

# Cross Correlators & New Correlators

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NRAO/Socorro

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Socorro, NM, June 8-15, 2010*



# What is a correlator?

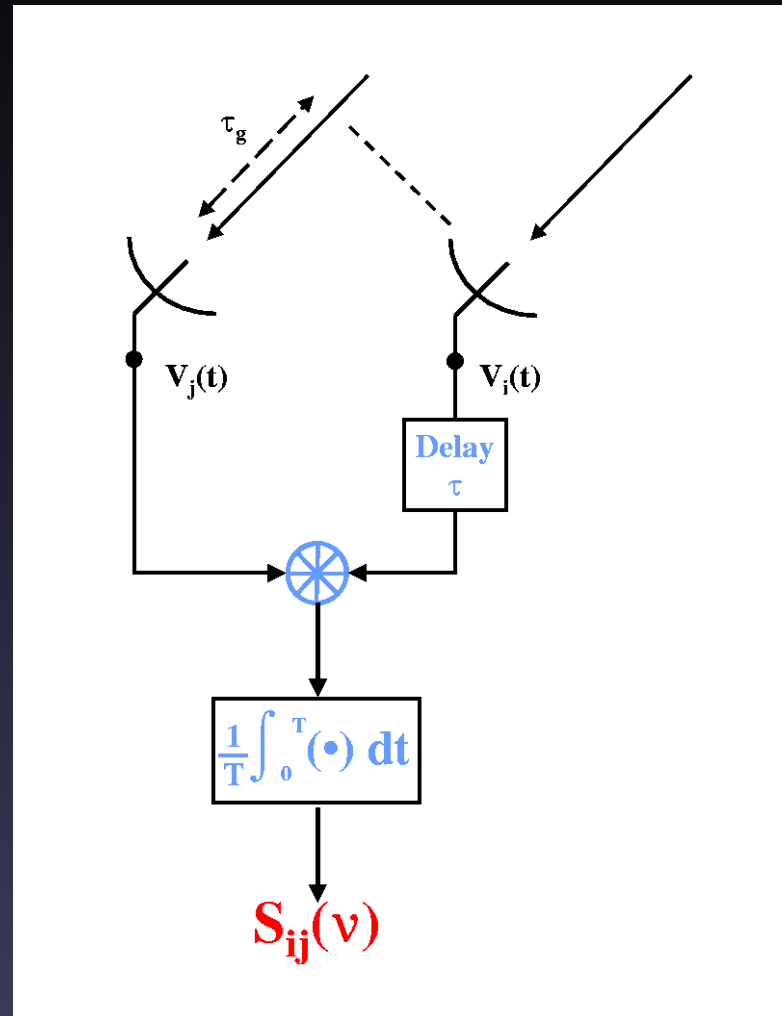
- In an optical telescope...
  - a **lens** or a mirror collects the light & brings it to a focus



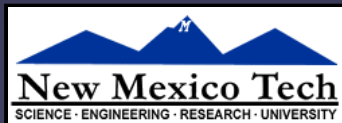
- a **spectrograph** separates the different frequencies



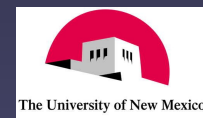
- In an interferometer, the **correlator** performs both these tasks, by correlating the signals from each telescope (antenna) pair: <sup>3</sup>



- The basic observables are the **complex visibilities:**  
**amplitude & phase**  
as functions of  
**baseline, time, and frequency.**
- The correlator takes in the signals from the individual telescopes, and writes out these visibilities.



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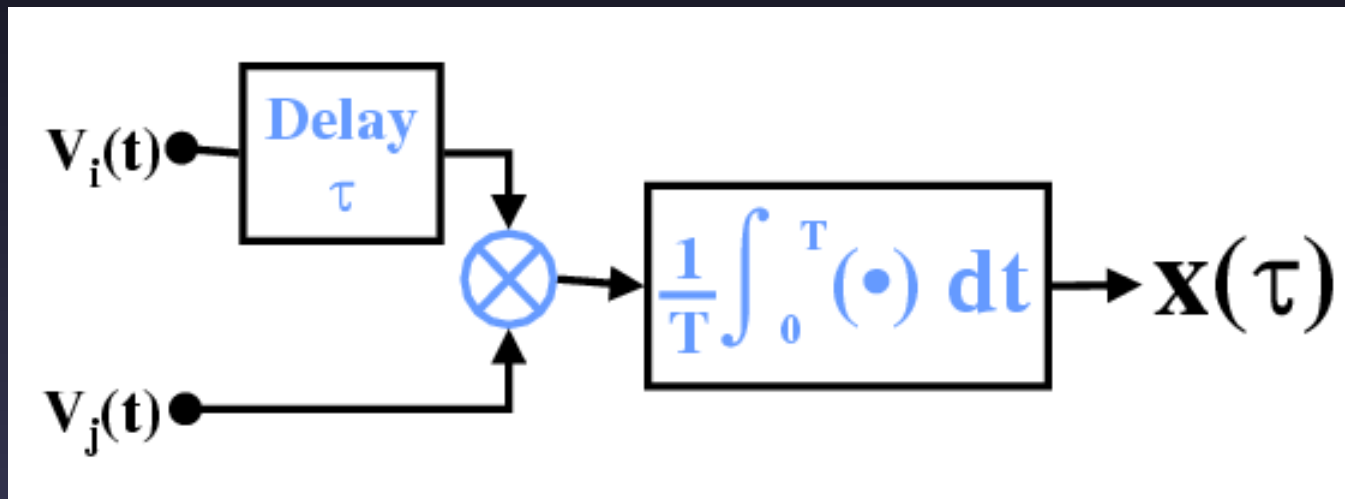




## Correlator Basics

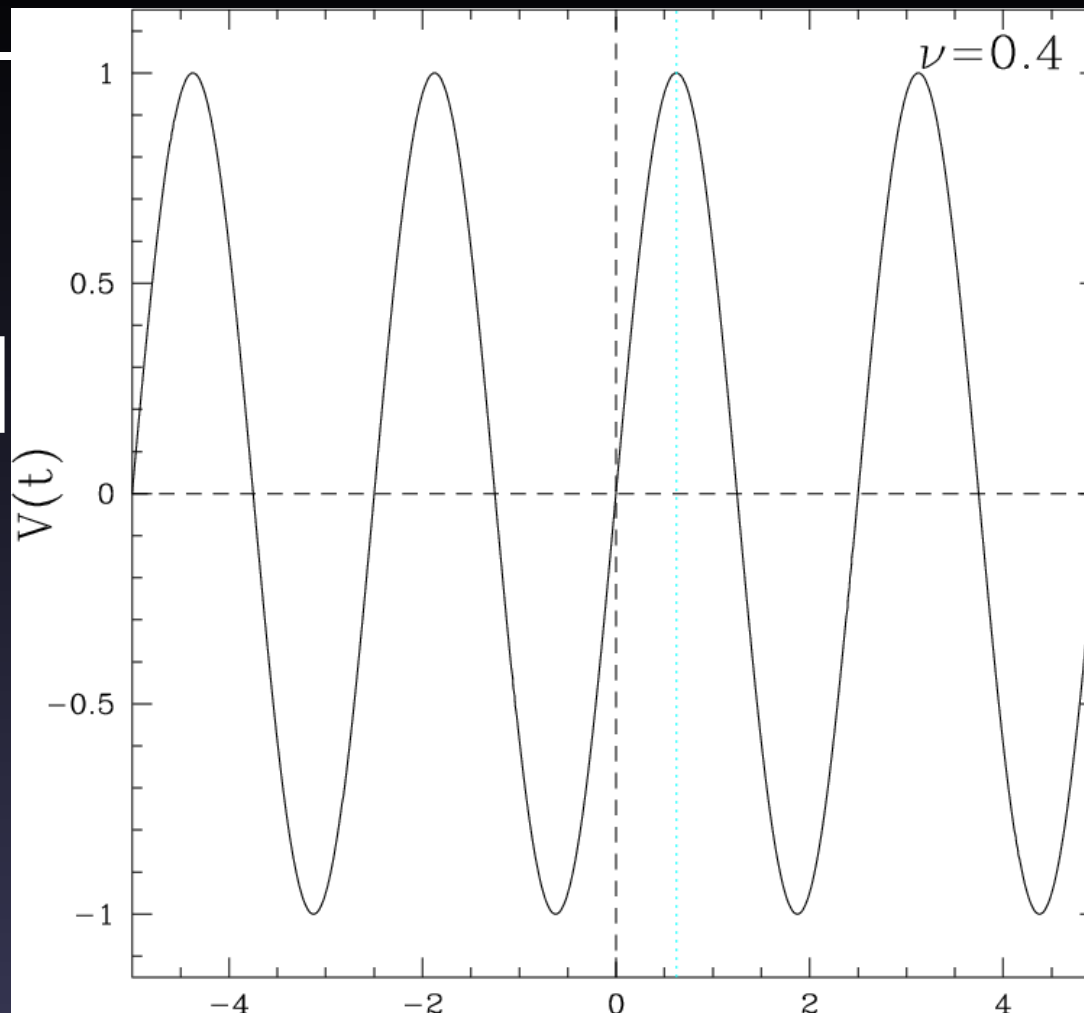
The cross-correlation of two real signals  $v_i(t)$  and  $v_j(t)$  is

$$x_{ij}(\tau) \equiv \langle v_i(t) v_j(t + \tau) \rangle$$

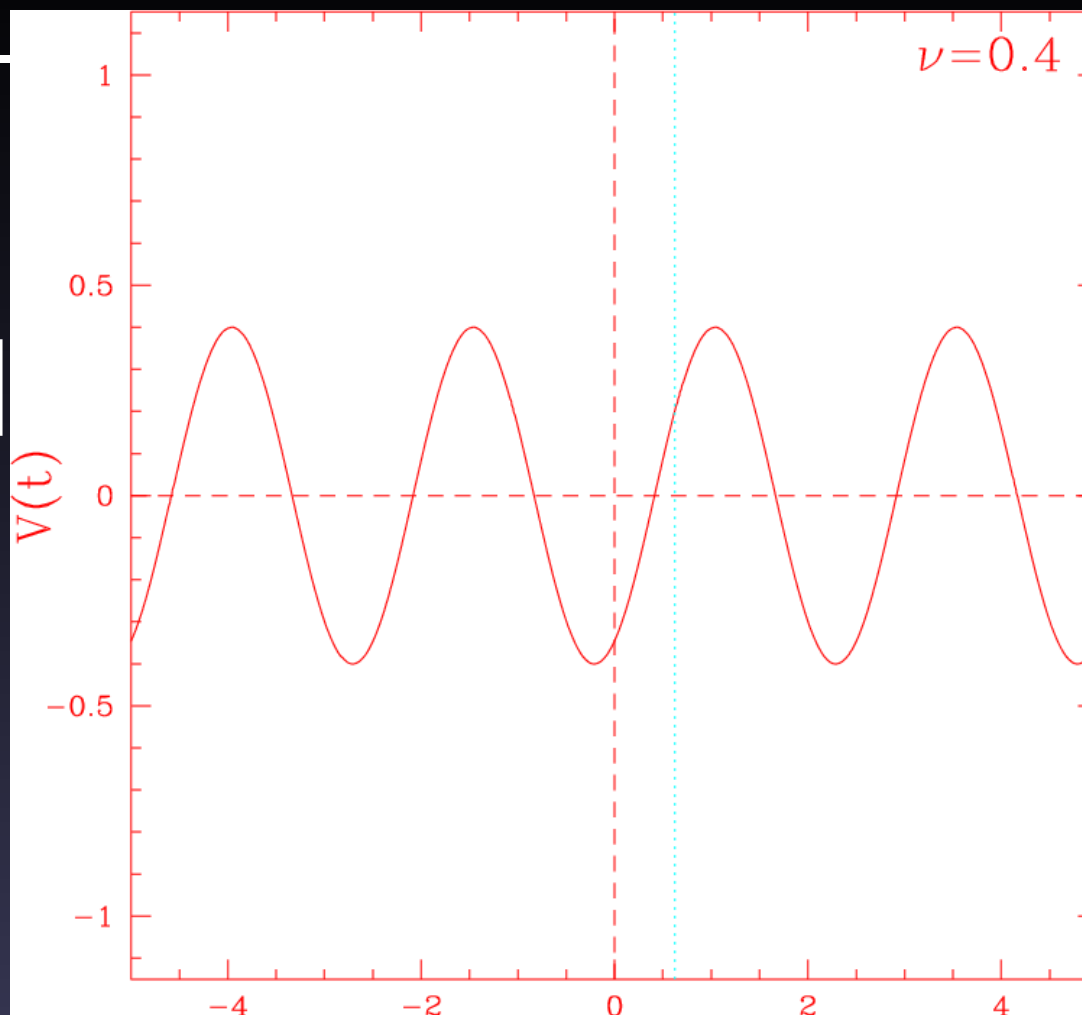


A simple (real) correlator.

