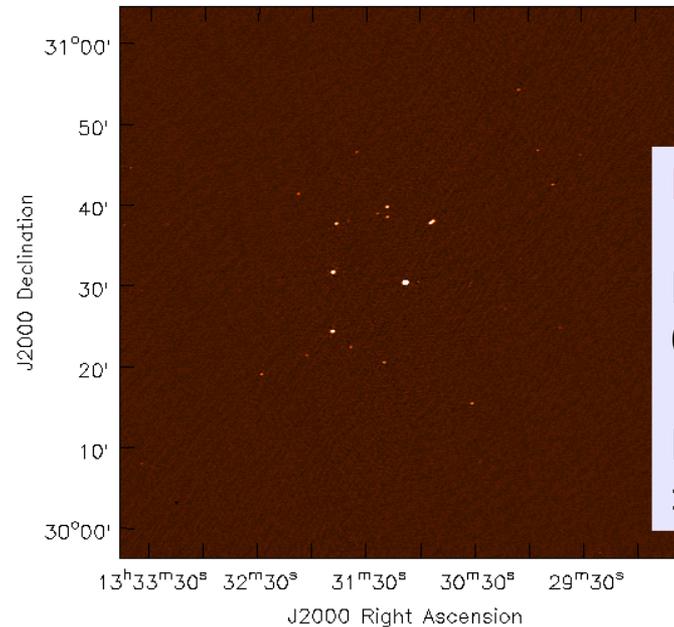
DR :  
65,000 -- 170,000



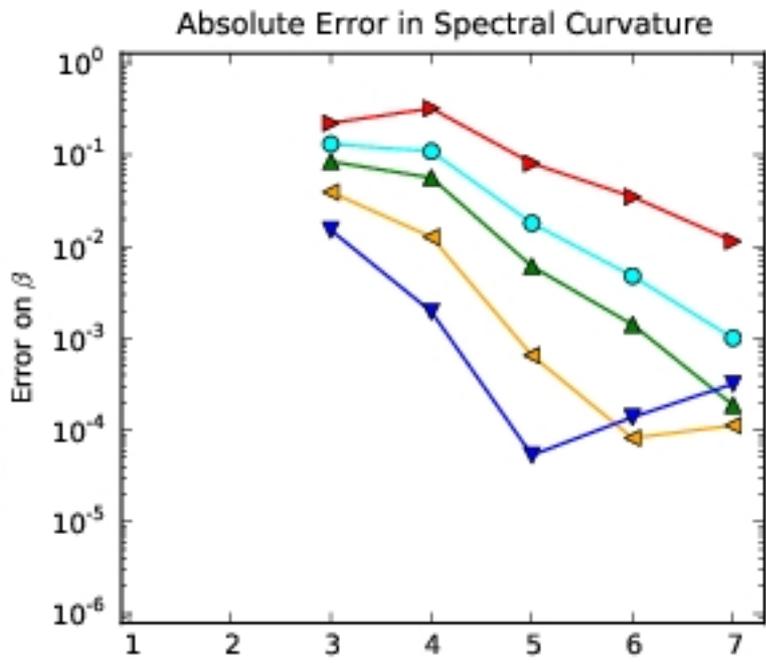
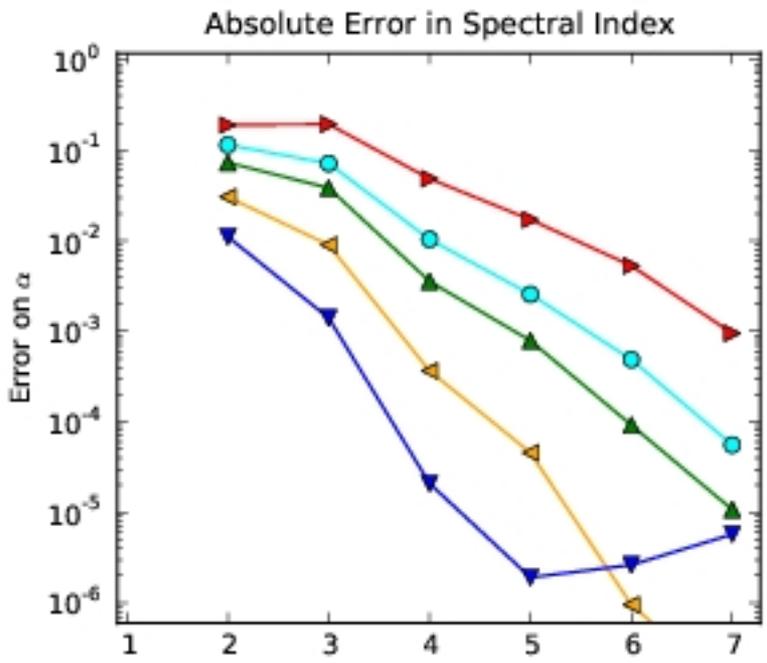
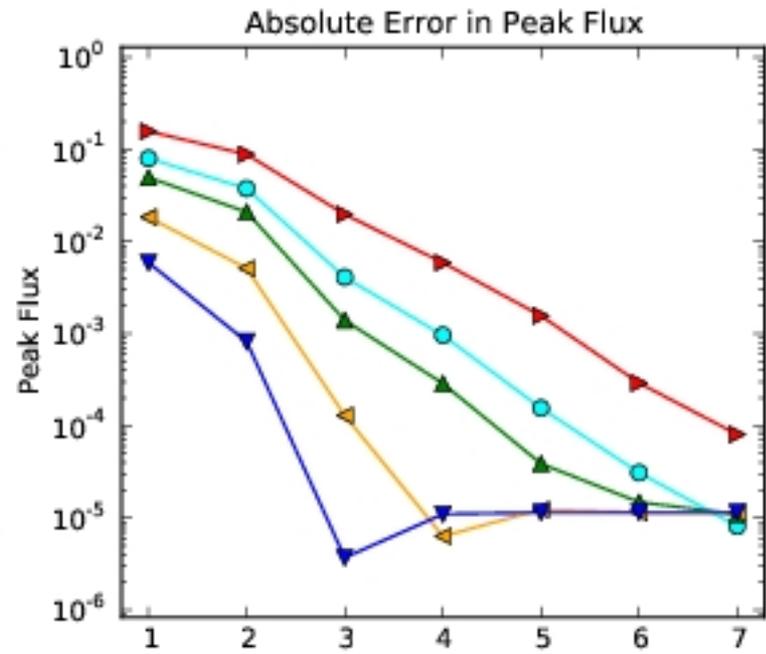
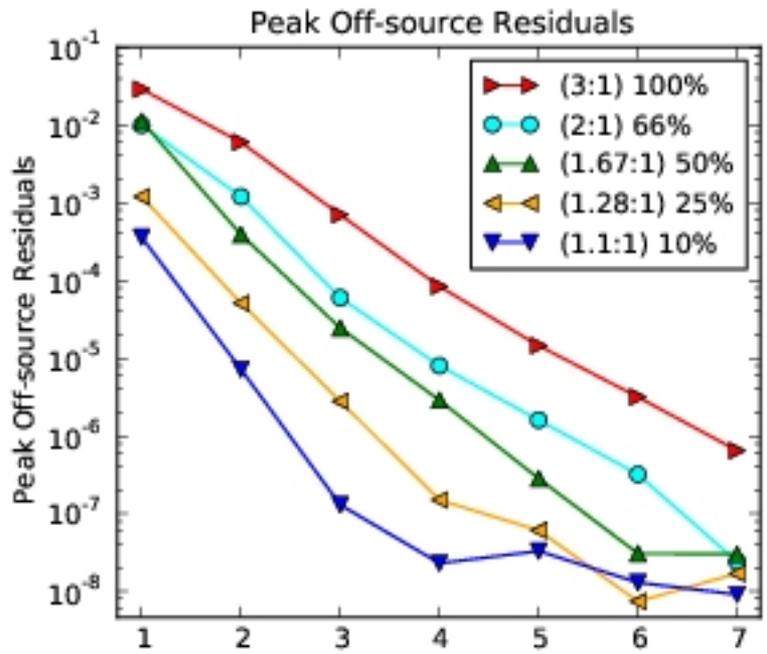
**NTERMS = 4**

Rms  
0.14 mJy -- 80 uJy

DR :  
>110,000 -- 180,000



# Errors vs Nterms, BWR ( for high signal-to-noise data )



If spectra are ignored

=> larger BWR gives larger errors

If there is high SNR,

=> more terms gives smaller errors

Note : These plots are for one point-source at the phase center, with very high signal-to-noise levels,  $I = 1.0$  Jy, Spectral Index = -1.0

In practice, use nterms>2 for high SNR (>100), and only if you can see spectral artifacts in the image with nterms=2

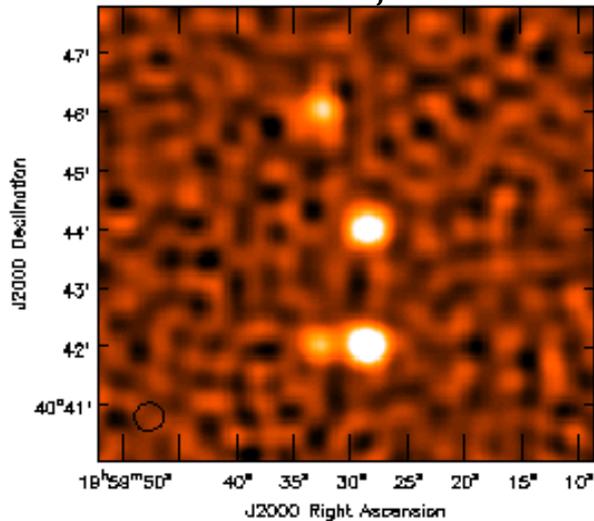
# Spectral Index Accuracy ( low signal-to-noise ratios )

Accuracy of the spectral-fit increases with larger bandwidth-ratio ( basic polynomial fitting )

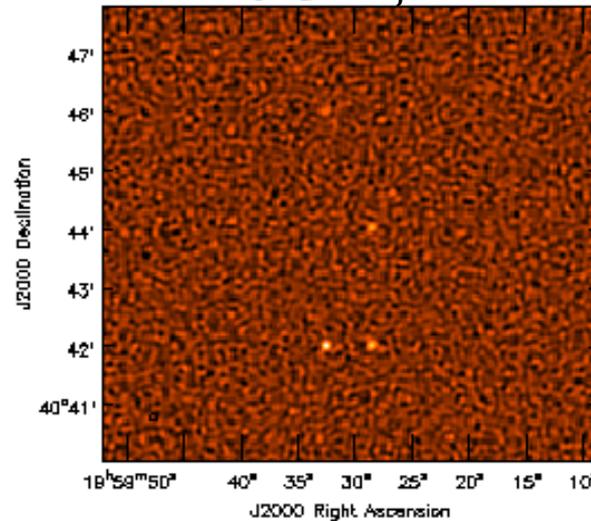
Source	Peak Flux	SNR	L alpha	C alpha	LC alpha	True
Bottom right	100 $\mu$ Jy	20	-0.89	-1.18	-0.75	-0.7
Bottom left	100 $\mu$ Jy	20	+0.11	+0.06	+0.34	+0.3
Mid	75 $\mu$ Jy	15	-0.86	-1.48	-0.75	-0.7
Top	50 $\mu$ Jy	10	-1.1	0	-0.82	-0.7

RMS  
5  $\mu$ Jy

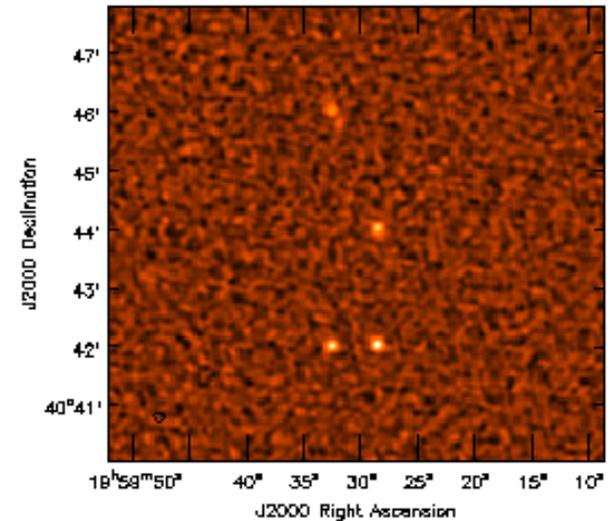
1 - 2 GHz, 4 hr



4 - 8 GHz, 4 hr



1 - 2 GHz, 4 - 8 GHz, 2 hrs each

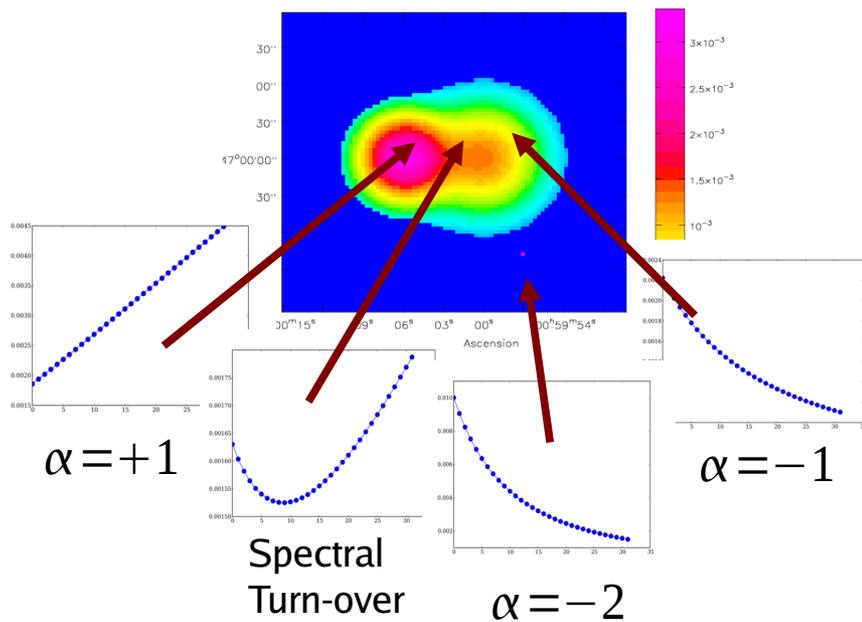


=> To trust spectral-index values, need SNR > 50 (within one band -2:1)  
For SNR < 50 need larger bandwidth-ratio.