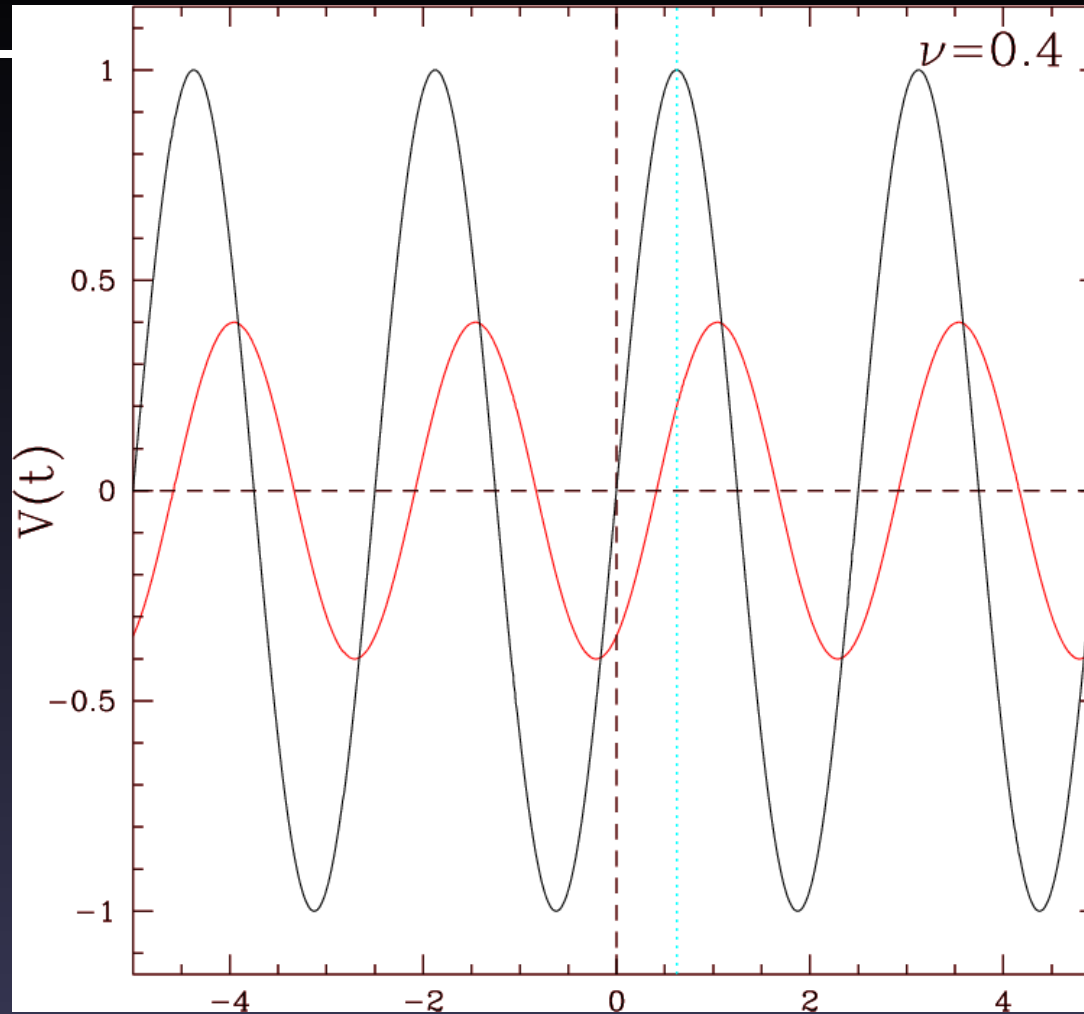
# Antenna 1:



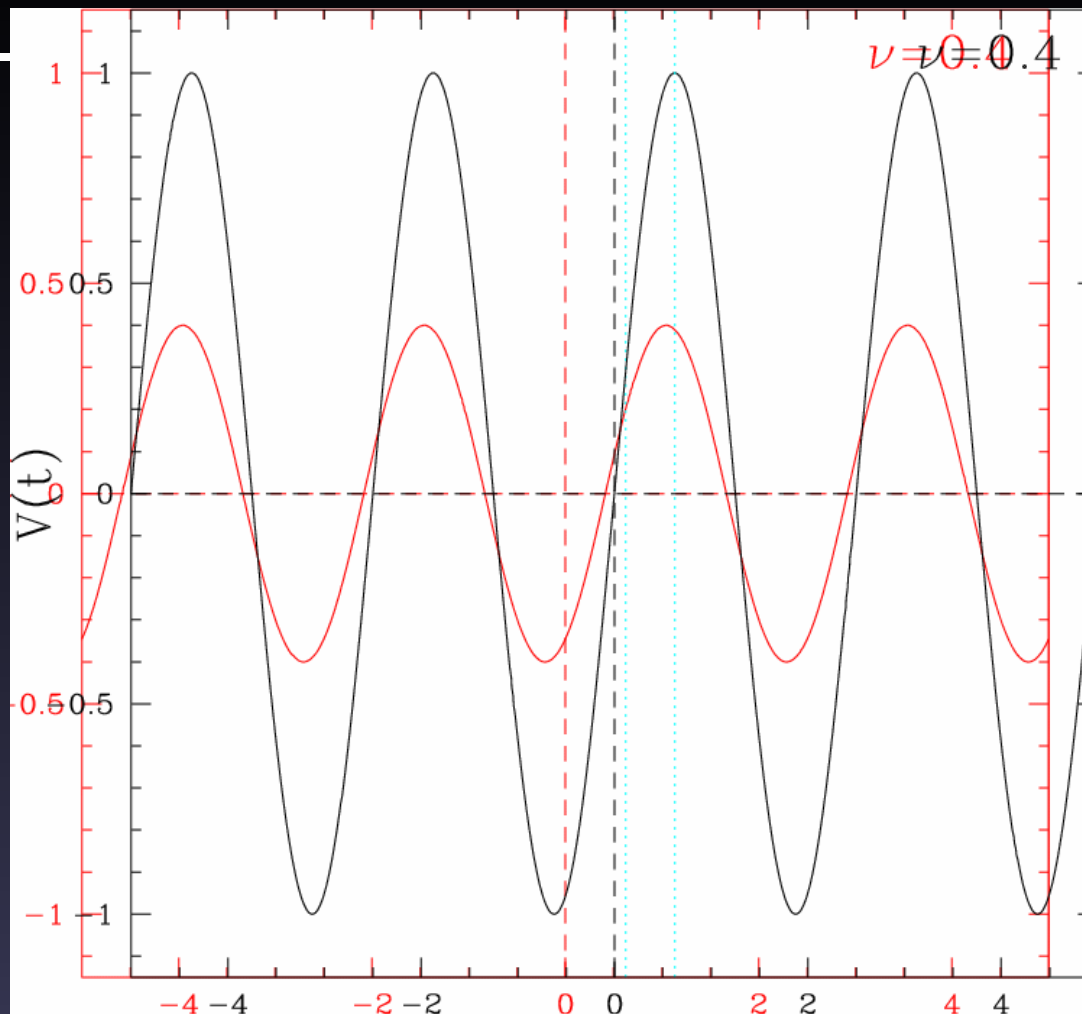
## Antenna 2:



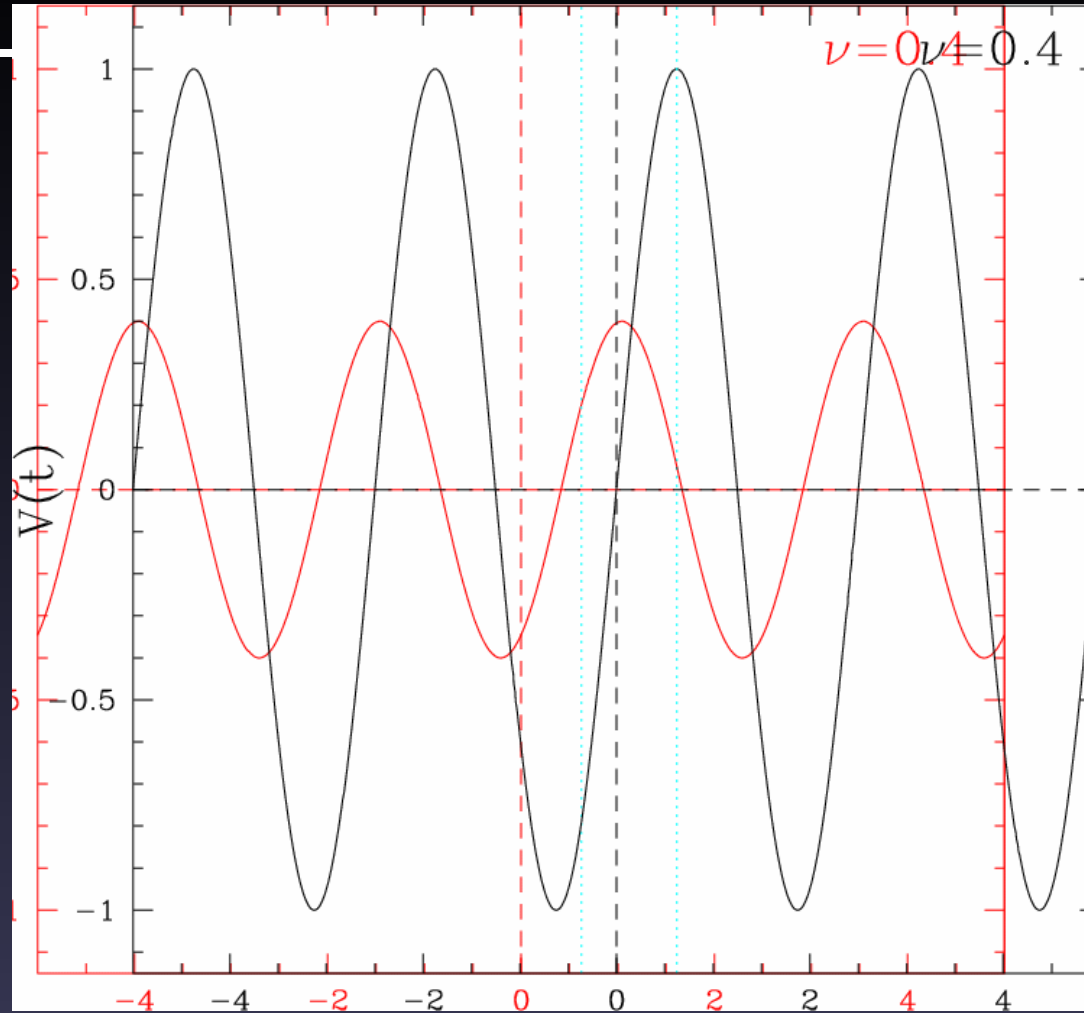
$\tau=0$ :



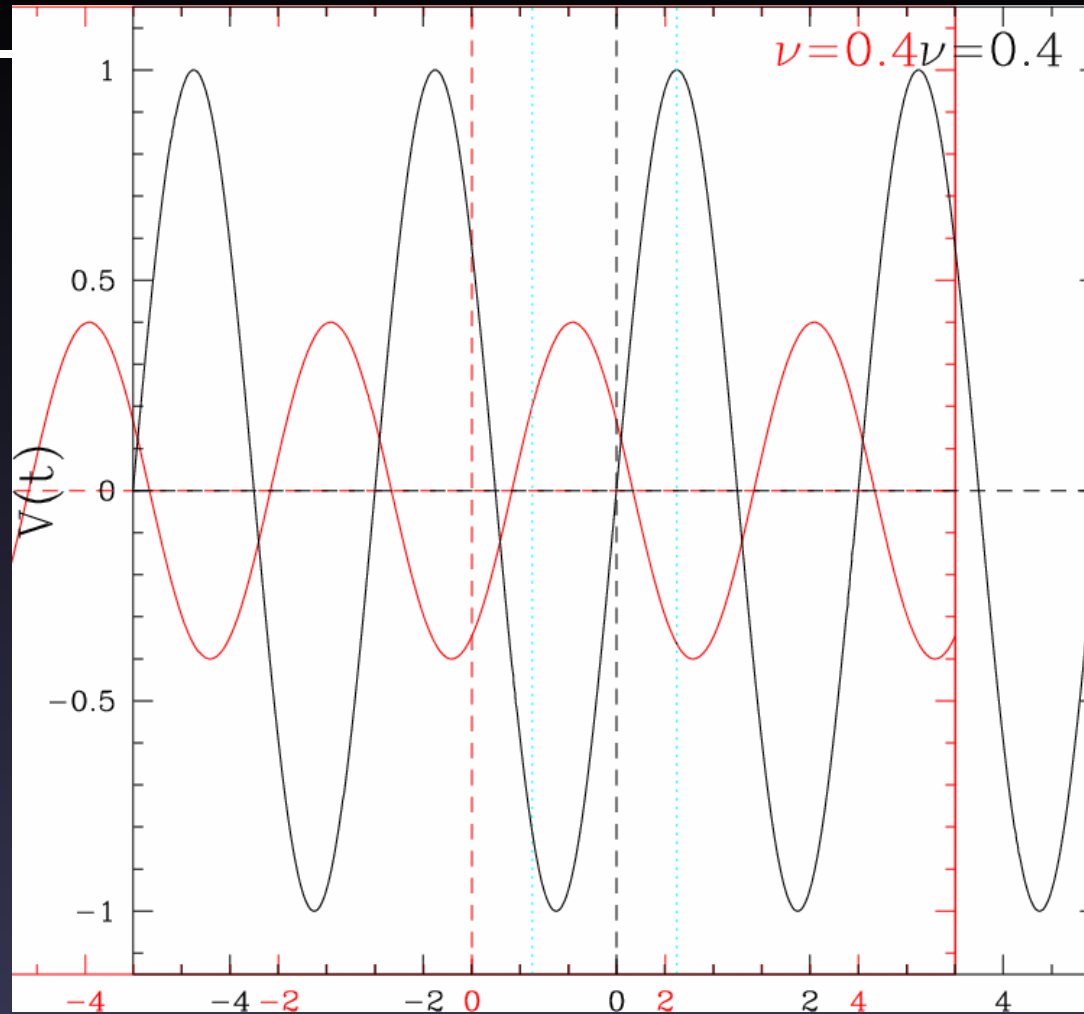
$\tau=0.5$ :



$\tau=1$ :

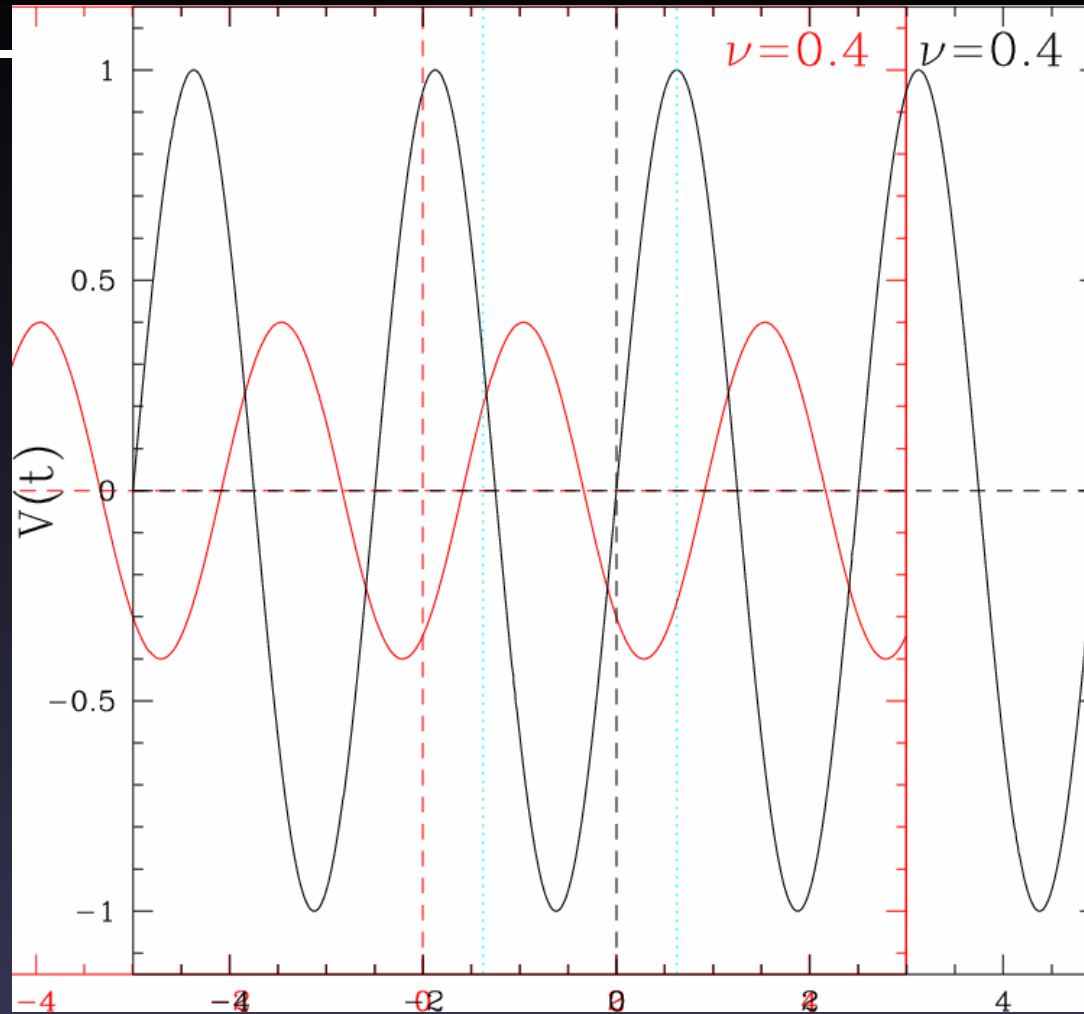


$\tau=1.5$ :

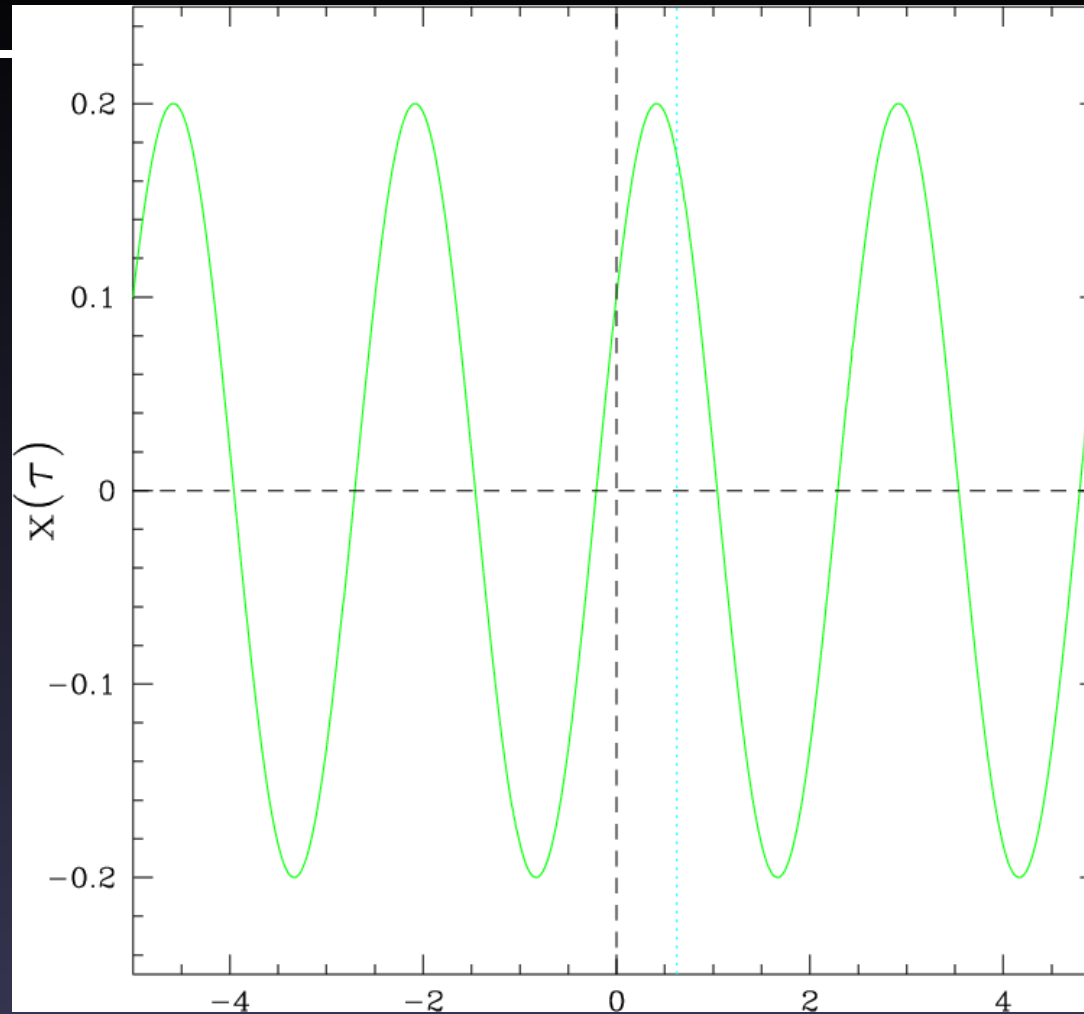




$\tau=2$ :



→ Correlation:



# Correlation of a Single Frequency

For a monochromatic signal:

$$\begin{aligned}v_i(t) &= \sin 2\pi\nu_0 t \\v_j(t) &= \sin (2\pi\nu_0 t + \phi)\end{aligned}$$

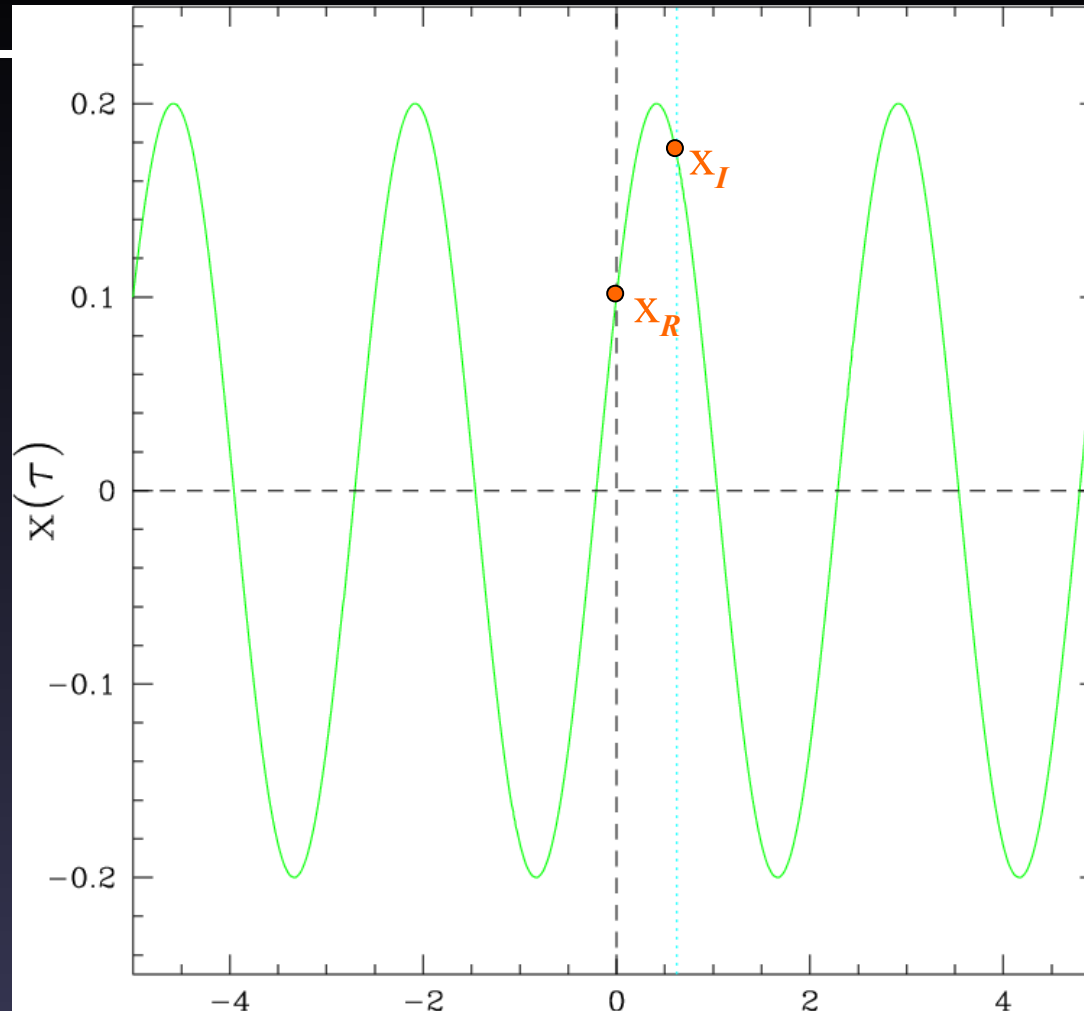
and the correlation function is

$$\begin{aligned}x_{ij}(\tau) &= \langle \sin 2\pi\nu_0 t \sin (2\pi\nu_0 (t + \tau) + \phi) \rangle \\&= x_R \cos 2\pi\nu_0 (\tau - \tau_0) + x_I \sin 2\pi\nu_0 (\tau - \tau_0)\end{aligned}$$

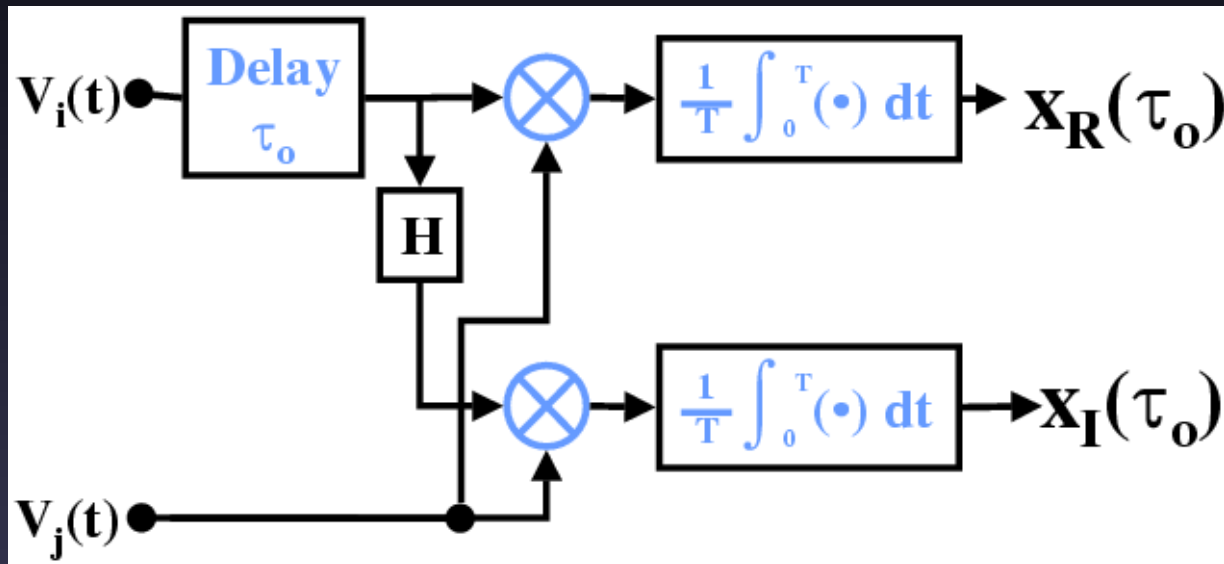
So we need only measure  $R_{ij} = x_R + ix_I$ , with

- $x_R = x_{ij}(\tau_0)$
- $x_I = x_{ij}(\tau_0 + \Delta\tau)$ , **with**  $\Delta\tau = 1/(4\nu_0)$  ( $\Delta\phi = 90^\circ$ ).

→ Correlation:



At a given frequency, all we can know about the signal is contained in two numbers: **the real and the imaginary part**, or **the amplitude and the phase**.