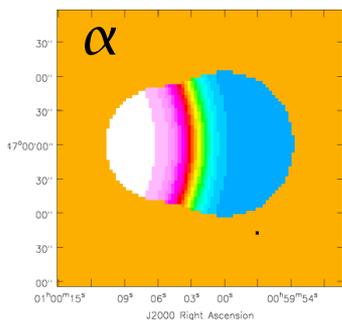
( Not tested ! )

# Example of wideband-imaging on extended-emission

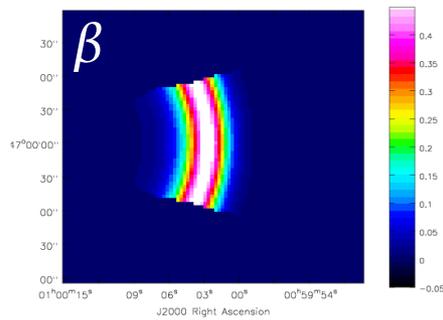
Intensity Image



Average Spectral Index

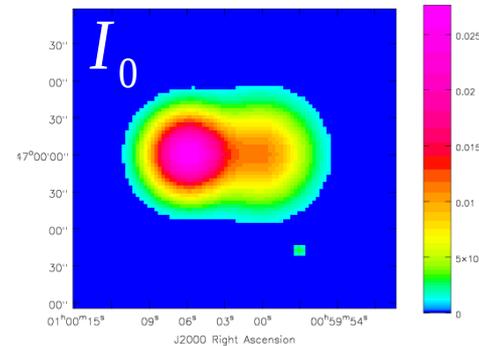


Gradient in Spectral Index

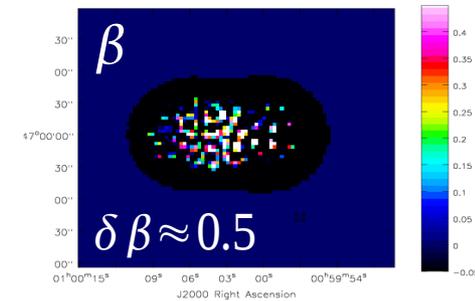
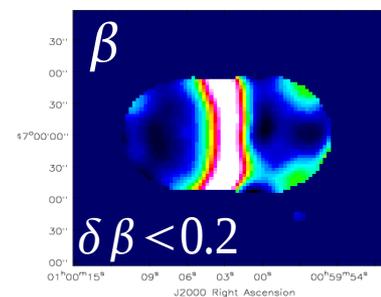
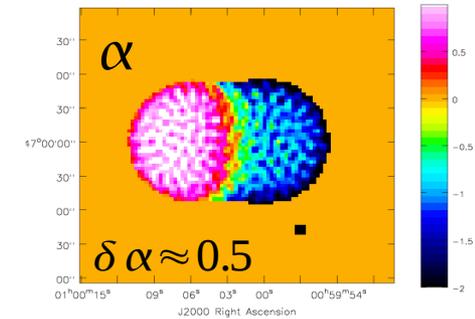
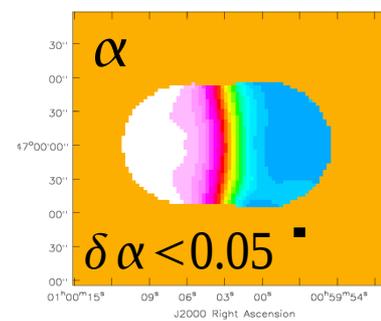
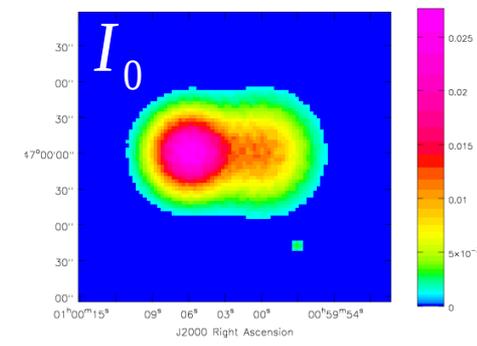


MFS

multi-scale

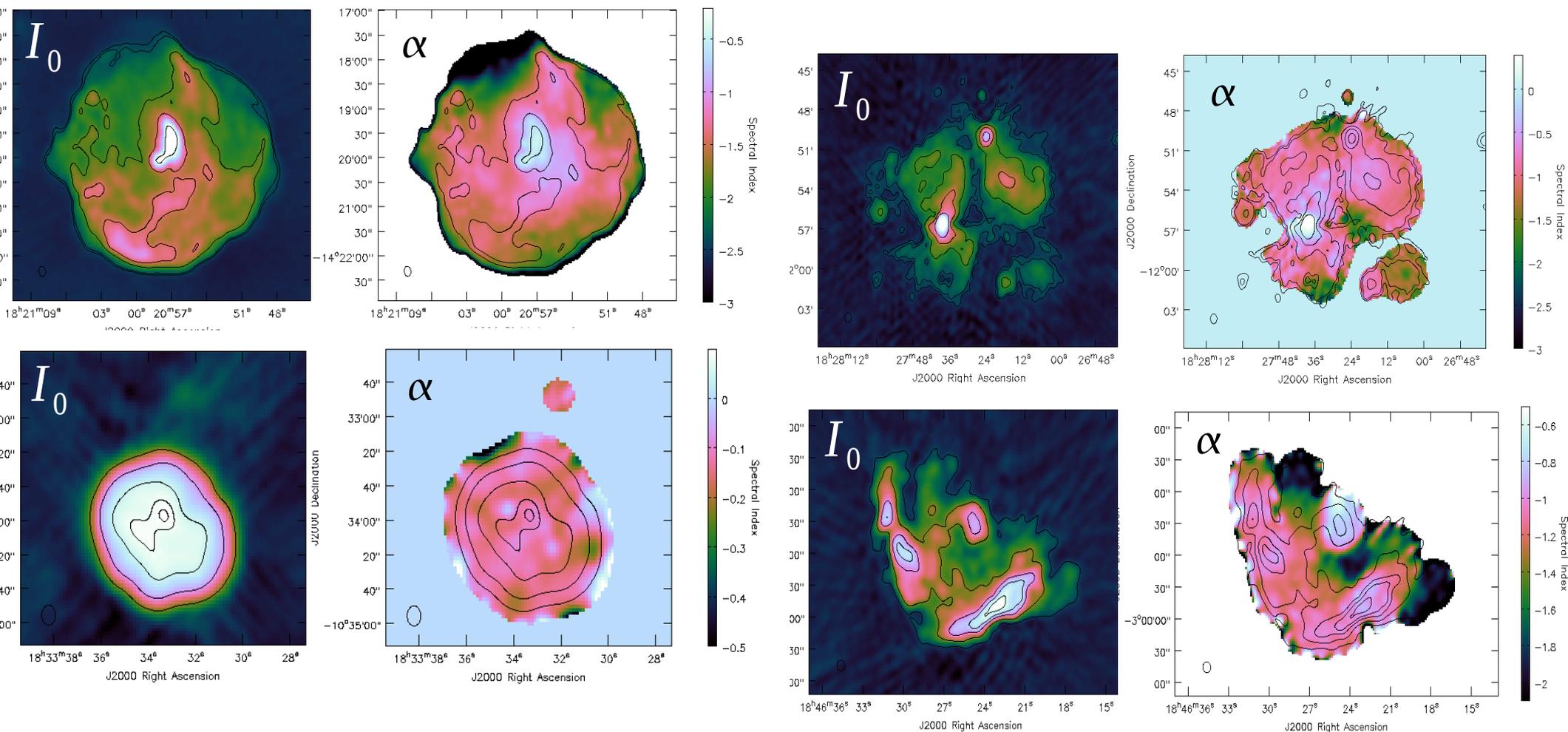


point-source



=> For extended emission - spectral-index error is dominated by 'division between noisy images'  
 - a multi-scale model gives better spectral index and curvature maps

# Extended emission – SNR example (a realistic expectation)



Results of a pilot survey ( EVLA RSRO AB1345 ). These examples used  $n_{\text{terms}}=2$ , and about 5 scales.

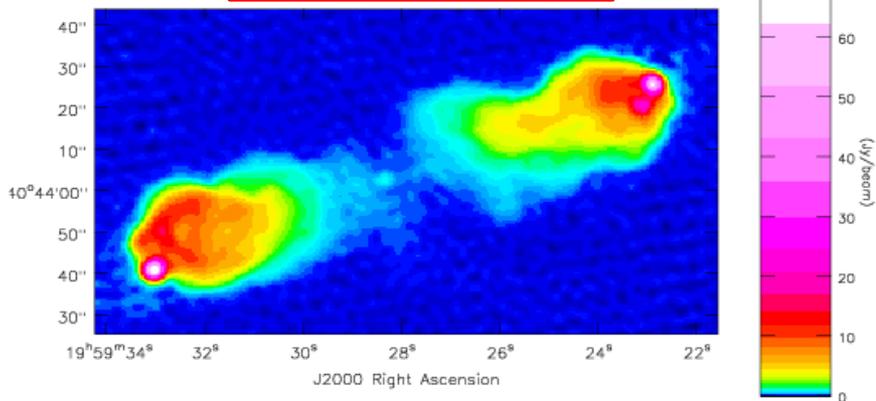
=> Within L-band and C-band, can tell-apart regions by their spectral-index (  $\pm 0.2$  ) if  $\text{SNR} > 100$ .

=> These images have a dynamic-range limit of few x 1000

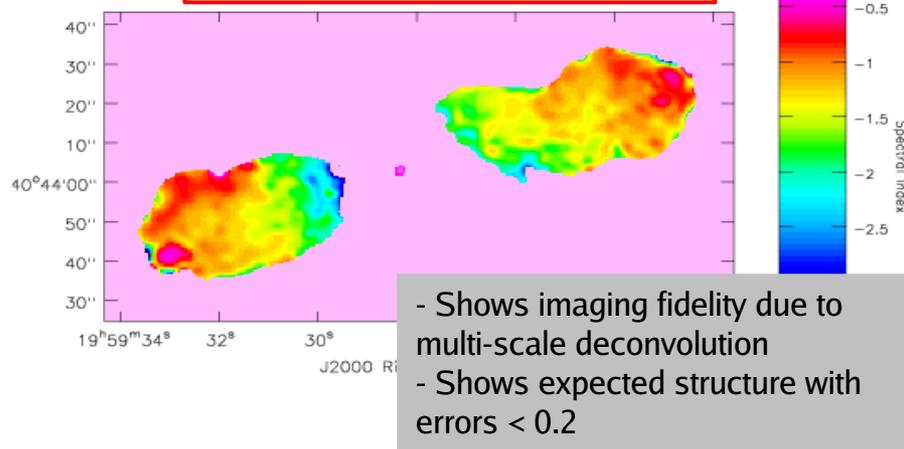
# Reconstruction ambiguity : Single-SPW imaging (vs) MS-MFS

Data : 20 VLA snapshots at 9 frequencies across L-band + wide-band self-calibration