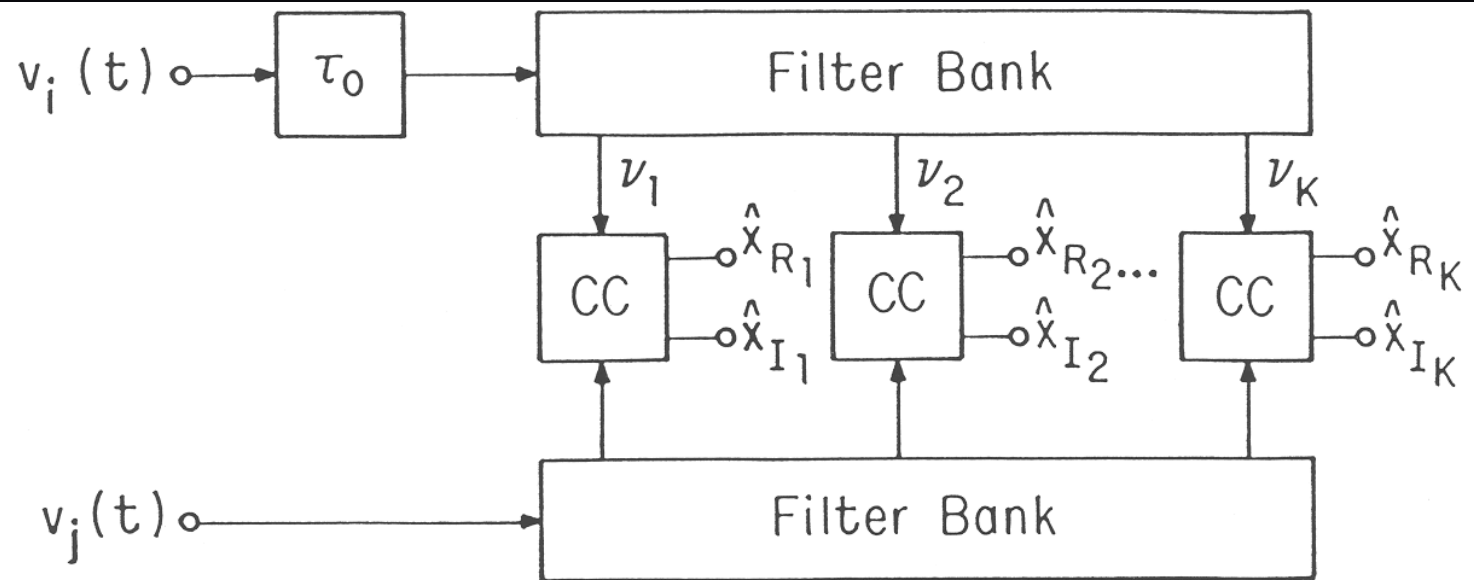
A complex correlator.

## 1. The simple approach:

- use a filterbank to split the signal up into quasi-monochromatic signals at frequencies  $\nu_k$
- hook each of these up to a different complex correlator, with the appropriate (**different**) delay:  $\Delta\tau_k = 1/(4\nu_k)$
- add up all the outputs

## 1. The clever approach:

instead of sticking in a delay, put in a filter that shifts the phase for *all* frequencies by  $\pi/2$



$$\hat{R}_{ij}(\tau_0) = \sum_{k=1}^K \hat{x}_{R_k} + i \hat{x}_{I_k}$$

**Figure 4-4.** A wide-band complex correlator synthesized from narrow-band complex correlators, or a spectroscopic correlator. Each box labeled “CC” is as indicated in Figure 4-3.



## 1. The simple approach:

- use a filterbank to split the signal up into quasi-monochromatic signals at frequencies  $\nu_k$
- hook each of these up to a different complex correlator, with the appropriate (**different**) delay:  $\Delta\tau_k = 1 / (4\nu_k)$
- record all the outputs:  $R_{ij}(\nu, t)$

# Fourier Transforms: a motivational exercise

**Short lags** (small delays)



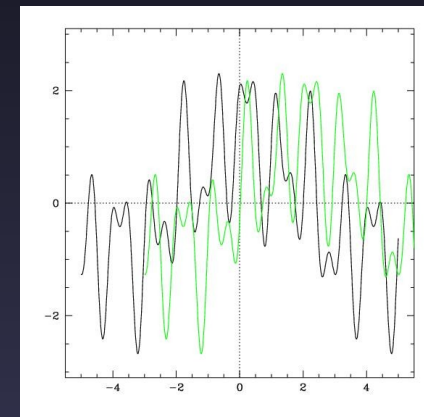
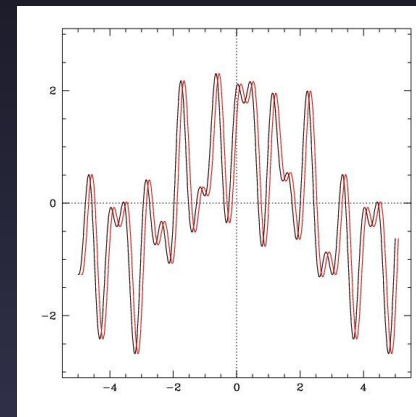
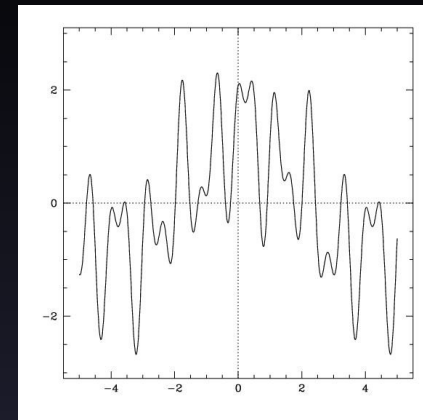
high frequencies

**Long lags** (large delays)



low frequencies

⇒ Measuring a range of lags corresponds to measuring a range of frequencies



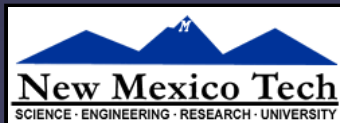
The **frequency spectrum** is the **Fourier transform** of the **cross-correlation (lag) function**.

## 2. Clever approach #1: the FX correlator

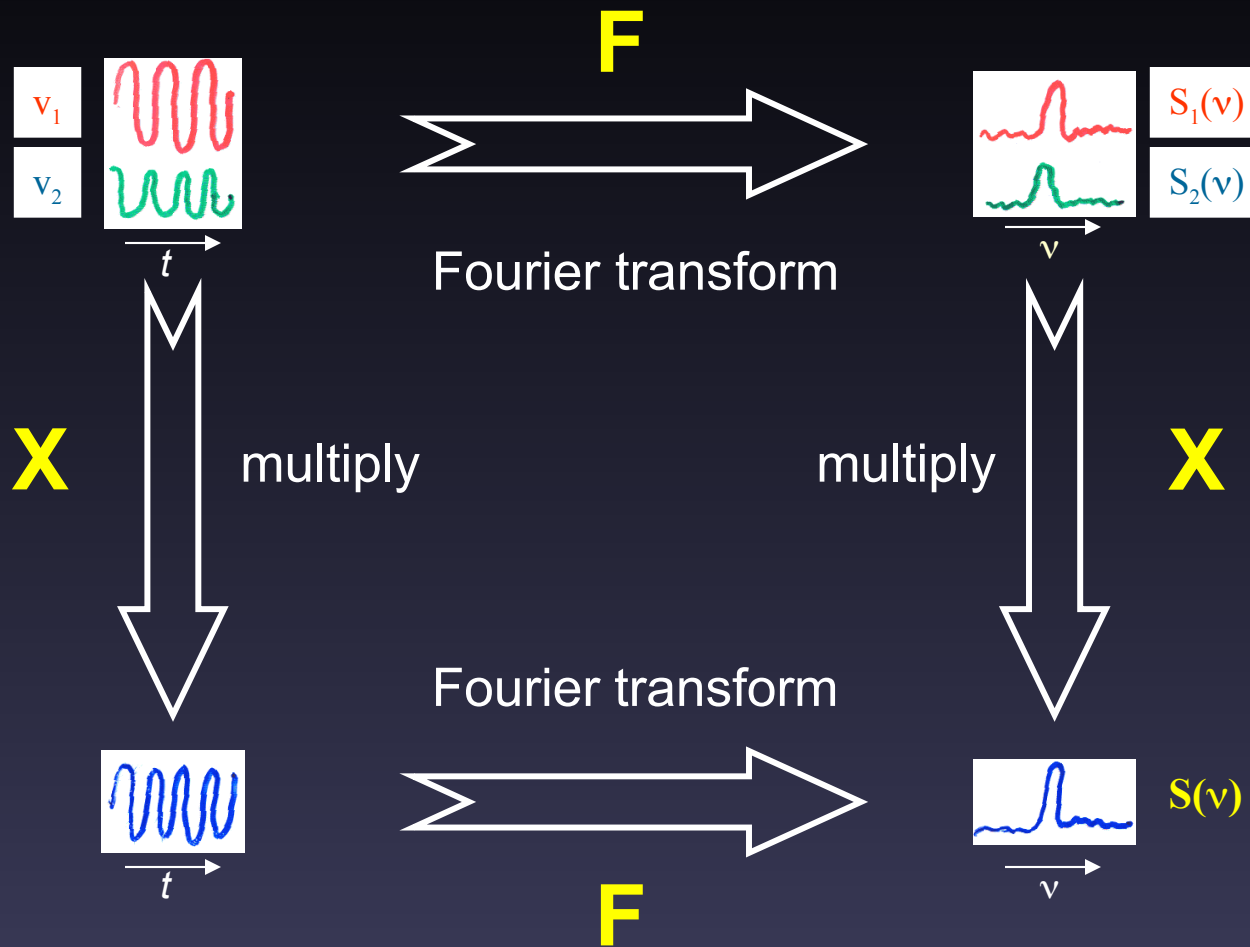
- **F**: replace the filterbank with a Fourier transform
- **X**: use the simple (complex) correlator above to measure the cross-correlation at each frequency
- average over time
- record the results
- Examples: NRO, VLBA, DiFX, ACA

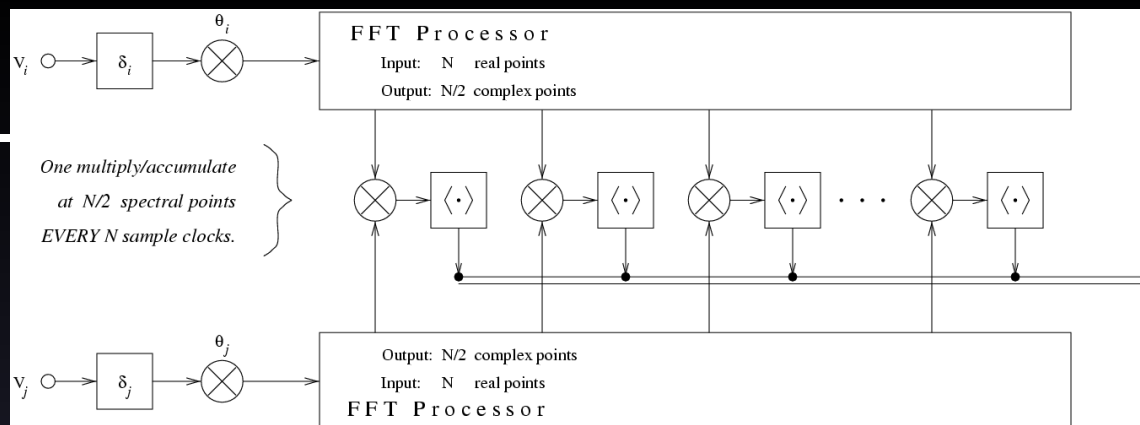
## 3. Clever approach #2: the XF (lag) correlator

- **X**: measure the correlation function at a bunch of different lags (delays)
- average over time
- **F**: Fourier transform the resulting time (lag) series to obtain spectra
- record the results
- Examples: VLA, IRAM; preferred for >20 antennas

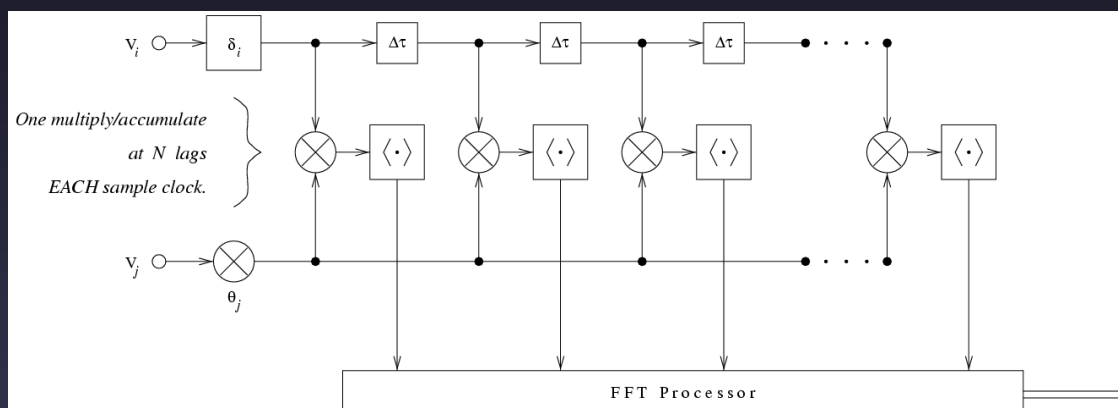


# FX vs. XF





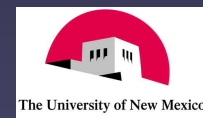
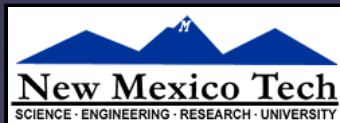
**Fig. 4-6: FX correlator baseline processing.**



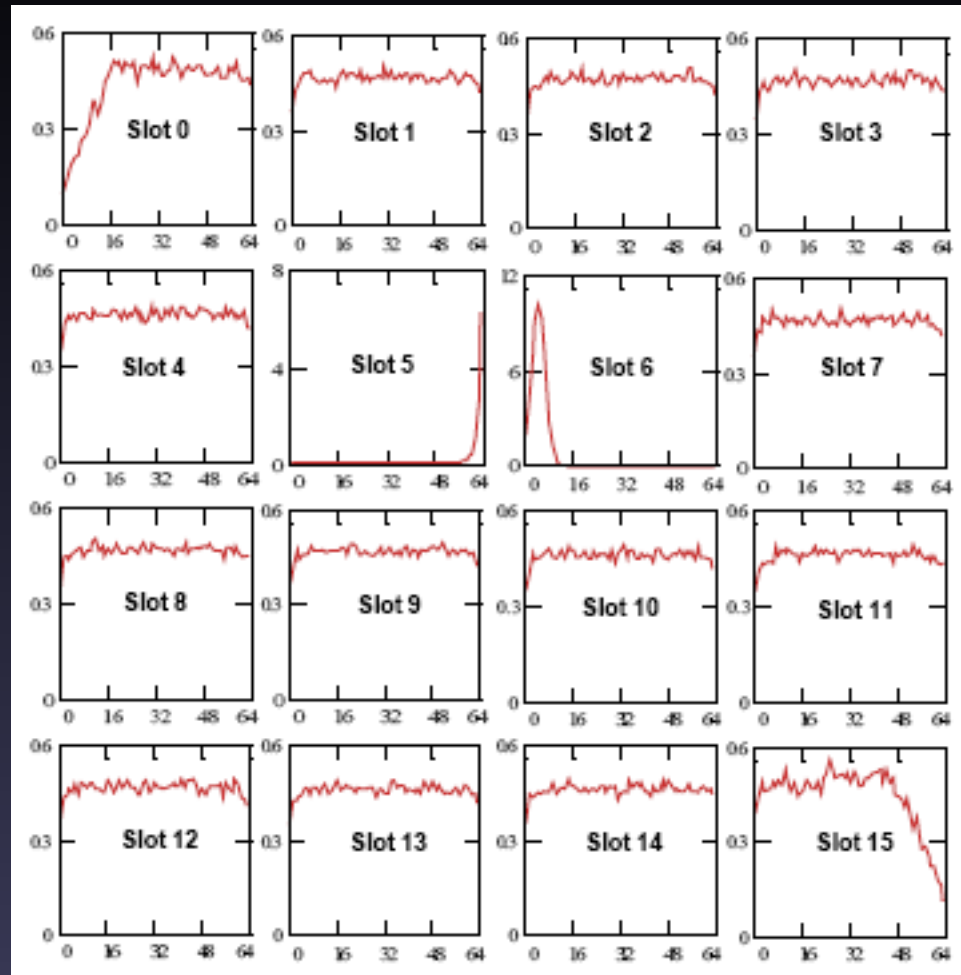
**Fig. 4-1: Lag (XF) correlator baseline processing.**

## 4. Clever approach #3: the FXF (hybrid) correlator

- **F**: bring back the filter bank! (but *digital*: polyphase FIR filters, implemented in field programmable gate arrays)
  - splits a big problem into lots of small problems (**sub-bands**)
  - digital filters allow recovery of full bandwidth ("**baseband**") through **sub-band stitching**
- **X**: measure the correlation function at a bunch of different lags (delays)
- average over time
- **F**: Fourier transform the resulting time (lag) series to obtain spectra
- stitch together sub-bands
- record the results
- Examples: EVLA/eMERLIN (WIDAR), ALMA (TFB+ALMA-B); preferred for large bandwidths



# FXF Output

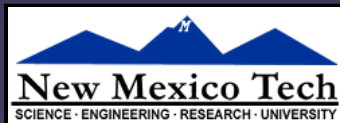


16 sub-bands



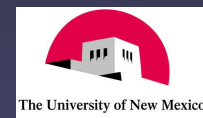
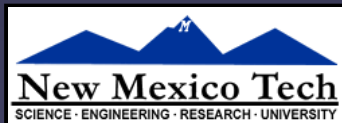
# Implementation & choice of architecture

- Correlators are **huge**
  - Size roughly goes as  $N_{ij} BW N_{den} = N_{at}^2 BW N_{den}$
  - $N_{at}$  driven up by...
    - sensitivity (collecting area)
    - cost (small is cheap)
    - imaging (more visibilities)
    - field-of-view (smaller dishes ==> larger potential FoV)
  - $BW$  driven up by...
    - continuum sensitivity
  - $N_{den}$  driven up by...
    - spectral lines (spectral resolution, searches, surveys)
    - Radio frequency interference (RFI) from large BW
    - field-of-view (fringe washing = beam smearing = chromatic aberration)

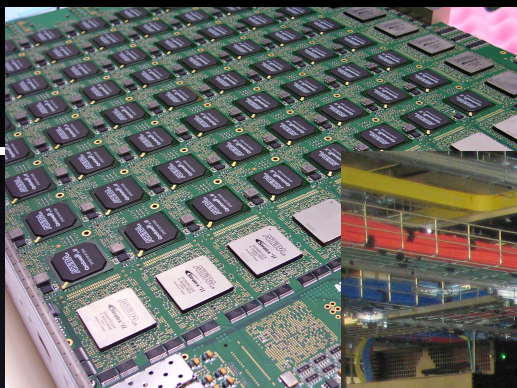
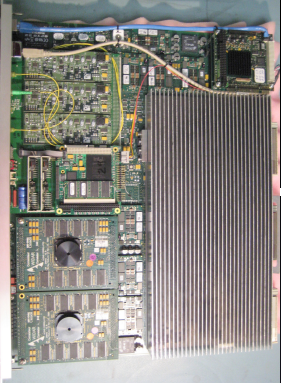


# Implementation & choice of architecture

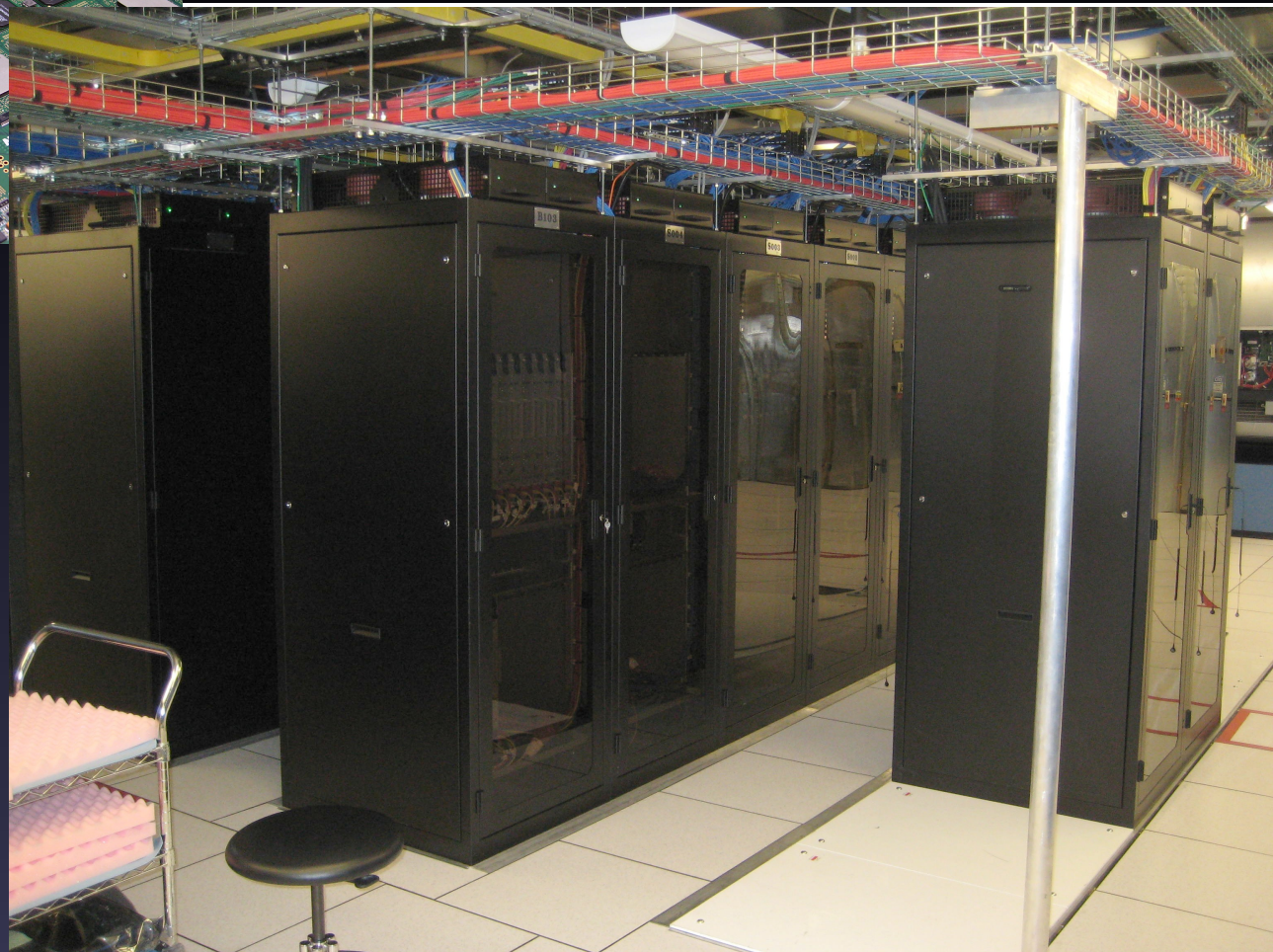
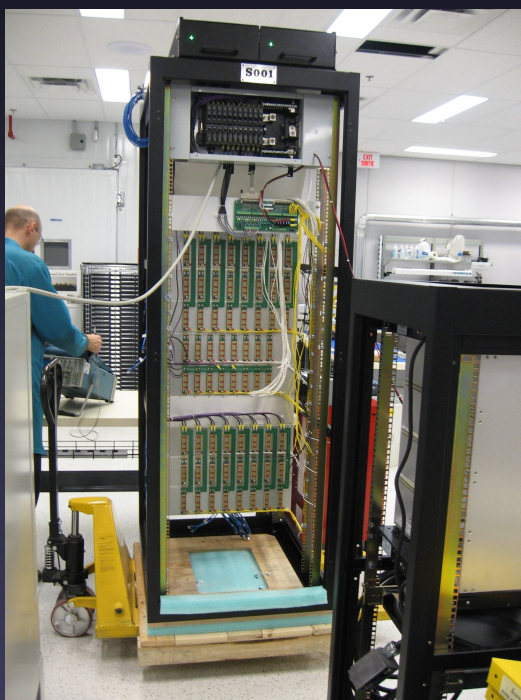
- Example: EVLA's WIDAR correlator (Brent Carlson & Peter Dewdney, DRAO)
  - $2 \times 4 \times 2 = 16$  GHz, 32 antennas
  - 128 sub-band pairs
  - Spectral resolution down to below a Hz
  - Up to 4 million spectral channels per baseline
  - Input: **3.8 Tbit/sec** ~ 160 DVDs/sec (120 million people in continuous phone conversation)
  - **40e15 operations per second (petaflops)**
  - Output (max): **30 Gbytes/sec** ~ 7.5 DVDs/sec
- N.B. SKA: ~100x larger: **4000 petaflops!** (xNTD approach)



# EVLA WIDAR

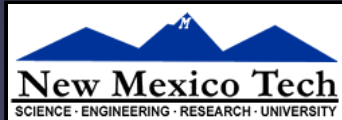


2 of 256  
Boards...



1 of 16  
racks...

plus LOTS of cables!



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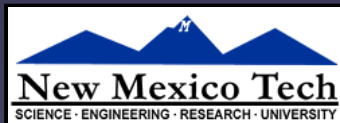
# ALMA



1 of 4 quadrants

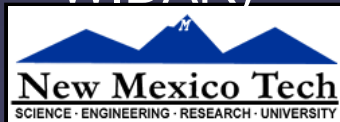
# Implementation & choice of architecture

- Huge & expensive ==> relies on cutting-edge technology, with trade-offs which change frequently (cf. Romney 1999)
  - Silicon vs. copper
  - Capability vs. power usage
- **Example: fundamental hardware**: speed & power usage vs. flexibility and “non-recoverable engineering” expense (**NRE**)
  - **A**pplication **S**pecific **I**ntegrated **C**ircuit (**ASIC**) (e.g., GBT, VLA, EVLA, ALMA)
  - **F**ield **P**rogrammable **G**ate **A**rray (**FPGA**) (e.g., VLBA, EVLA, ALMA)
  - Graphics cards
  - ROACH boards (Casper: “lego” correlator)
  - Software (PCs; supercomputers) (e.g., DiFX, LOFAR)

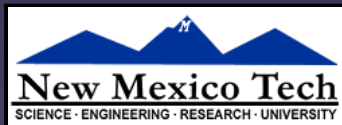


# Implementation & choice of architecture

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- **Example: fundamental hardware**: speed & power usage vs. flexibility and “non-recoverable engineering” expense (**NRE**)
  - Application Specific Integrated Circuit (**ASIC**) (e.g., GBT, VLA, EVLA, ALMA)
  - Field Programmable Gate Array (**FPGA**) (e.g., VLBA, EVLA, ALMA)
  - Graphics cards
  - Software (PCs; supercomputers) (e.g., DiFX, LOFAR)
- So big and so painful they tend to be used forever (exceptions: small arrays, VLA, maybe ALMA)
- Trade-offs are so specific they are never re-used (exception: WIDAR)



- Why digital?
  - precise & repeatable
  - “embarrassingly parallel” operations
  - piggy-back on industry (Moore’s law et al.)
- ...but there are some complications as well...