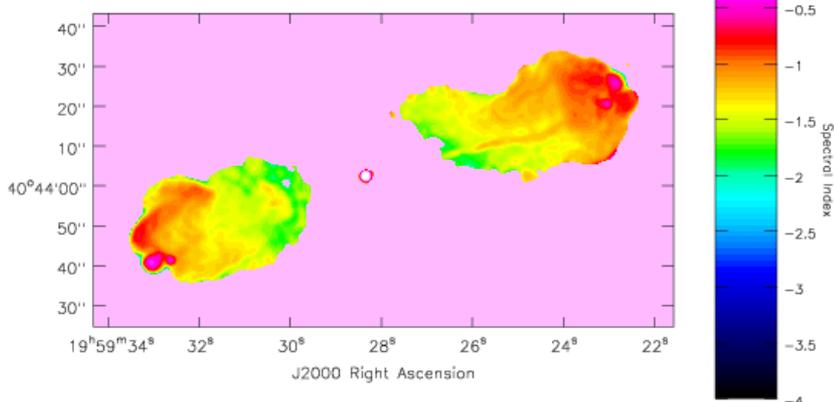
Intensity Image



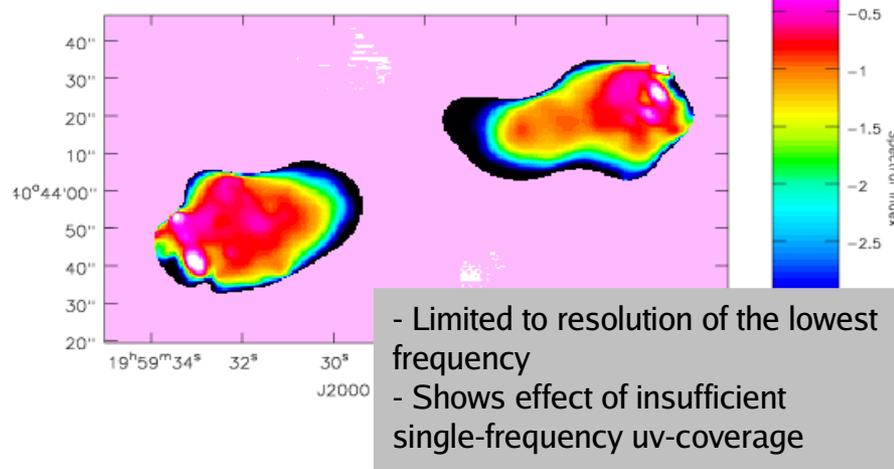
MS-MFS Spectral Index



Two-point spectrum (1.4 –4.8 GHz)



Spectral Index from single-SPW images

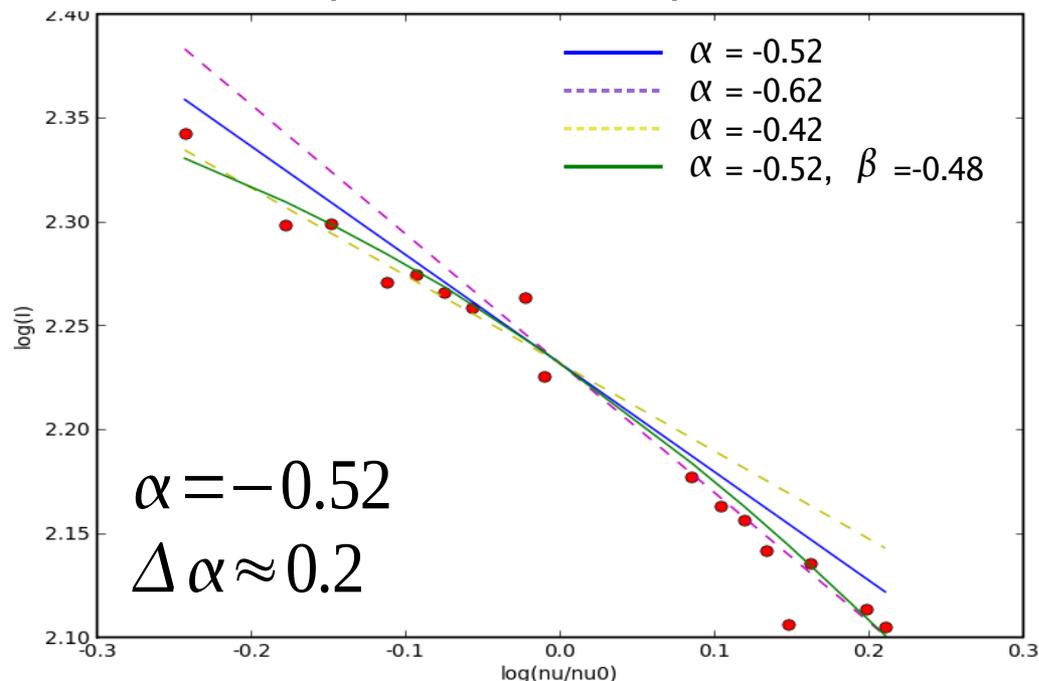


C.Carilli et al, Ap.J. 1991.  
(VLA A,B,C,D Array at L and C band)

=> It helps to use the combined uv-coverage

# Spectral Curvature

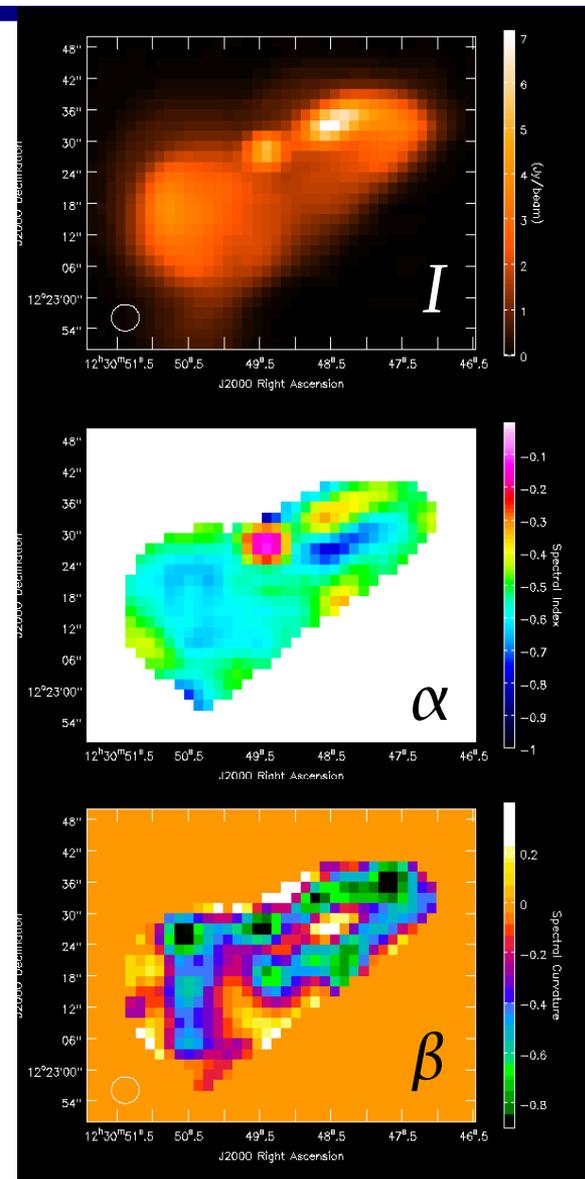
Data : 10 VLA snapshots at 16 frequencies across L-band



From existing P-band (327 MHz), L-band(1.42 GHz) and C-band (5.0 GHz) images of the core/jet

P-L spectral index : -0.36 ~ -0.45

L-C spectral index : -0.5 ~ -0.7

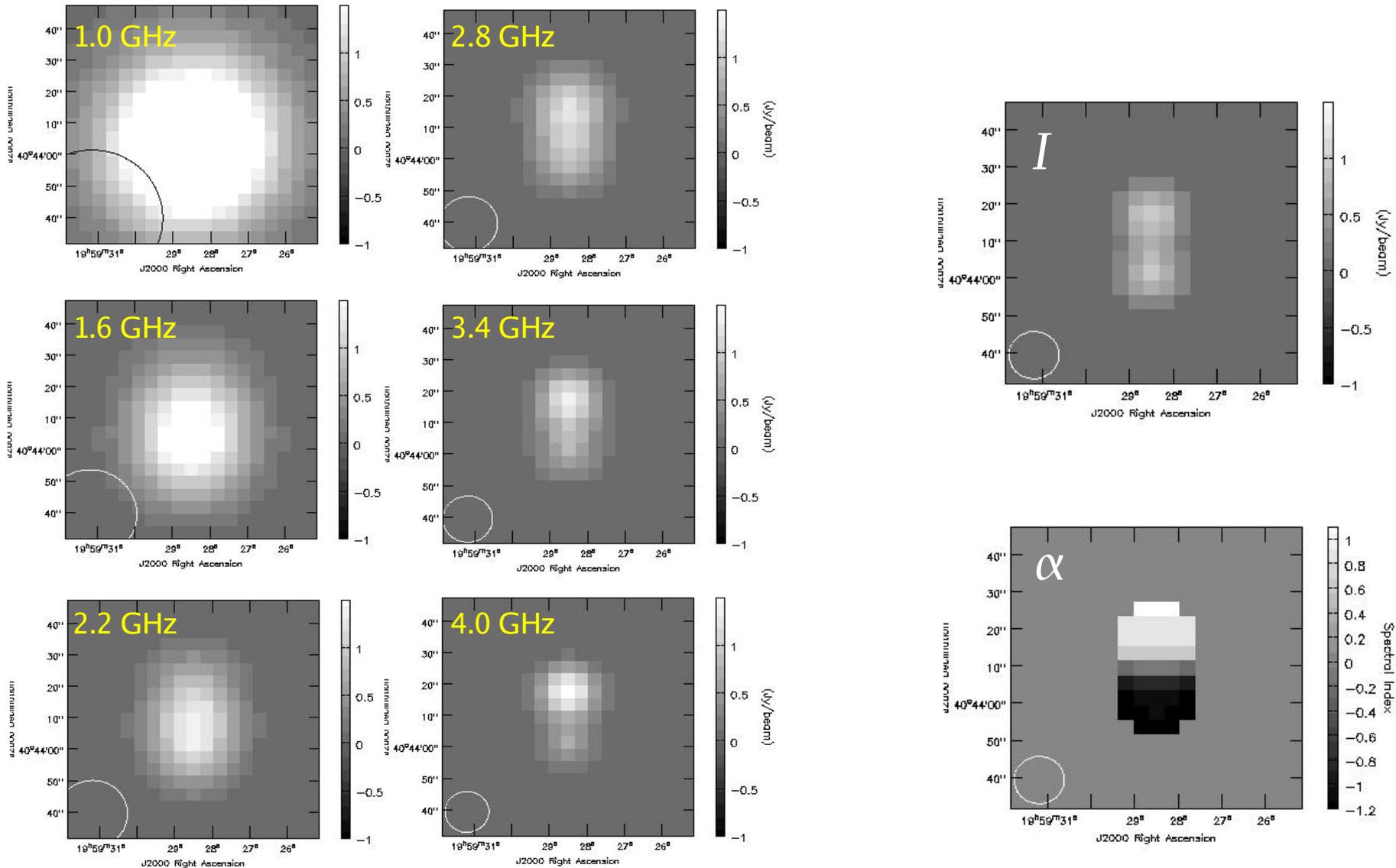


=> Need SNR > 100 to fit spectral index variation ~ 0.2 (at the 1-sigma level ... )