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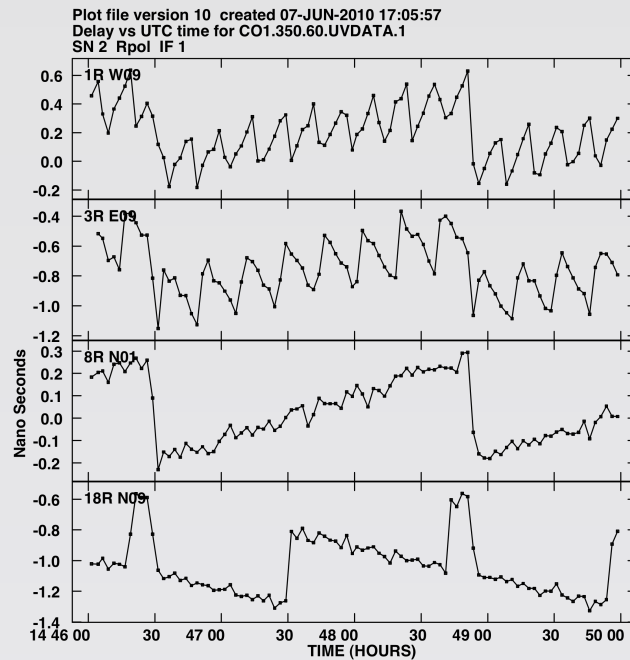
## 1. Sampling: $v(t) \Rightarrow v(t_k)$ , with $t_k = (0, 1, 2, \dots) \Delta t$

- For signal  $v(t)$  limited to  $0 < v \leq \Delta v$ , this is lossless if done at the **Nyquist rate**:

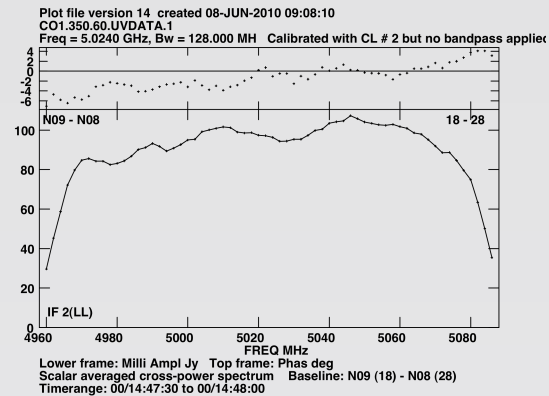
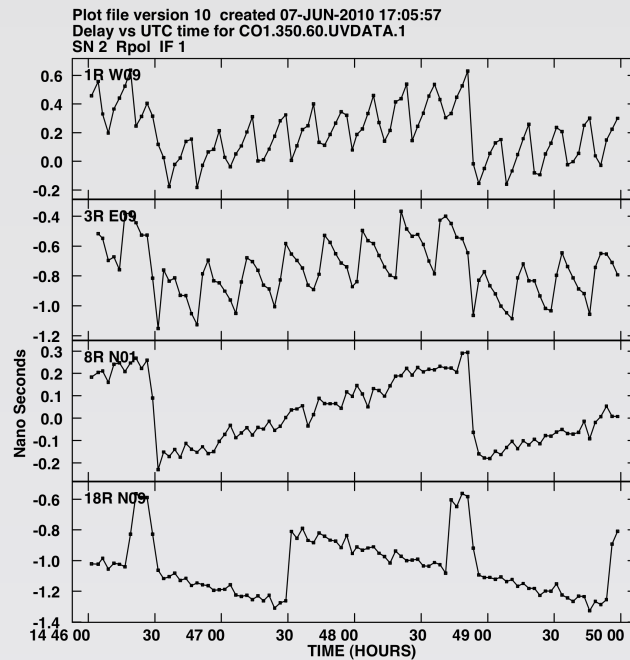
$$\Delta t \leq 1/(2\Delta v)$$

- *n.b.* wider bandwidth  $\Rightarrow$  finer time samples!
- limits accuracy of delays/lags

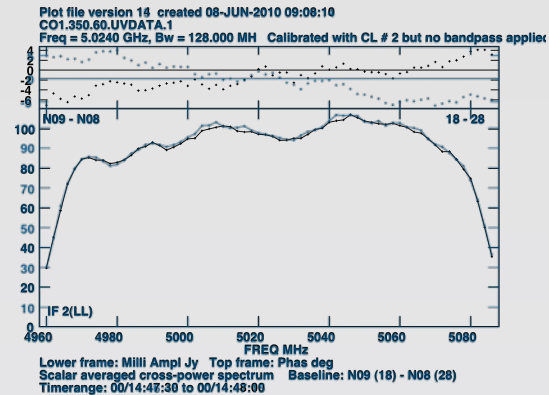
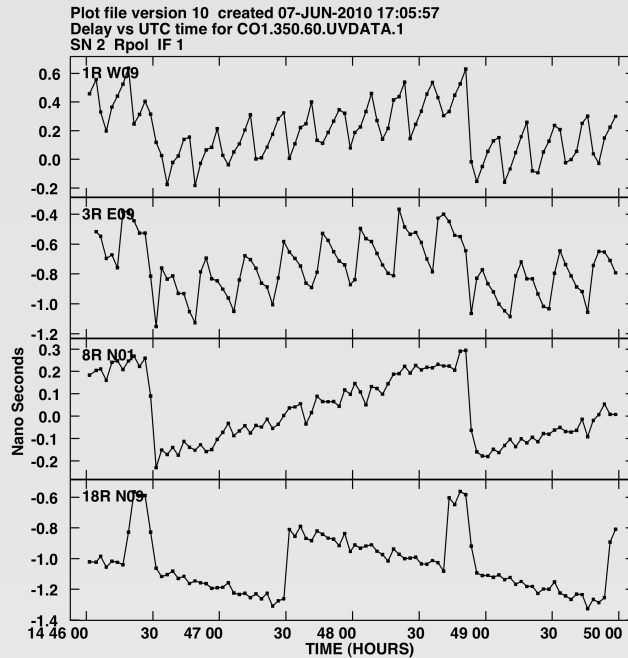
# Example: subsample delay errors



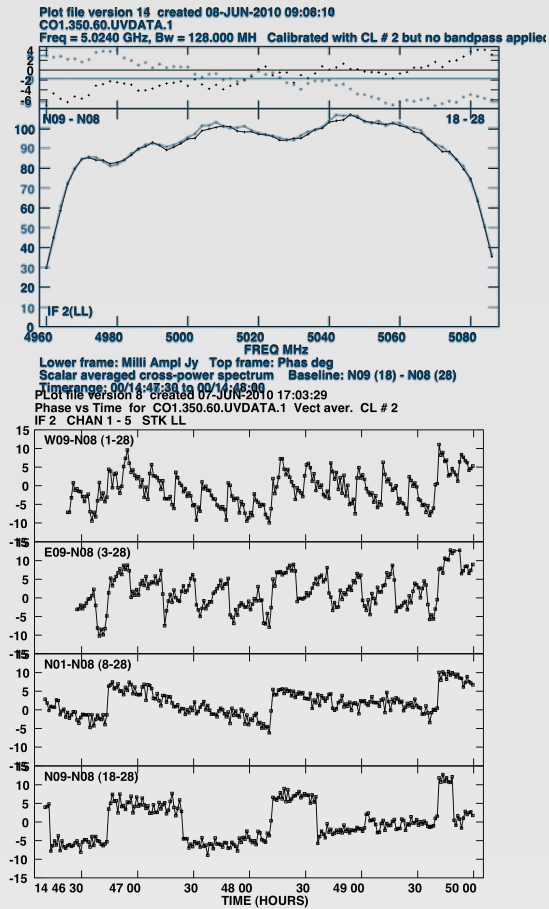
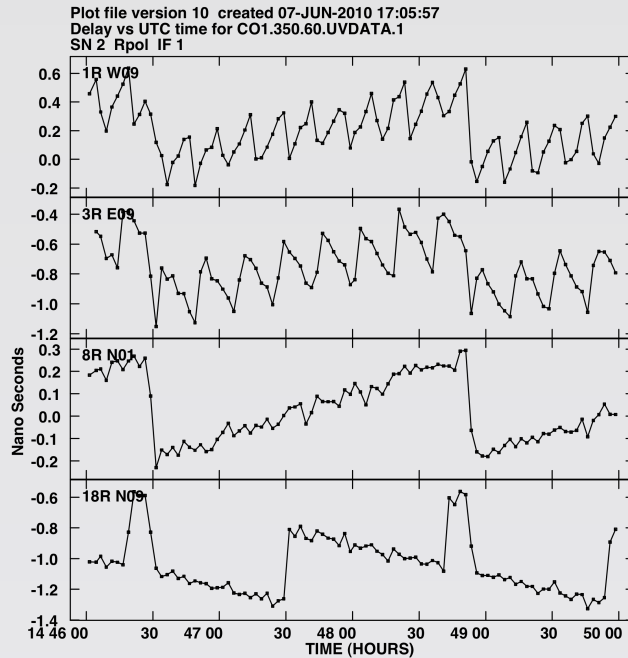
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# Example: subsample delay errors



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$$\Delta t \leq 1/(2\Delta v)$$

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- limits accuracy of delays/lags

## 1. Quantization: $v(t) \Rightarrow v(t) + \delta$

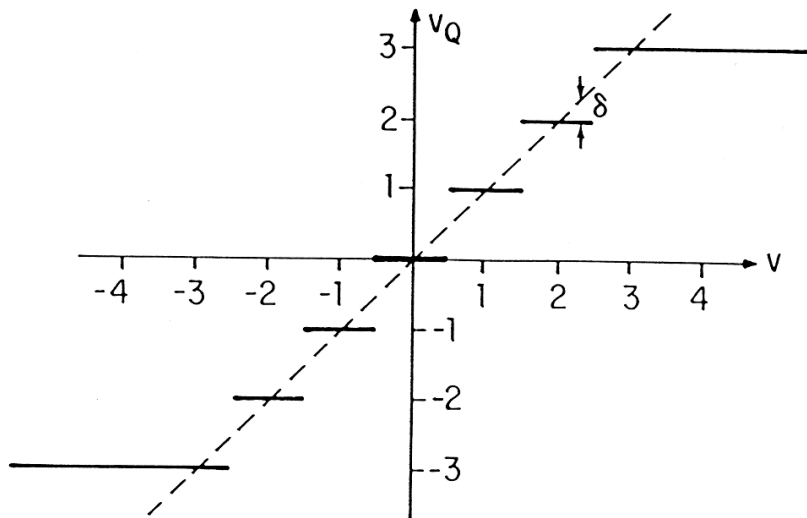
- quantization noise
  - quantized signal is *not* band-limited  $\Rightarrow$  oversampling helps
- N.B. FFX correlators quantize *twice*, ruling out most analytic work...

# Quantization & Quantization Losses

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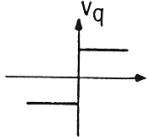
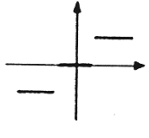
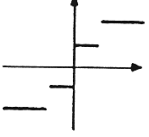
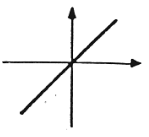
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**Figure 4-6.** An example of a quantizer transfer function (solid lines); this quantizer has seven levels. The dashed line is the line defined by  $v_q = v$ , and the difference between it and the transfer function is the quantization noise,  $\delta$ .

Table 4-1.  
Signal-to-Noise Ratio vs. Quantization and Sampling Rate

Quantization	Sampling Rate	$\frac{S/N(\text{digital})}{S/N(\text{continuous})}$
 2-level (1 bit)	$2\Delta\nu$	.64
	$4\Delta\nu$	.74
 3-level	$2\Delta\nu$	.81*
	$4\Delta\nu$	.89
 4-level	$2\Delta\nu$	.88
	$4\Delta\nu$	.94
 $\infty$ -level (continuous)	$2\Delta\nu$	1.00
	$4\Delta\nu$	1.00

\*VLA Case.

All cases assume rectangular bandpasses of width  $\Delta\nu$ , signal levels adjusted to maximize the signal-to-noise ratio, and small correlation coefficients.

# Cross-Correlating a Digital Signal

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- We measure the cross-correlation of the digitized (rather than the original) signals.
- digitized CC is monotonic function of original CC
- 1-bit (2-level) quantization:

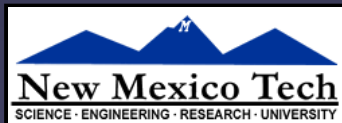
$$x_{ij}(\tau) = \sigma_i \sigma_j \sin \frac{\pi \rho_{ij}(\tau)}{2}$$

- $\sigma_i$  is average signal power level – *NOT* kept for 2-level quantization!

– roughly linear for correlation coefficient

$$x_{ij}(\tau) \ll 1$$

- For high correlation coefficients, requires non-linear correction: the **Van Vleck correction**



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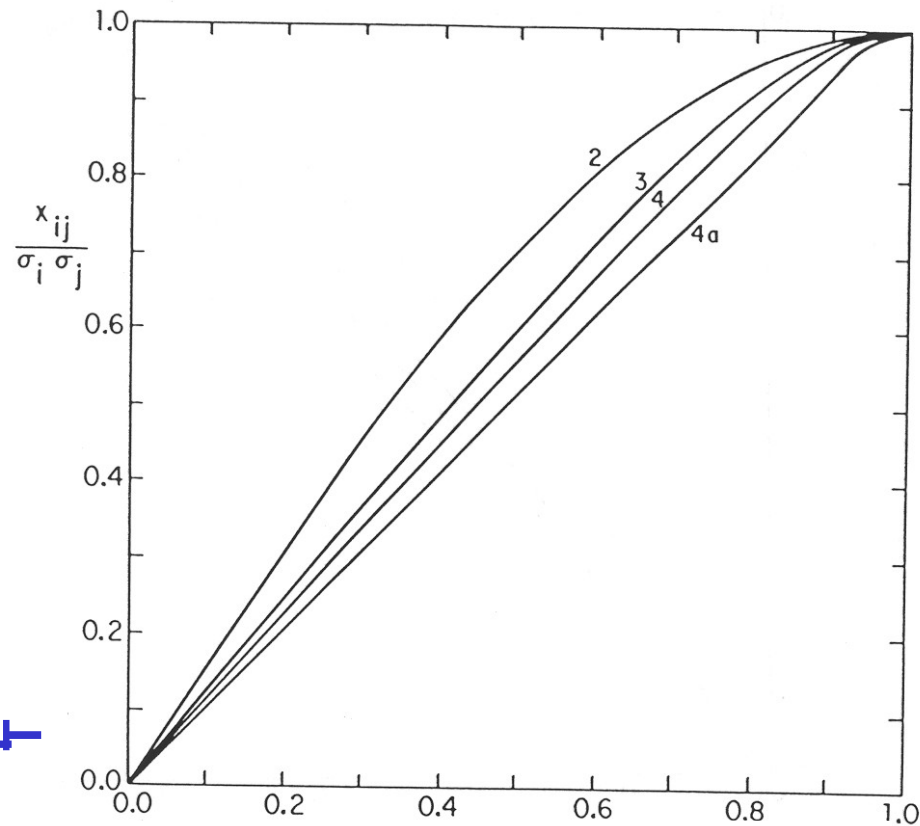


# Van Vleck Correction

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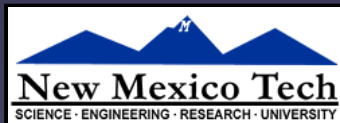


## Digital correlation coefficient

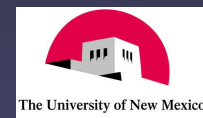
Figure 4-7. Quantization correction functions for various quantizations. In each case the signal powers are set for maximum signal-to-noise ratio. The curves are labeled according to the number of quantization levels; 4a uses a simplified multiplier (see Cooper, 1970).

# Correlation Coefficient & Tsys

- Correlation coefficients are **unitless**
  - 1.0 ==> signals are identical
- More noise means lower corr'n coeff, even if signal is identical at two antennas
- Must scale corr'n coeff by noise level (**Tsys**) as first step in calibration

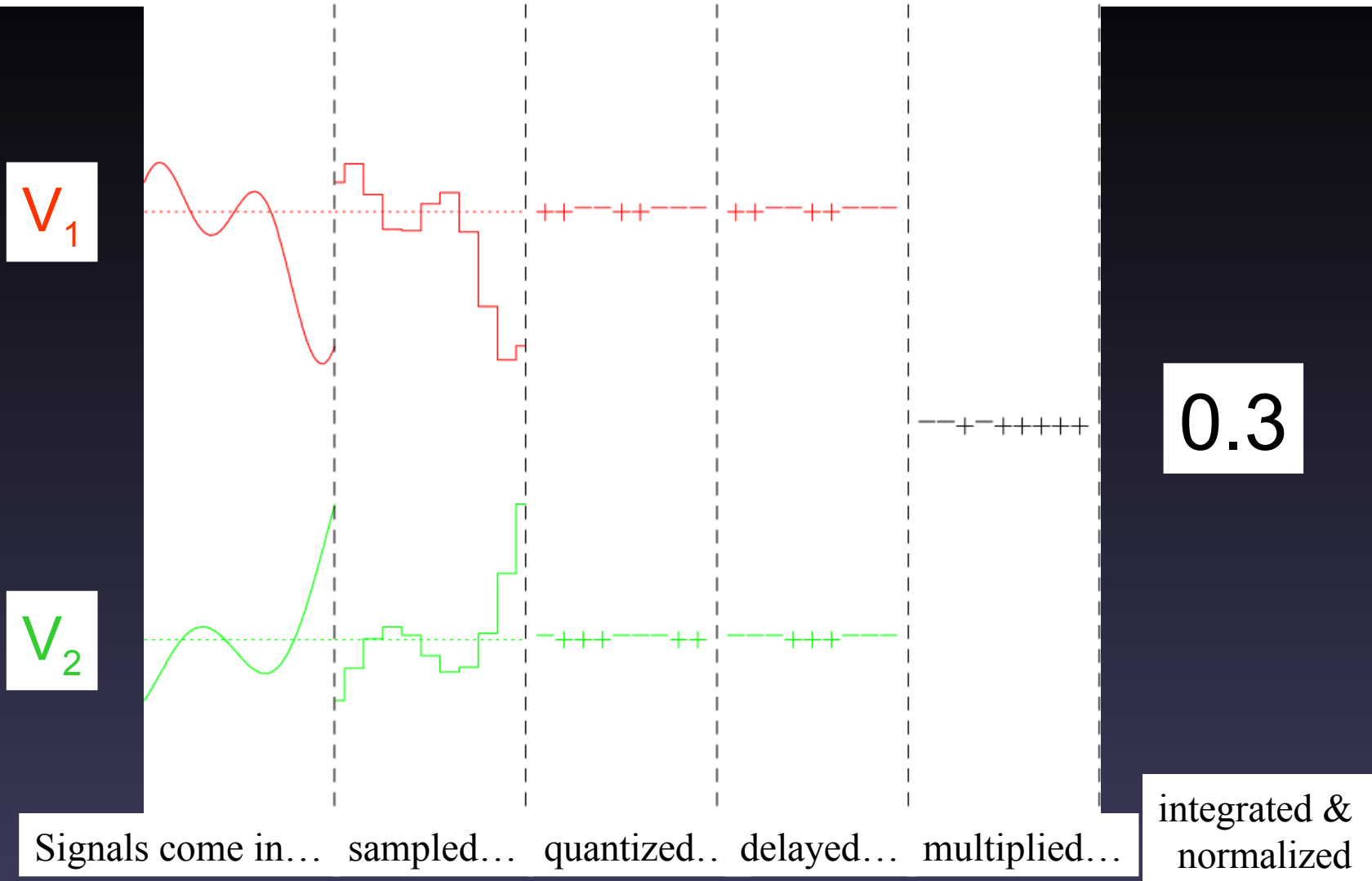


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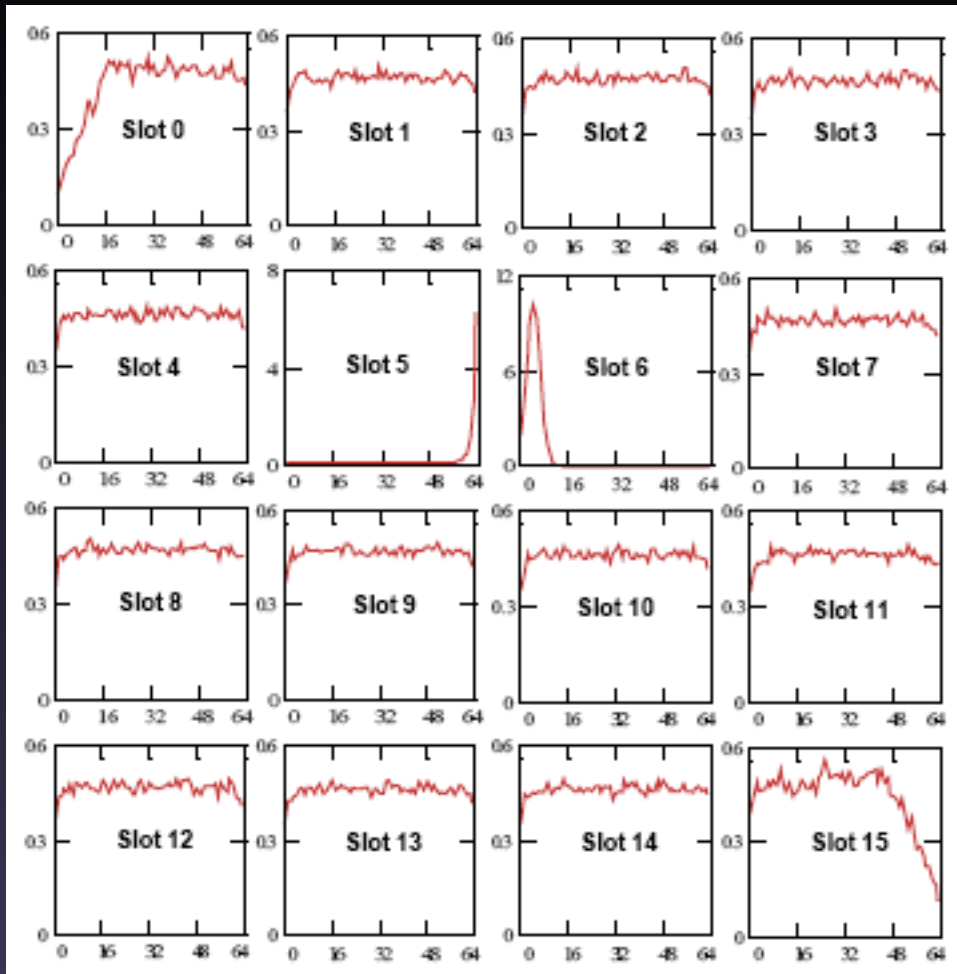


# Michael's Miniature Correlator

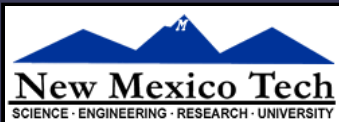
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# FXF Output: sub-band alignment & aliasing



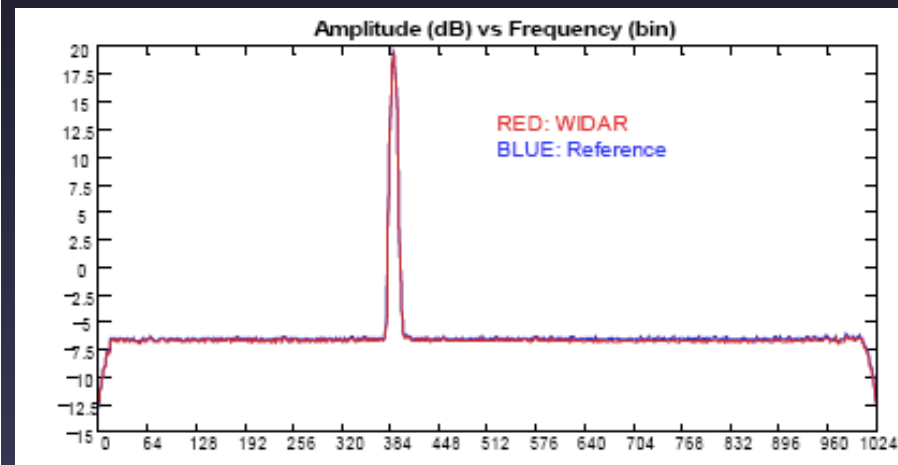
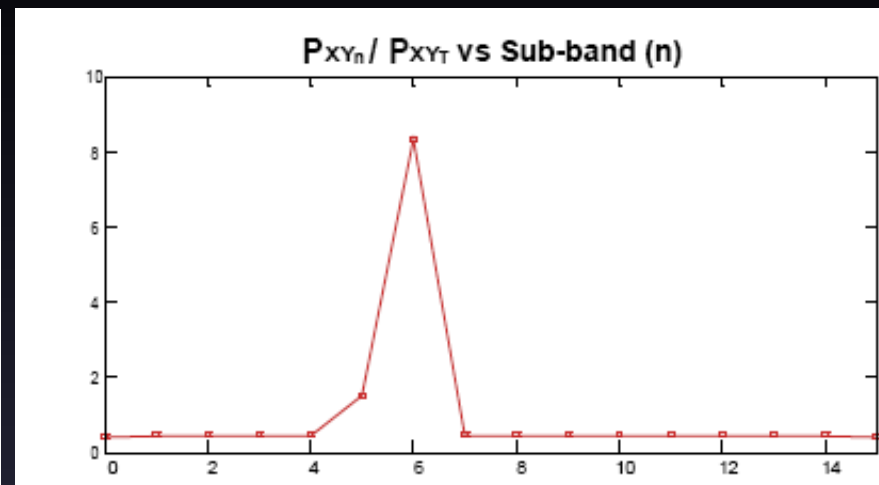
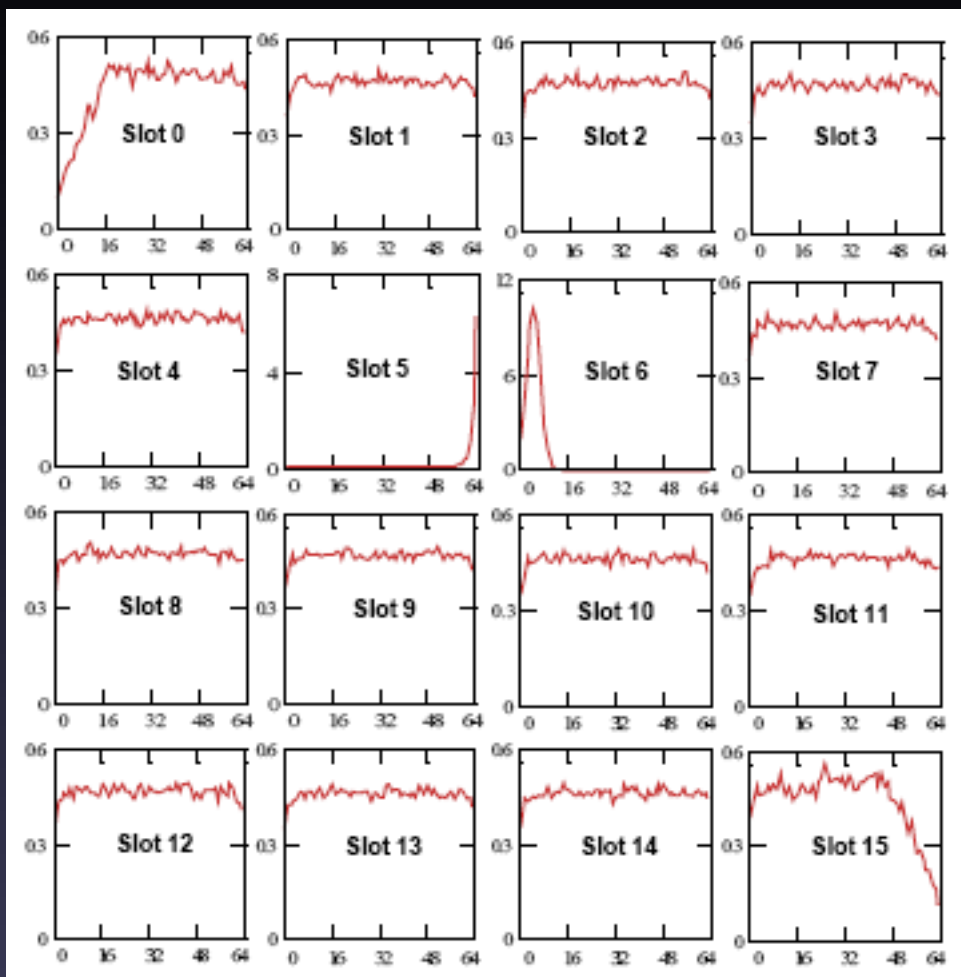
16 sub-bands



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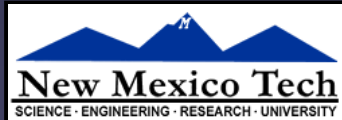


# FXF Output: sub-band alignment & aliasing



16 sub-bands

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# How to Obtain Finer Frequency Resolution

- The size of a correlator (number of chips, speed, etc.) is generally set by the **number of baselines** ( $\propto N_{ant}^2$ ) and the **maximum total bandwidth**. [note also copper/connectivity costs...]