=> Be very careful about interpreting  $\beta$

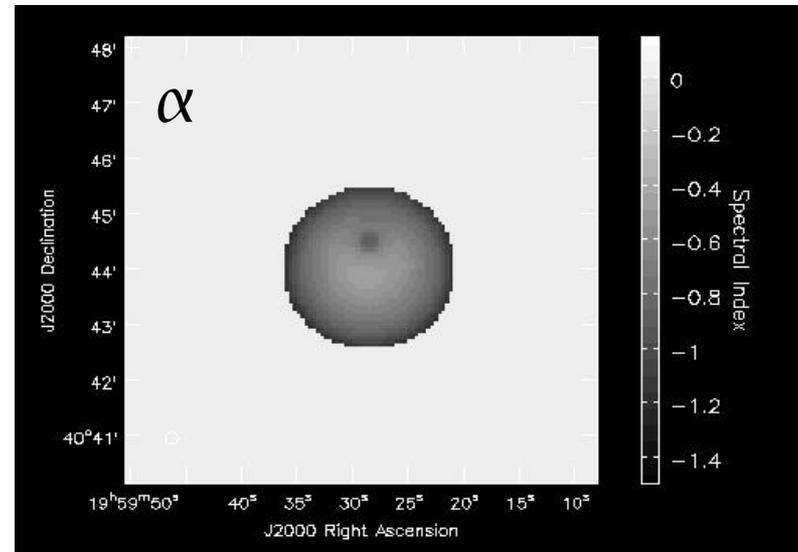
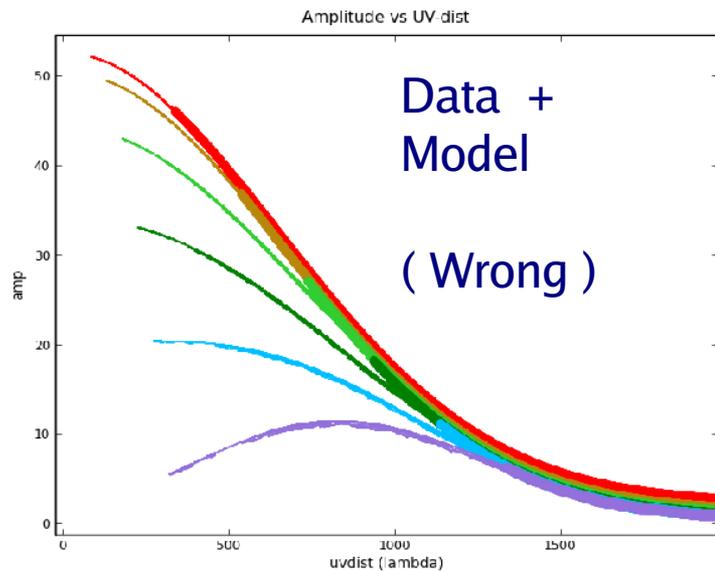
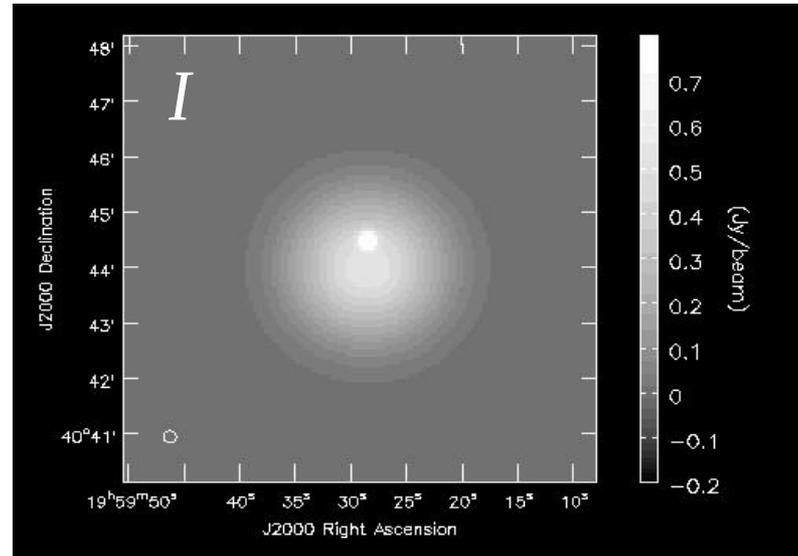
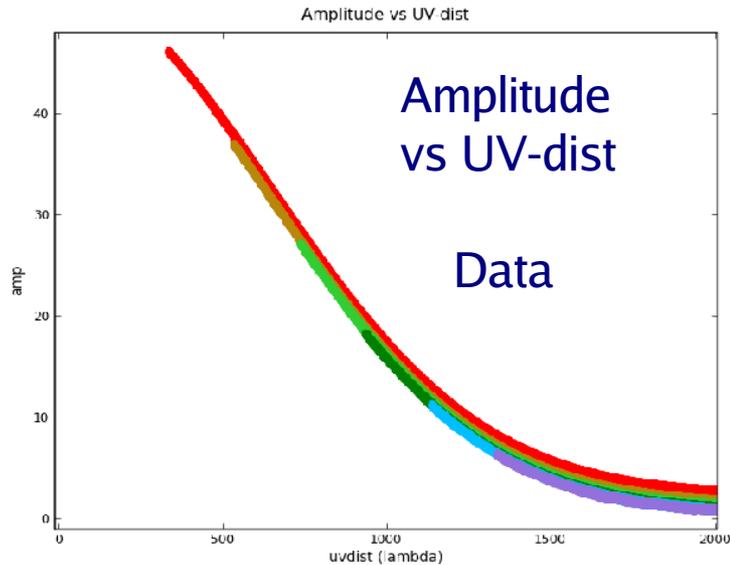
# Moderately Resolved Sources + High SNR

Can reconstruct the spectrum at the angular resolution of the highest frequency (only high SNR)



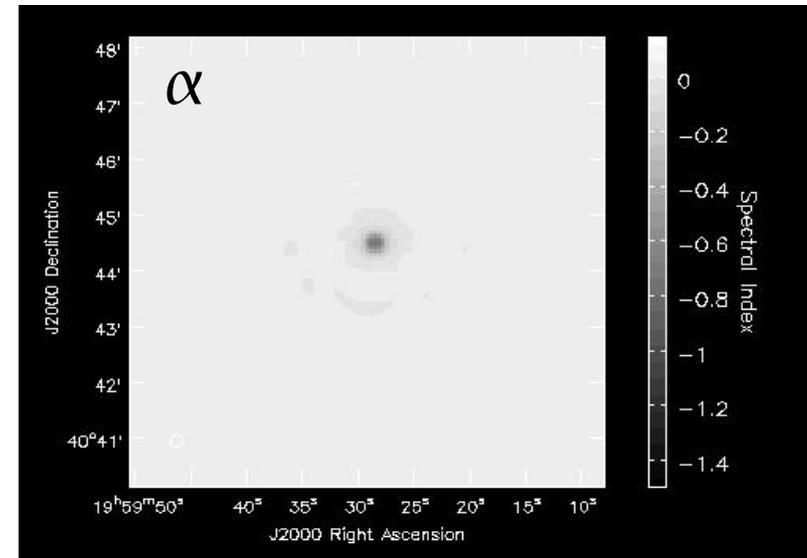
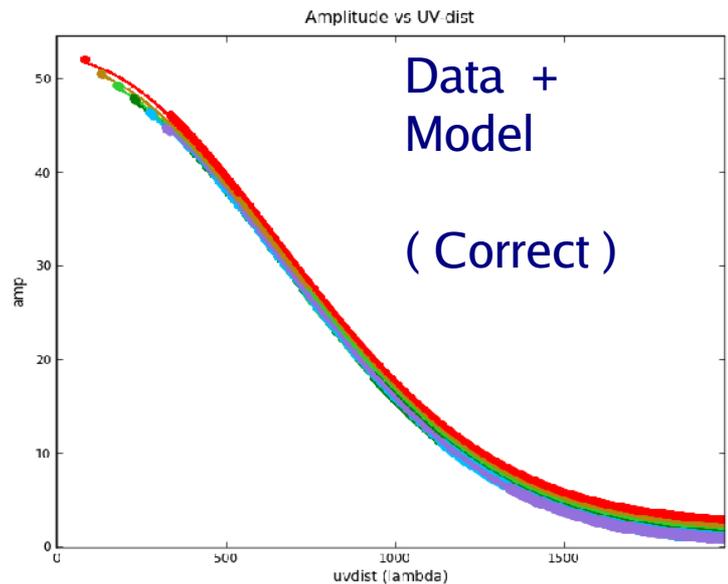
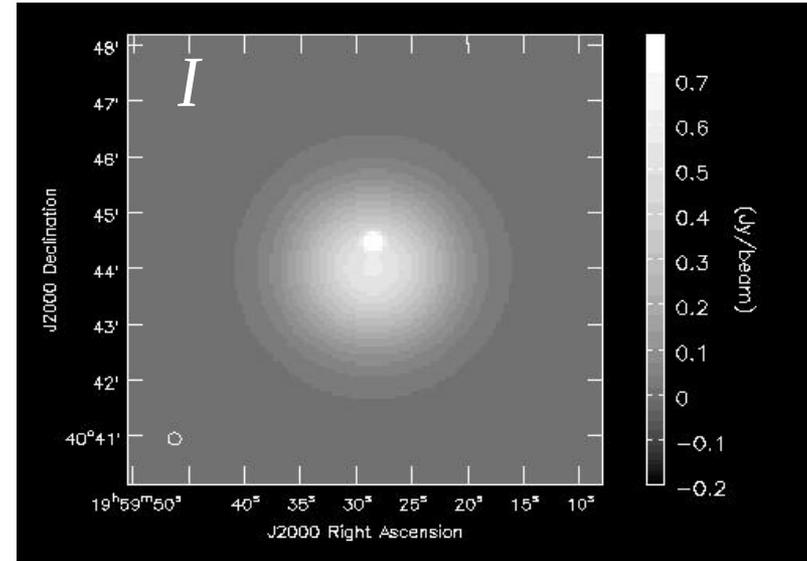
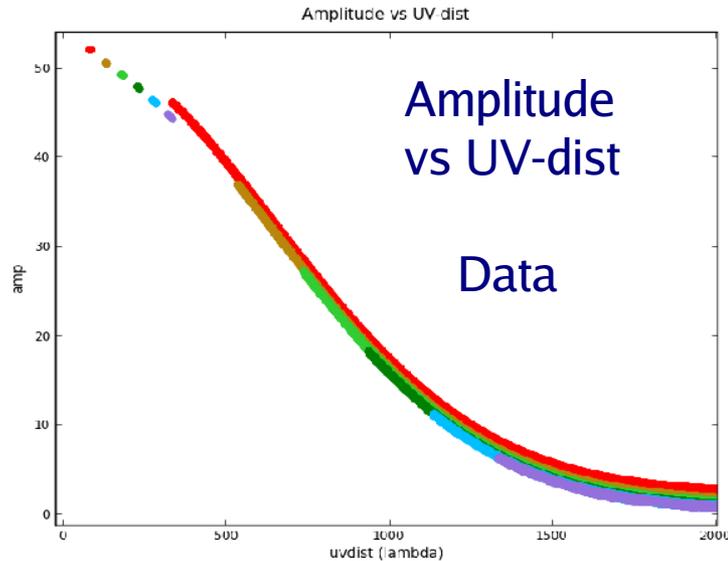
# Very large spatial scales – Unconstrained spectrum

The spectrum at the largest spatial scales is NOT constrained by the data



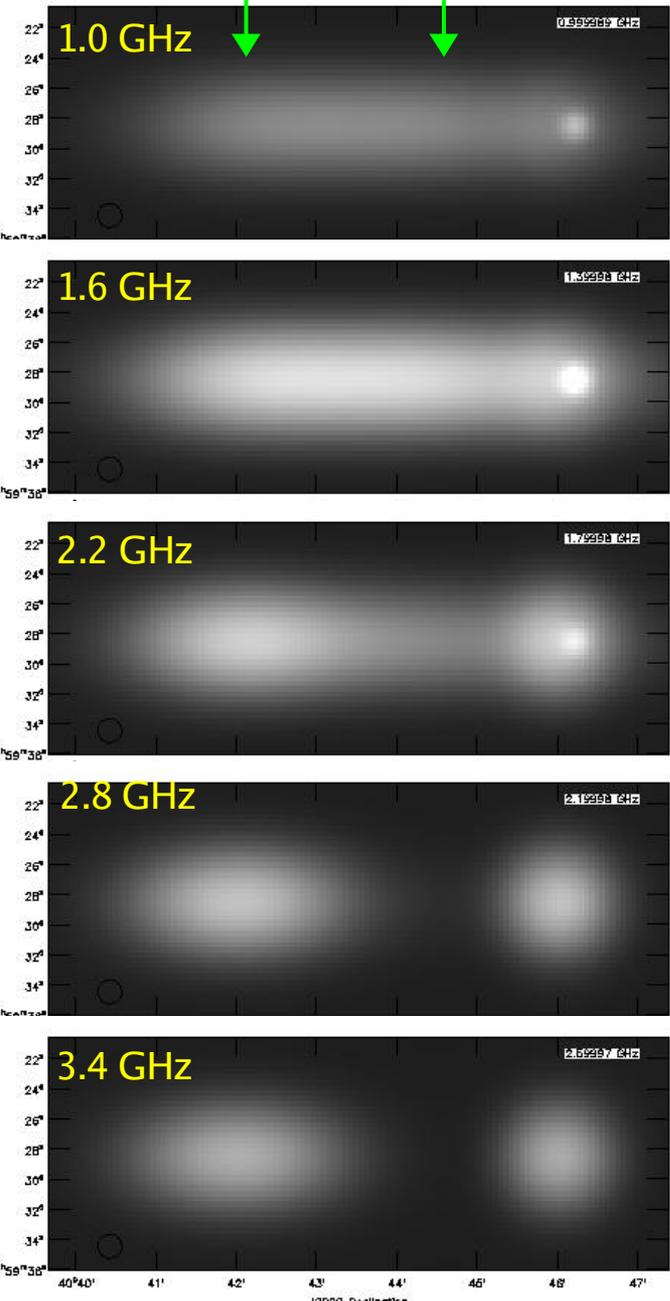
# Very large spatial scales – Need additional information

External short-spacing constraints help ( visibility data, or starting image model )



# Non power-law spectra : Polynomial Spectral Fit

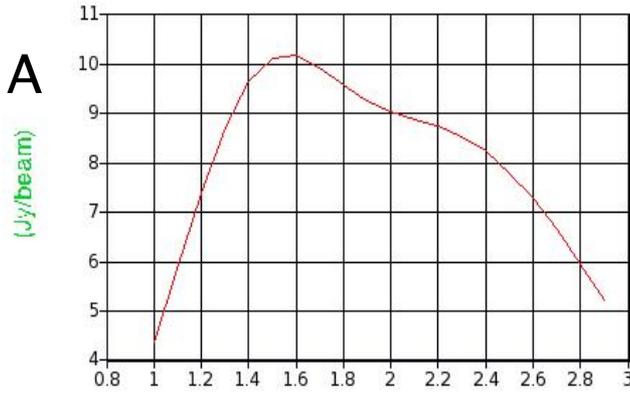
A  
B



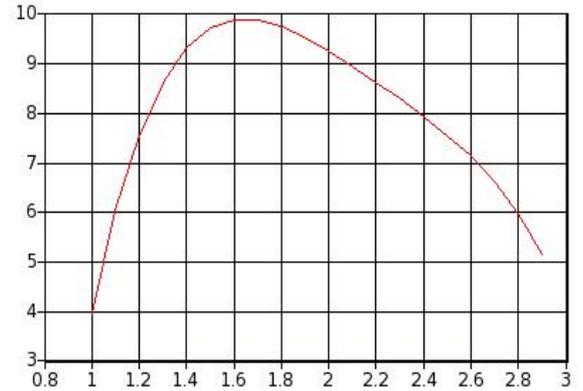
True Spectrum

Reconstructed Spectrum

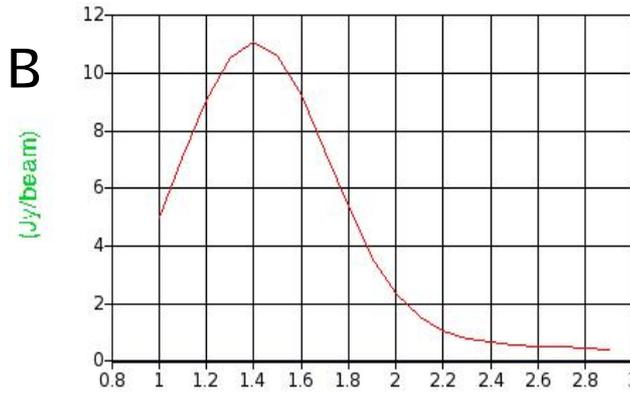
A



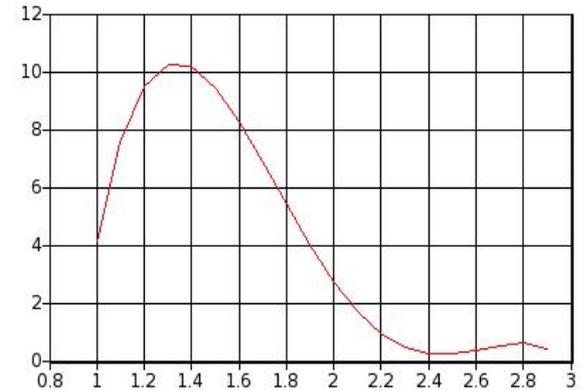
(Jy/beam)



B



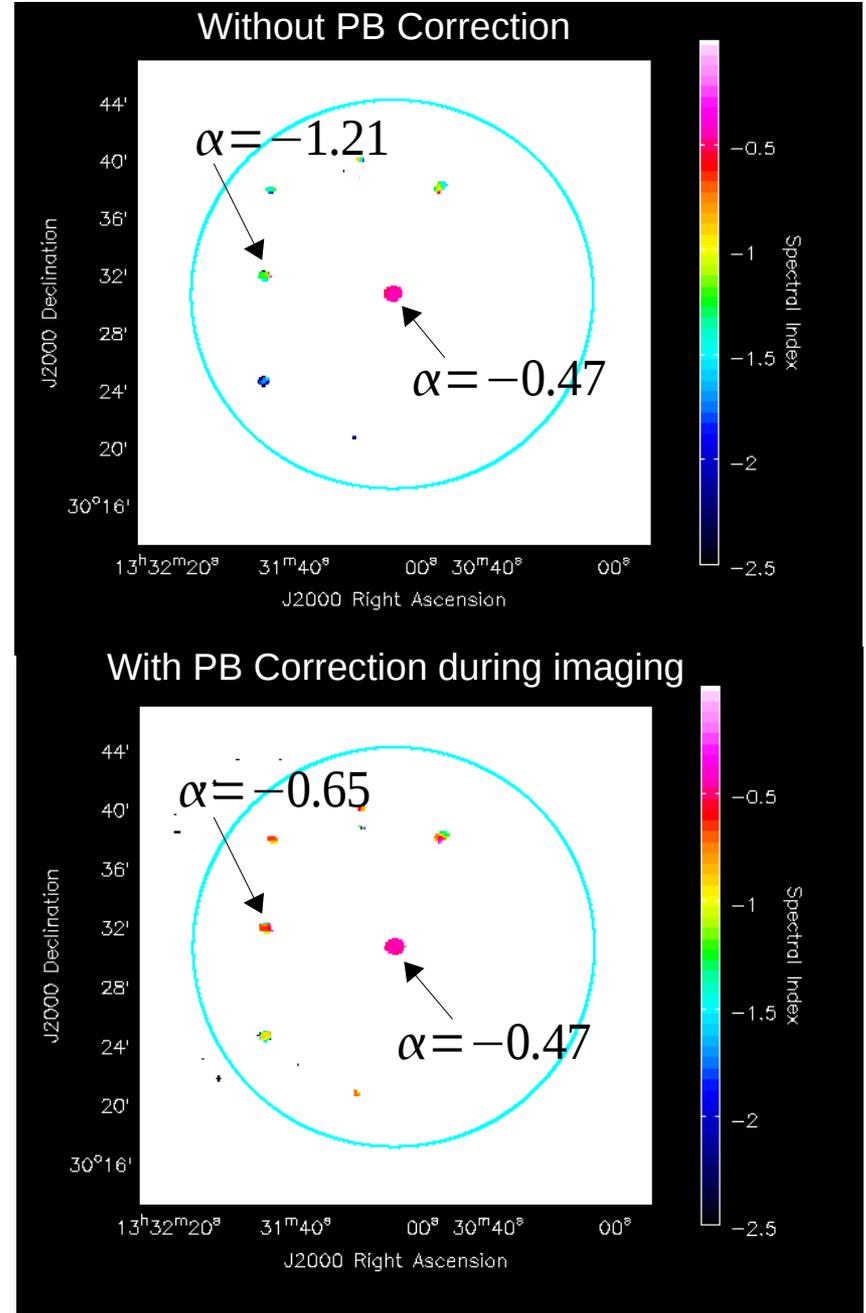
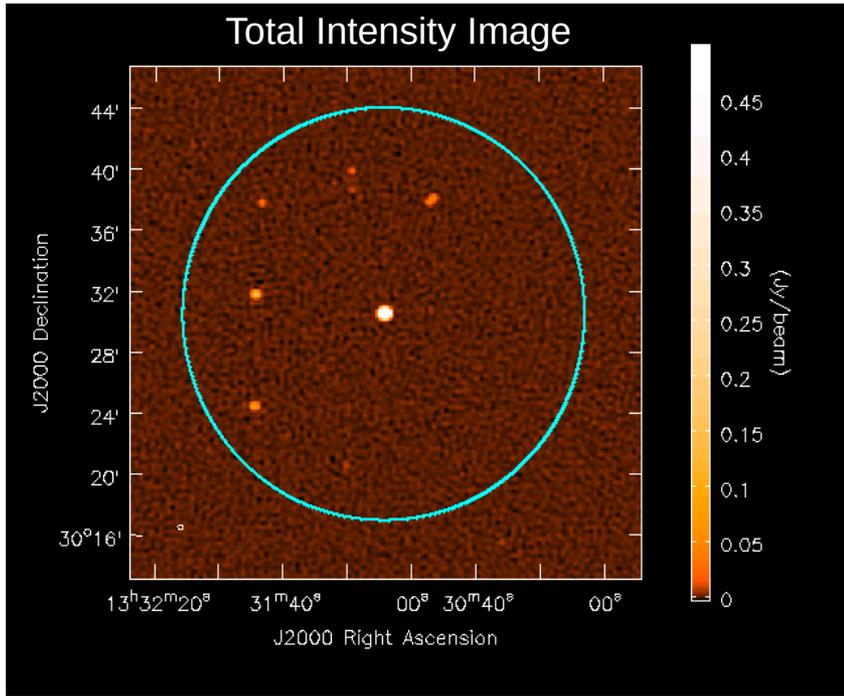
(Jy/beam)



Angular resolution depends on the highest sampled frequency at which the emission exists.

# Example of Imaging with wide-band PB (artificial spectrum)

3C286 field , C-config , L-band (30min)

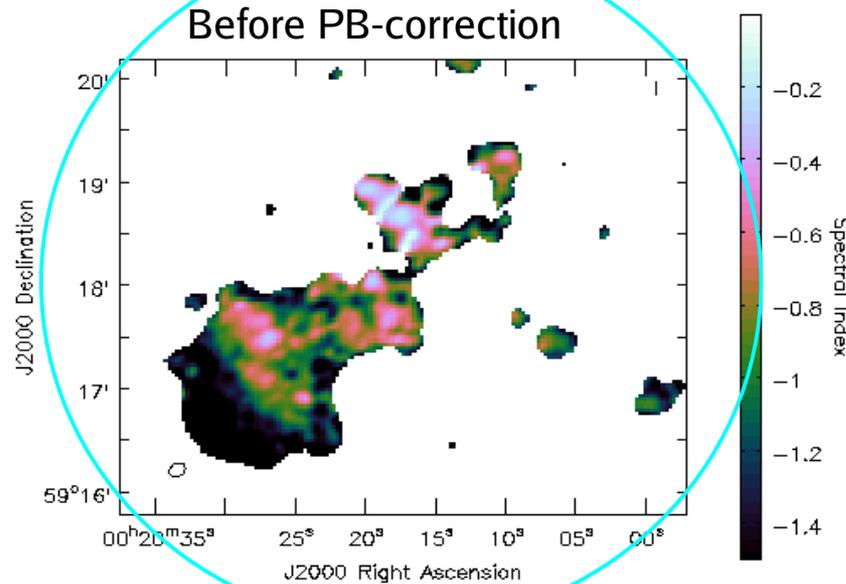
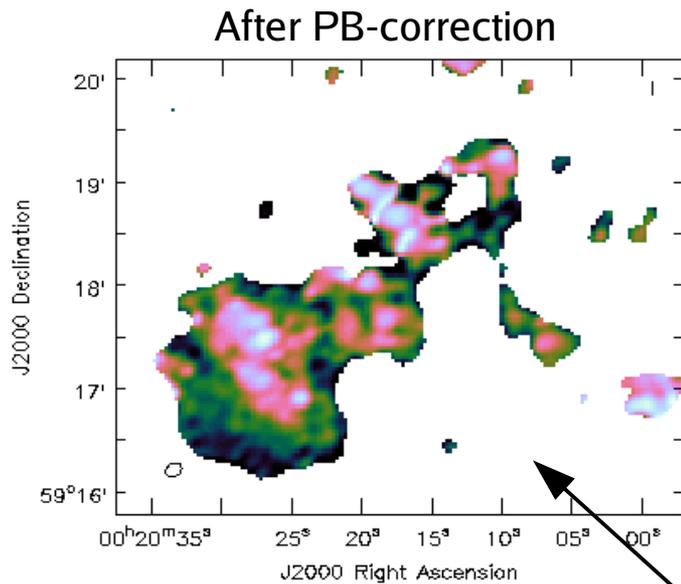


Post-deconvolution polynomial-division of the model spectrum by the PB-spectrum

Verified spectral-indices by pointing directly at one background source.

Obtained  $\delta \alpha = 0.05$  to  $0.1$  for SNR or 1000 to 20

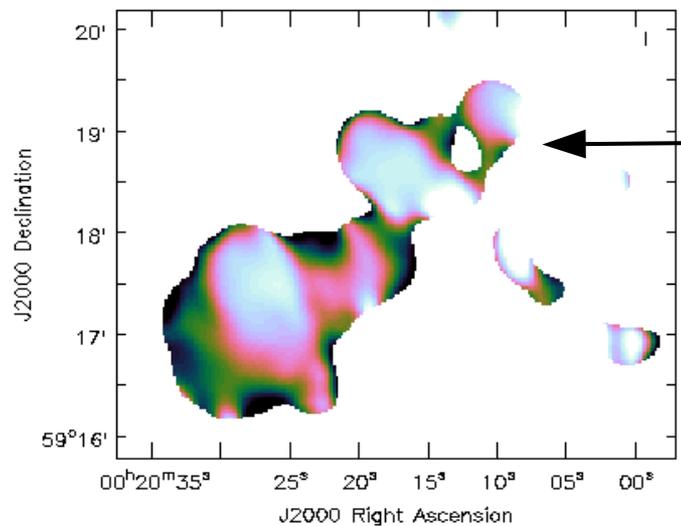
# Continuum (MS-MFS) vs Cube Imaging (with PB-correction)



IC10 Dwarf Galaxy :

Spectral Index across C-Band.

50% of PB



**MS-MFS** : Result of wide-band PB-correction after MT-MS-MFS.

**Cube** : Spectral-index map made by PB-correcting single-SPW images smoothed to the lowest resolution.

Any post-deconvolution PB-correction assumes that the primary-beam does not vary / rotate during the observation.

=> Dynamic range limit of  $10^4 \sim 10^5$

=> Valid within  $\sim$ HPBW (depends on dynamic-range)

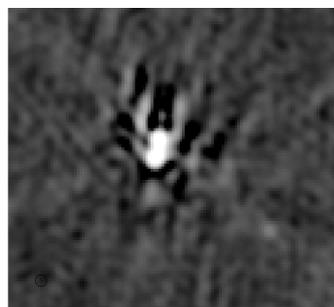
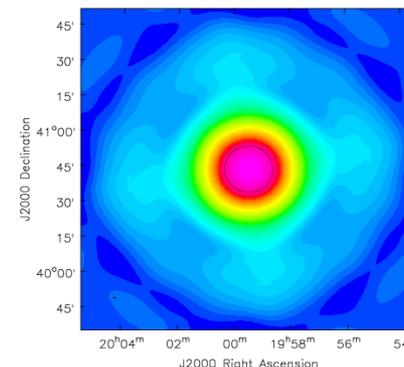
# Other wide-field issues (primary-beam, w-term, mosaicing)

Wide-Band Imaging often requires Wide-field imaging techniques.

**“Primary Beam”** : The antenna-primary beam introduces a time-varying spectrum in the data.

Any algorithm that works only with “time-averaged” beams will not suffice for high dynamic-range imaging

( S.Bhatnagar's talk will describe techniques to deal with this )

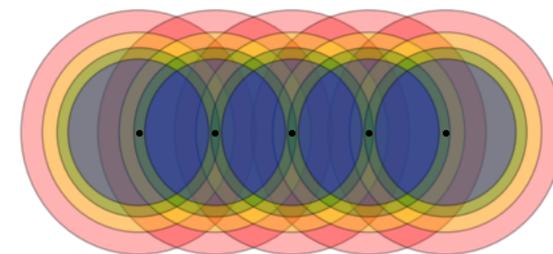


**“W-term”** : Also a frequency-dependent instrumental effect.

Narrow-band w-projection algorithm works for wide-band.

( S.Bhatnagar's talk will explain what this is )

**“Mosaicing”** : Make observations with multiple pointing and delay-tracking centers. Combine the data during (or after) image-reconstruction.



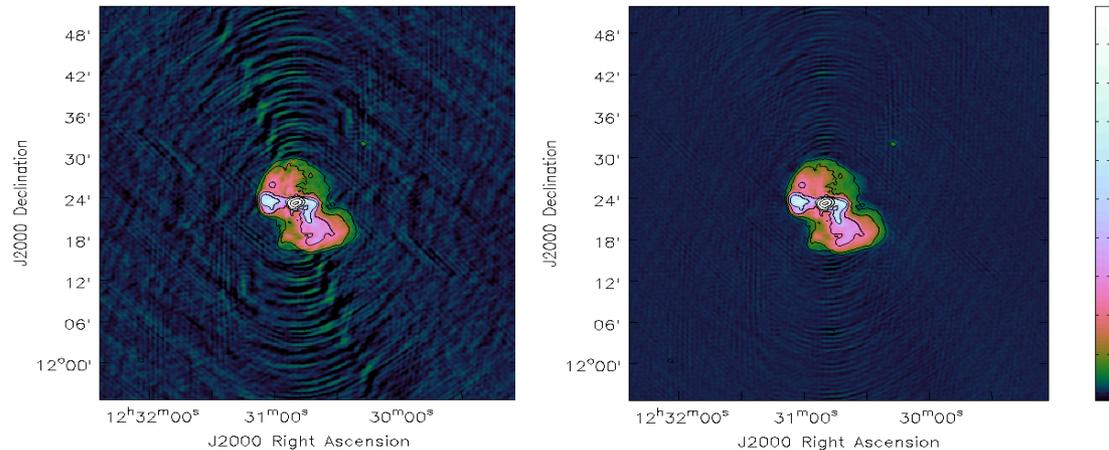
Single-pointing wide-band-imaging ideas will work for mosaics too.

( J.Ott's talk will describe mosaicing )

# Using Wide-Band Models : Self-Calibration, Continuum-subtraction

WideBand Model :  $I_0^m, I_1^m, I_2^m, \dots$

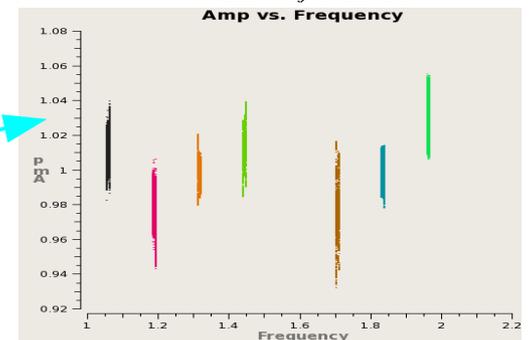
Evaluate spectrum  $I_\nu^{sky} = \sum_t I_t \left( \frac{\nu - \nu_0}{\nu_0} \right)^t$



## (1) Wide-Band Self-Calibration

- Can be used on target source, after initial calibration per spw.
- Can use it on the calibrator itself to bootstrap the model.

Amplitudes of bandpass gain solutions.....



## (2) Continuum Subtraction

- De-select frequency channels in which your spectral-lines exist.
- Make a wide-band image model of the continuum intensity and spectra
- Predict model-visibilitys over **all** channels
- Subtract these model visibilitys from the data

# Wide-Bandwidths and Polarization / Faraday-Rotation

So far, we have focused on imaging the Stokes  $I = RR + LL$  and its frequency-dependence. Stokes  $Q, U, V$  can also be imaged (cube or continuum).

$$Q = RR + I LL, \quad U = RR - I LL, \quad V = RR - LL$$

$Q, U, V$  also change with frequency,

- Their spectra usually do not follow a power-law.
- Spectra may not even be smooth (i.e. cannot use a Taylor-polynomial) => Make a Cube

## Faraday Rotation-Measure Synthesis

Brentjens, 2008

Make images of  $F(\phi)$ , the polarized surface-brightness at various Faraday-depths.

-  $P = Q + I U$  : Make spectral cubes for  $Q$  and  $U$  separately, and calculate  $P$

- For each pixel in the  $P$ -cube, solve  $P(\lambda^2) = \int F(\phi) e^{2\pi i \phi \lambda^2} d\phi$  for  $F(\phi)$

This calculation is currently done post-deconvolution, but it could be folded into the major/minor cycle framework.

# Outline

## (1) What is wide-band imaging ?

- Bandwidth and sensitivity
- Frequency-dependent Instrument and Sky
- Bandwidth smearing
- Multi-frequency synthesis

## (2) Imaging Algorithms

- Recap. of image-reconstruction methods
- Cube vs Continuum imaging (intensity and spectrum)

## (3) Examples of various effects/corrections/errors

(4) Example of wide-band imaging trials on JVLA observations of a Galactic super-nova-remnant between 1-2 GHz.

## Example : SNR G55.7+3.4

7 hour synthesis, L-Band, 8 spws x 64 chans x 2 MHz, 1sec integrations

Due to RFI, only 4 SPWs were used for initial imaging ( 1256, 1384, 1648, 1776 MHz )

( All flagging and calibration done by D.Green )

J2000 Declination

30'

15'

22°00'

45'

30'

15'

21°00'

45'

Imaging Algorithms applied : MS-MFS with W-Projection

( nterms=2, multiscale=[0, 6, 10, 18, 26, 40, 60, 80] )

Peak Brightness : 6.8 mJy

Extended Emission : ~ 500 micro Jy

Peak residual : 65 micro Jy

Off-source RMS : 10 micro Jy (theoretical = 6 micro Jy)

19<sup>h</sup>26<sup>m</sup>

24<sup>m</sup>

23<sup>m</sup>

22<sup>m</sup>

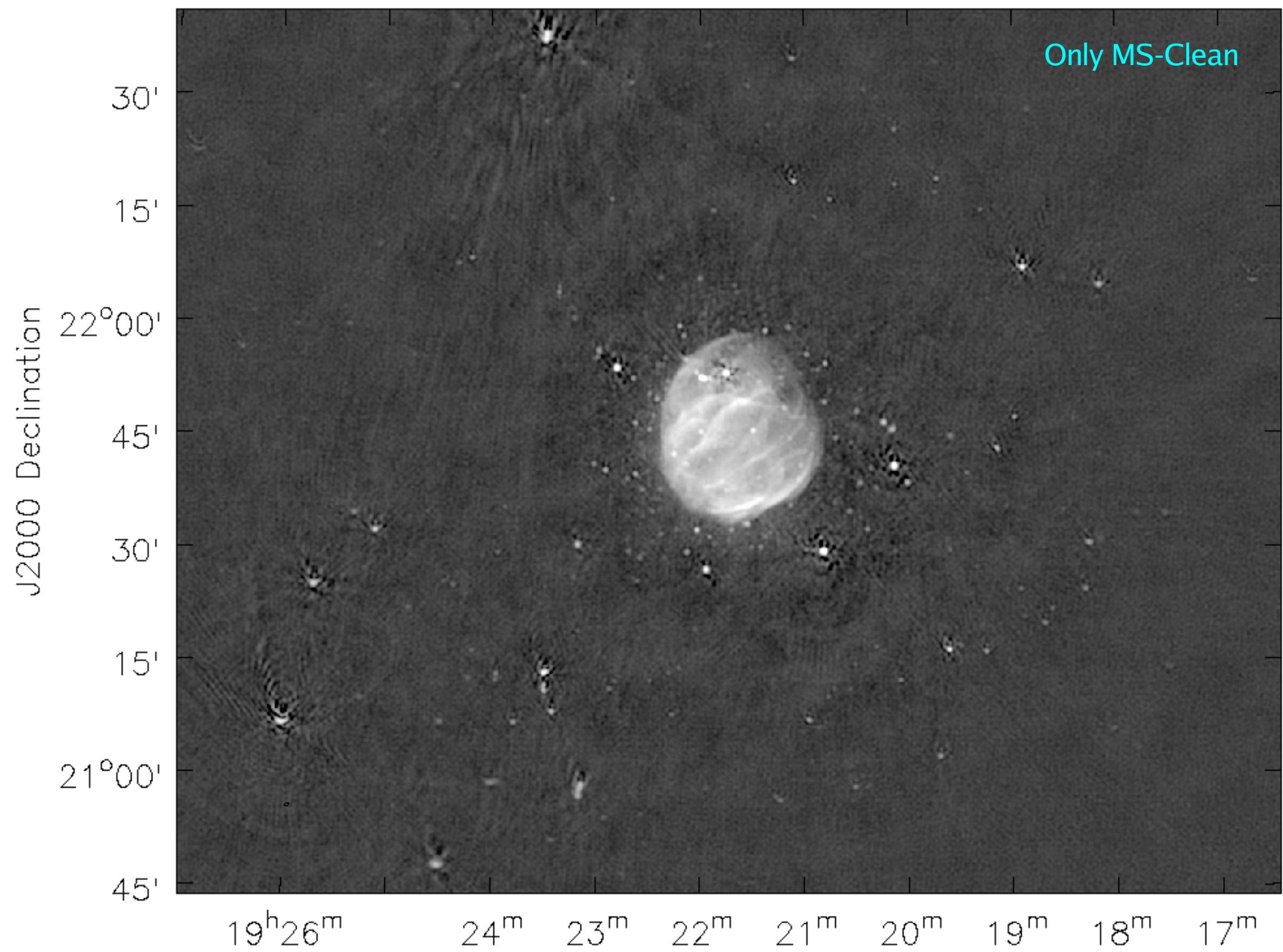
21<sup>m</sup>

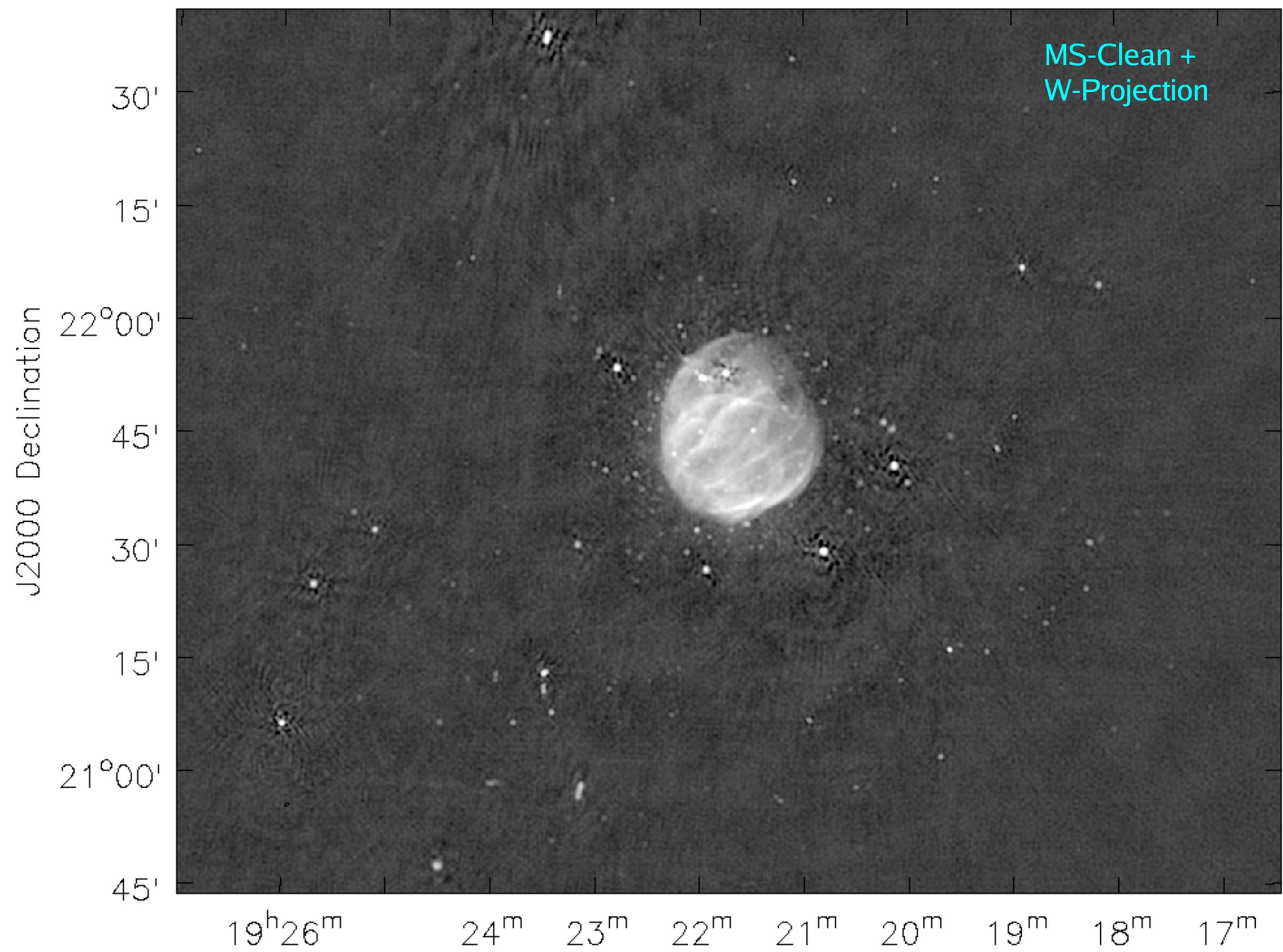
20<sup>m</sup>

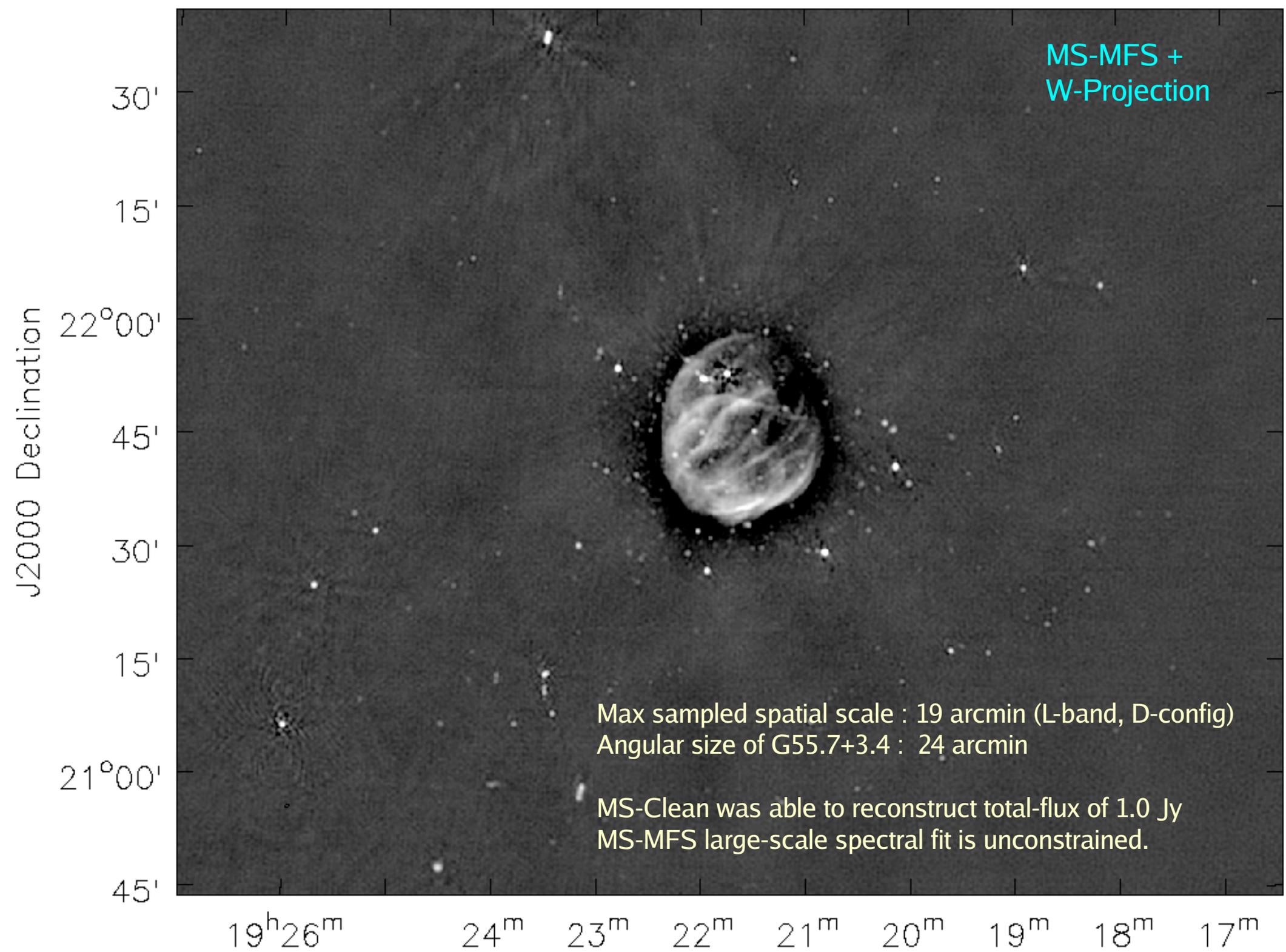
19<sup>m</sup>

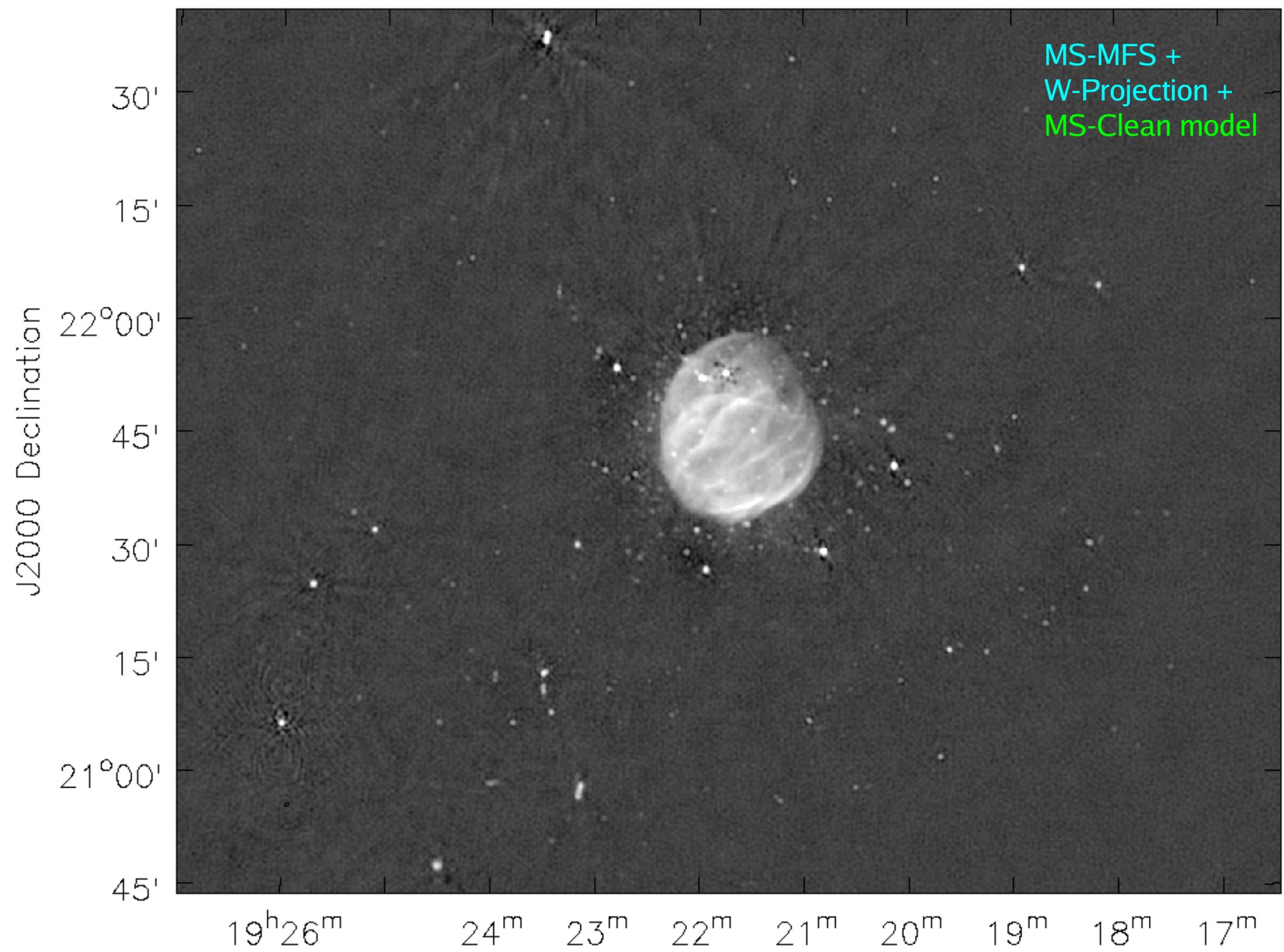
18<sup>m</sup>

17<sup>m</sup>

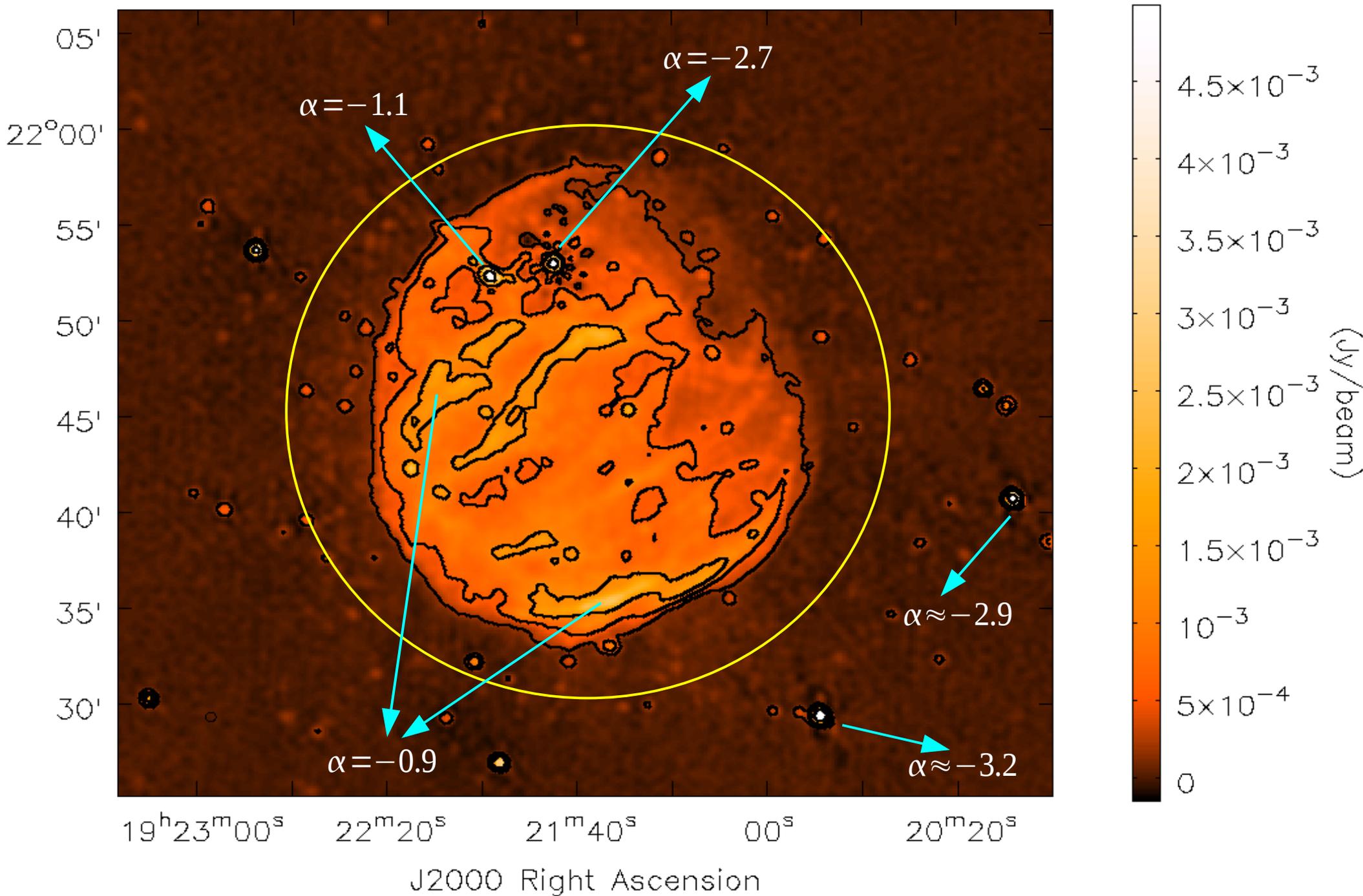








# G55.7+3.4 : Supernova-Remnant + Pulsar



# Example of wide-field sensitivity, because of wide-bandwidths

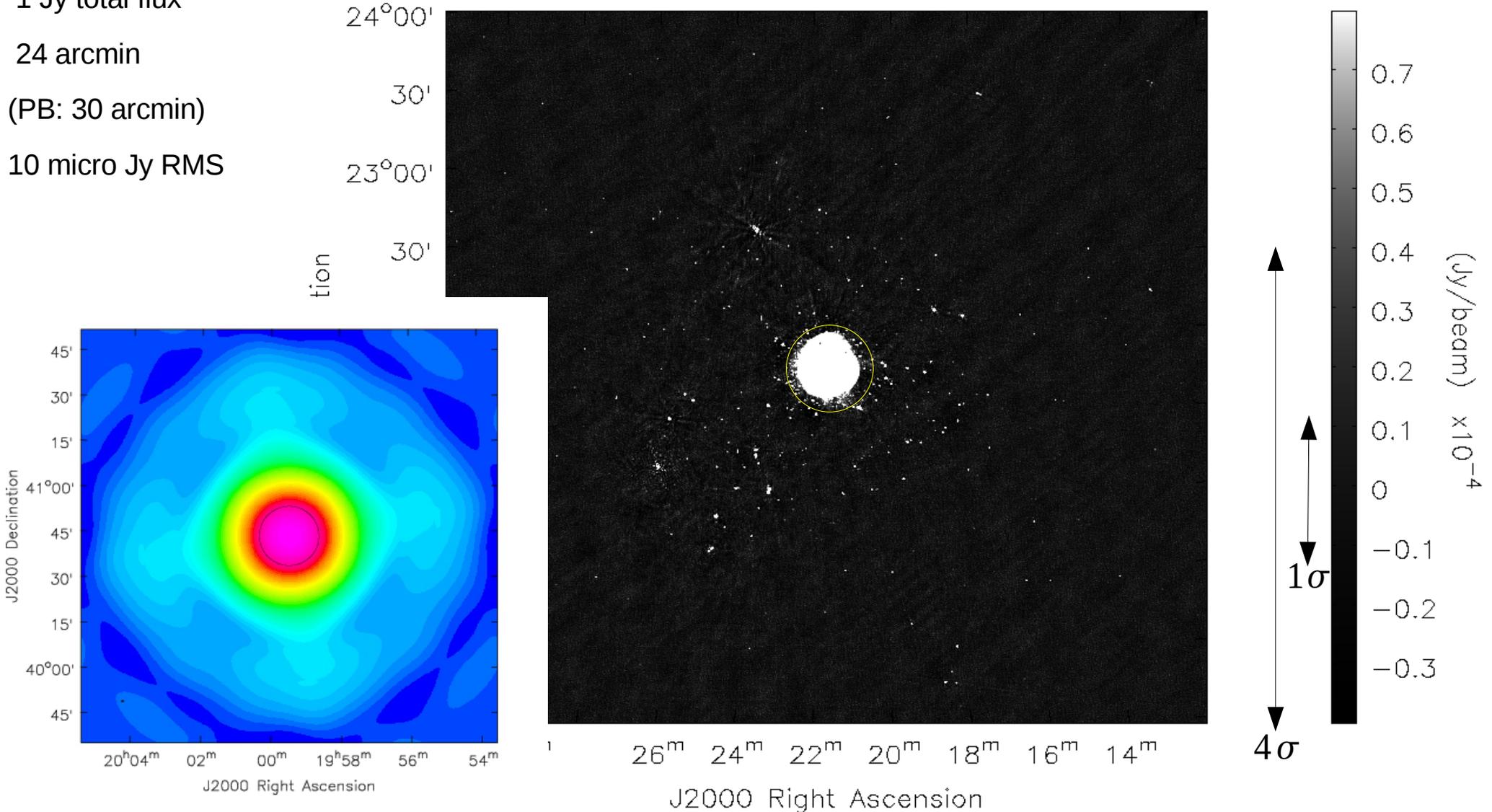
G55.7+3.4 : Galactic supernova remnant : 4 x 4 degree field-of-view from one EVLA pointing

1 Jy total flux

24 arcmin

(PB: 30 arcmin)

10 micro Jy RMS



# Summary

Broad-Band Receivers



Cube-Imaging (or per SPW) will suffice for a quick-look.



Multi-Frequency-Synthesis for better sensitivity



Reconstruct Intensity and Spectrum during Imaging

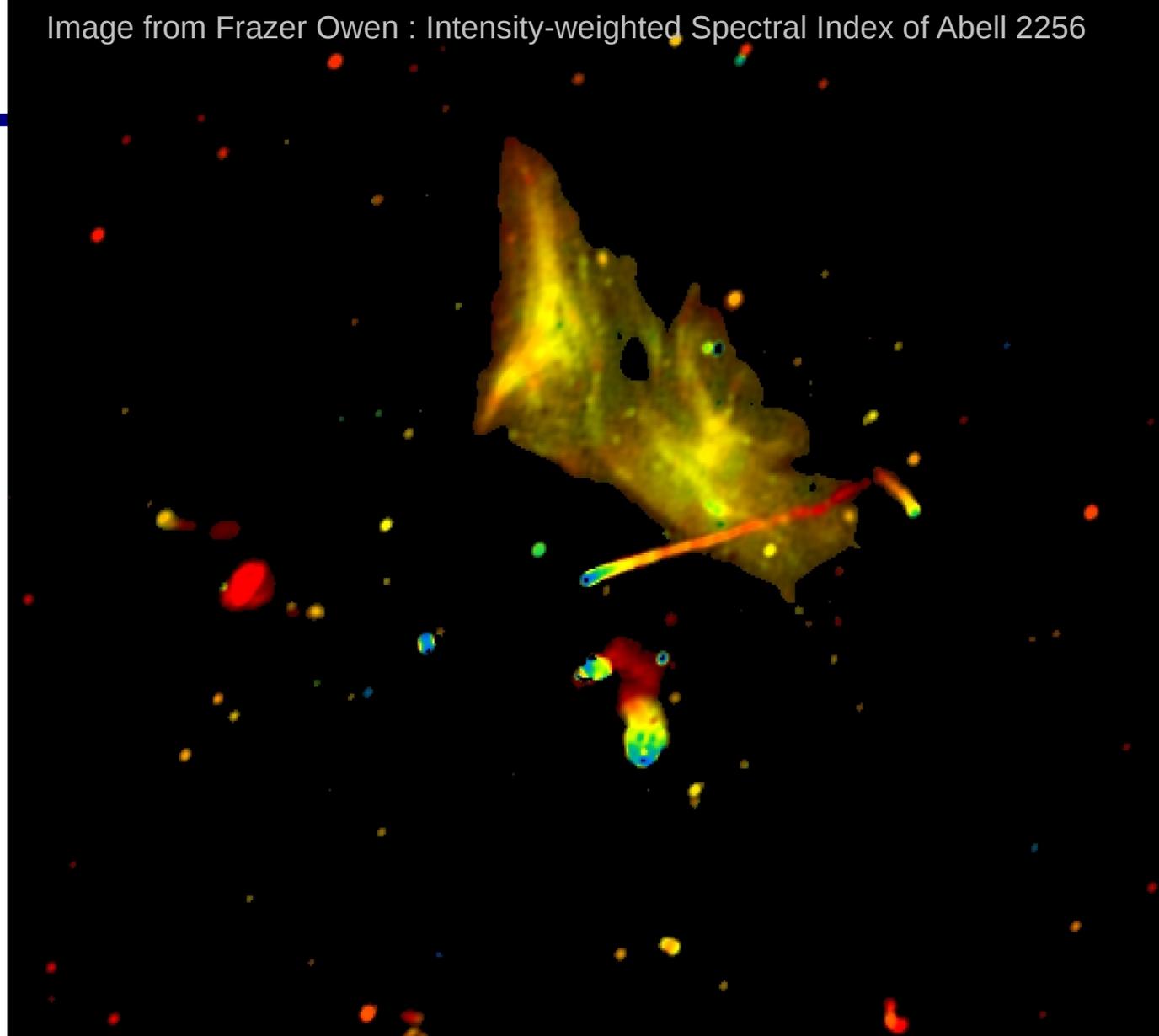


Pay attention to the **many** sources of error in the model-fitting process.



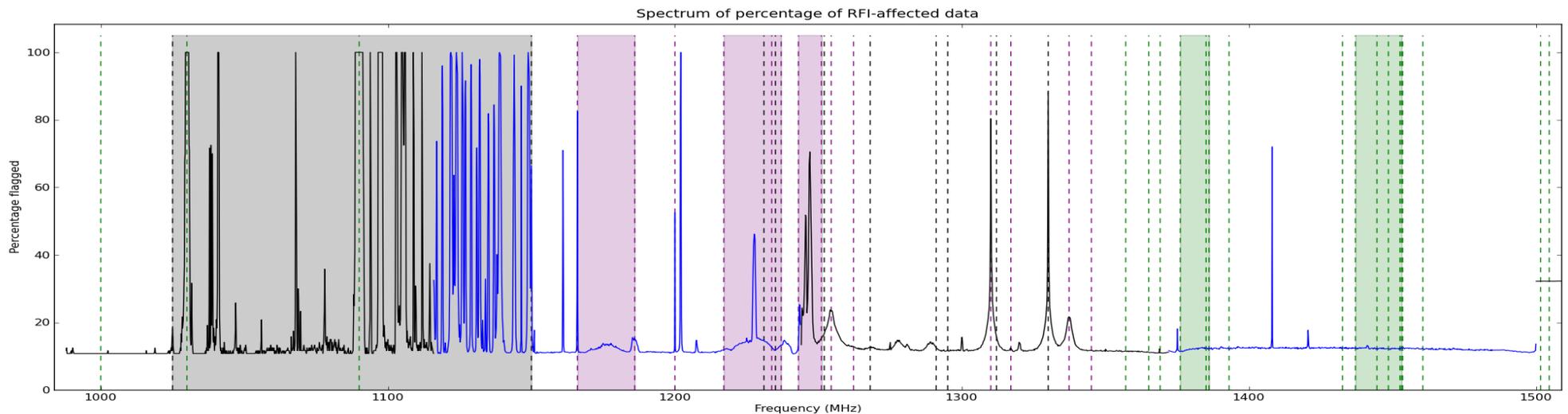
If this is done correctly, you could get increased imaging sensitivity (over wide fields), high-fidelity high dynamic-range reconstructions of both spatial and spectral structure, all from a single wide-band observation.

Image from Frazer Owen : Intensity-weighted Spectral Index of Abell 2256



# Radio Frequency Interference and Flagging

## Fraction of RFI-affected data vs Frequency



At L-Band, with the JVLA, you can use ~500 MHz with very rough flagging,  
~800 MHz if done carefully.

Flagging RFI-affected data : Manual flagging,  
Automatic flagging (several algorithms in use at  
( Loss of Data ) different observatories)

Subtracting RFI from data : Model the measurement-process of RFI.  
Fit this model from the data, and subtract it out.

( Recovery of RFI-affected data )

# Automatic RFI identification and flagging

**TFCrop** : Detect outliers on the 2D time-freq plane,  
(based on visibility amplitudes)

- Average visibility amplitudes along one dimension
- Fit a piece-wise polynomial to the base of RFI spikes
  - calculate 'sigma' of data - fit.
- Flag points deviating from the fit by  $> N$ -sigma
- Repeat along the second dimension.

Can operate on un-calibrated data + one pass through MS  
'testautoflag' in CASA 3.3. 'tflagdata, mode=tfcrop' in CASA 3.4

**RFLAG** : Detect outliers using a sliding-window  
statistics in time and frequency (real/imag)

- For each channel, calculate rms of real and imag parts of visibilities across a sliding time window.
- Calculate the mean-rms, and deviations of these rmss from the mean.
- Search for outliers  
(local rms  $> N \times$  (median-rms + median-deviation))

Needs calibrated data + two passes through data.  
"RFLAG" in AIPS. 'tflagdata, mode=rflag' in CASA 3.4