- **Subarrays**

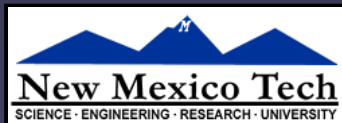
... trade antennas for channels

- **Bandwidth**

-- cut  $\Delta\nu$ :

$\Rightarrow$  same number of lags/spectral points across a smaller  $\Delta\nu$ :  $N_{\text{lag}} = \text{constant}$

$\Rightarrow$  narrower channels:  $\nu \propto \Delta\nu$   
...limited by filters



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## -- recirculation:

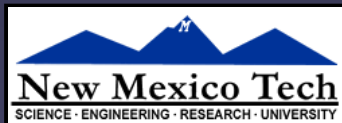
- chips are generally running flat-out for max.  $\Delta\nu$  (e.g. EVLA/WIDAR uses a 256 MHz clock with  $\Delta\nu = 128$  MHz/sub-band)
- For smaller  $\Delta\nu$ , chips are sitting idle most of the time: e.g., pass 32 MHz to a chip capable of doing 128 M multiplies per second

⇒ add some memory, and send two copies of the data with different delays

$$\Rightarrow N_{\text{chan}} \propto 1/\Delta\nu$$

$$\Rightarrow \delta\nu \propto (\Delta\nu)^2$$

...limited by memory & data output rates



# VLA Correlator:

## Bandwidths and Numbers of Channels

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Table 14: Available bandwidths and number of spectral line channels in normal mode

BW Code	Bandwidth MHz	Single IF Mode <sup>(1)</sup>		Two IF Mode <sup>(2)</sup>		Four IF Mode <sup>(3)</sup>	
		No. Channels <sup>(4)</sup>	Freq. Separ. kHz	No. Channels <sup>(4)</sup> per IF	Freq. Separ. kHz	No. Channels <sup>(4)</sup> per IF	Freq. Separ. kHz
0	50	16	3125	8	6250	4	12500
1	25	32	781.25	16	1562.5	8	3125
2	12.5	64	195.313	32	390.625	16	781.25
3	6.25	128	48.828	64	97.656	32	195.313
4	3.125	256	12.207	128	24.414	64	48.828
5	1.5625	512	3.052	256	6.104	128	12.207
6	0.78125	512	1.526	256	3.052	128	6.104
8	0.1953125	256	0.763	128	1.526	64	3.052
9	0.1953125	512	0.381	256	0.763	128	1.526

Notes:

(1) Observing Modes 1A, 1B, 1C, 1D.

(2) Observing Modes 2AB, 2AC, 2AD, 2BC, 2BD, 2CD.

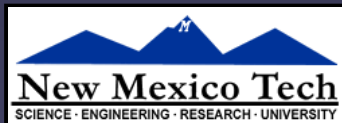
(3) Observing Modes 4, PA, PB. It is possible to use the output from one, two or four IFs in such a way as to obtain different combinations of number of spectral line channels and channel separation. The minimum and maximum number of channels is 4 and 512 respectively.

(4) These are the numbers of spectral line channels produced in the array processor. Any number of spectral line channels that is a power of 2, that is less than or equal to the number in the table and that is greater than or equal to 2 may be selected using the data selection options available within the **OBSERVE** and **JObserve** programs.

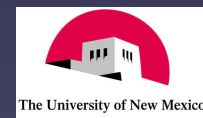


## VLBI

- difficult to send the data to a central location in real time
- long baselines, unsynchronized clocks  $\Rightarrow$  relative phases and delays are poorly known
- So, record the data and correlate later
- Advantages of 2-level recording

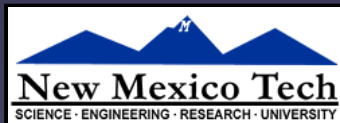


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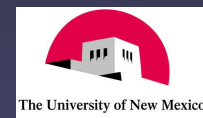


# Correlator Efficiency $\eta_c$

- quantization noise
- overhead
  - don't correlate all possible lags
  - blanking
- errors
  - incorrect quantization levels
  - incorrect delays

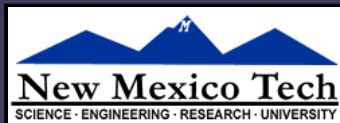


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# Choice of Architecture

- **number of multiplies**: FX wins as  $\{N_{at}, N_{den}\} \uparrow$   
 multiplies per second  $\sim N_{at}^2 \Delta\nu N_{pol} N_{den}$
- **number of logic gates**: XF multiplies are much easier than FX; which wins, depends on current technology
- **shuffling the data about**: “copper” favors XF over FX for big correlators
- **bright ideas** help: hybrid correlators, nifty correlator chips, etc.

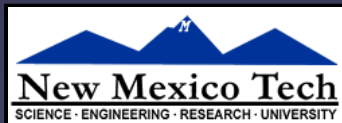


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# New Mexico Correlators

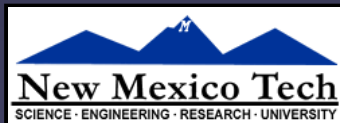
	VLA	EVLA (WIDAR)	VLBA
Architecture	XF	FXF	FX
Quantization	3-level	16/256-level	2- or 4-level
$N_{at}$	27	40	20
Max. $\Delta\nu$	0.2 GHz	16 GHz	0.256 GHz
$N_{dm}$	1 - 512	16,384 - 262,144	256 - 2048
Min. $\delta\nu$	381 Hz	0.12 Hz	61.0 Hz
$dt_{m}$	1.7 s	0.01 s	0.13 s
Power req't.	50 kW	135 kW	10-15 kW
Data rate	$3.3 \times 10^3$ vis/sec	$2.6 \times 10^7$ vis/sec	$3.3 \times 10^6$ vis/sec



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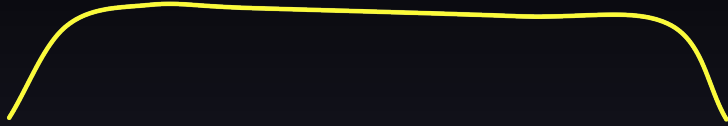
# Spectral tuning, shaping, & response



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# The spectrum: “receiver” response



Receiver response (analog)  
...fixed in frequency

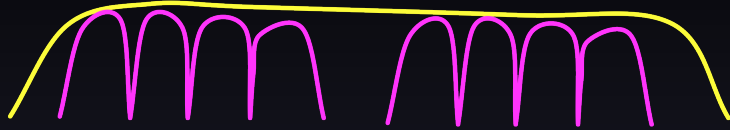
Examples:

EVLA Ka band: 26.5- 40 GHz

ALMA Band 4: 125 -163 GHz

VLBA 4cm: 8 - 8.8 GHz

# Basebands: final analog filtering



...split into **basebands**  
(final analog filtering)

Examples:

EVLA 2 x 1 GHz or 4 x 2 GHz

ALMA 4 x 2 GHz

VLBA 16 x 0.0625-16 MHz

VLBA upgrade 2 x 512 MHz

# Basebands: tuning



Sets of basebands are independently tunable (multiple **LO chains**)

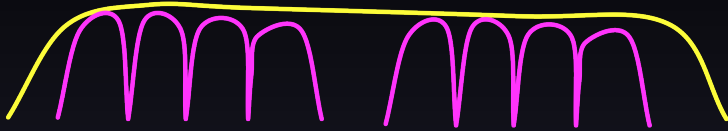
Examples:

EVLA 2 LO chains (AC, BD)

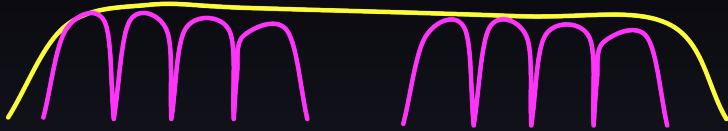
ALMA similar



# Basebands: tuning



# Basebands: tuning



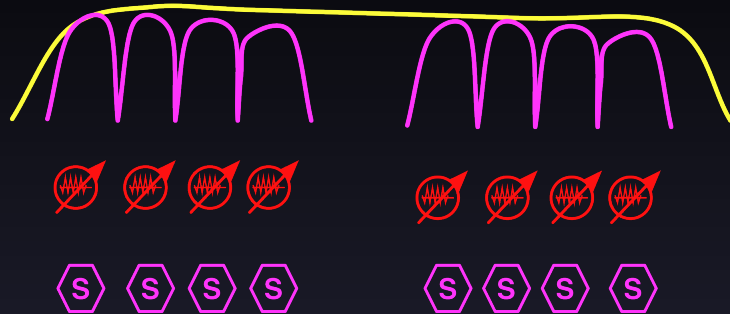
# Basebands: digitizing



Each baseband is digitized  
by a *sampler*

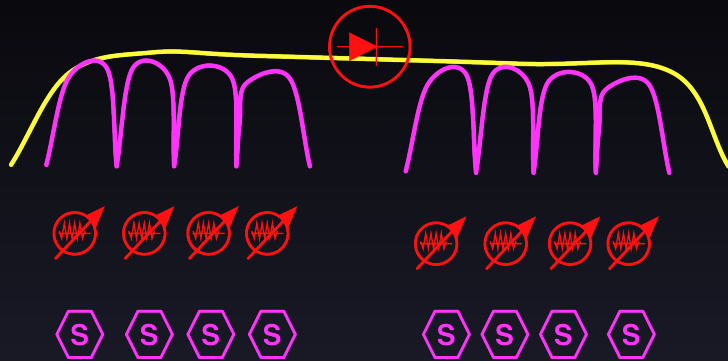


## Basebands: variable gain



Since we want to use all available bits in the samplers, we insert a *variable gain* (attenuation) to keep the input power constant...

## Basebands: variable gain



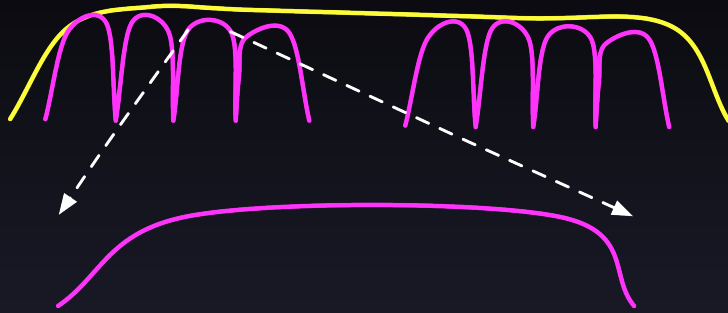
...we track the resulting variable gain by adding a known amount of noise before the samplers:

*noise tube ( $T_{cal}$ )*

This is the *switched power* measurement.

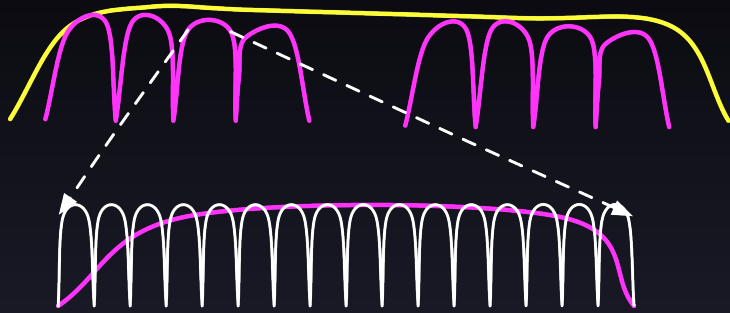
N.B. millimeter telescopes don't do this – instead they track the total power (system temperature) and use a hot load as reference. See Crystal Brogan's talk.

## Zooming in on a baseband: subbands



Even single basebands (1-2 GHz) are too wide for easy processing...

## Zooming in on a baseband: subbands



...so in hybrid correlators  
(EVLA, ALMA) we use  
digital (polyphase/FIR)  
filters to subdivide into  
*subbands*

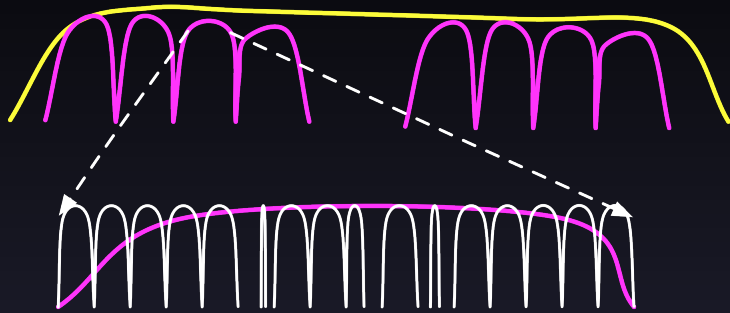
Examples:

EVLA 16 subbands/baseband

ALMA 32 subbands/baseband

(TFB=Tunable Filter Bank)

## Zooming in on a subband: basebands



More complex filters (more taps) give better filter shapes, and/or narrower filters

Note that each filter is *independent*

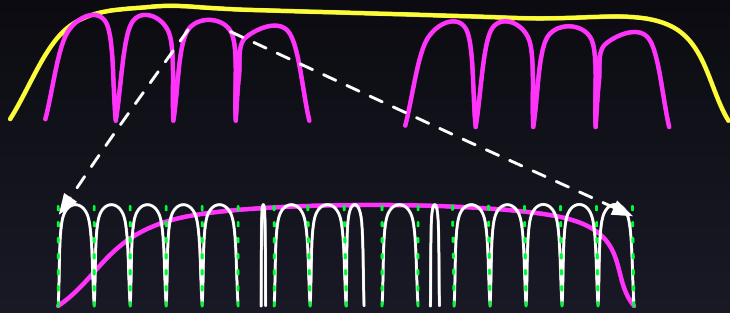
Examples:

EVLA 31.25 kHz-128 MHz

ALMA 31.25 MHz or 62.5 MHz



## Subbands: tuning restrictions



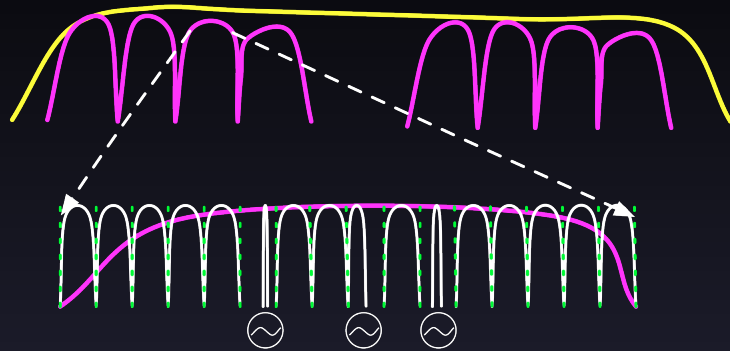
Polyphase filters divide the baseband *evenly* into subbands; you can put the subbands only into certain **slots** in the baseband.

Examples:

EVLA @ 128 MHz BW:

0-128, 128-256, 256-384,  
384-512, 512-640, 640-768,  
768-896, 896-1024 MHz

# Subbands: tuning restrictions



...so we add digital **mixers**  
to fine-tune the subbands

Examples:

EVLA after 128 MHz filtering

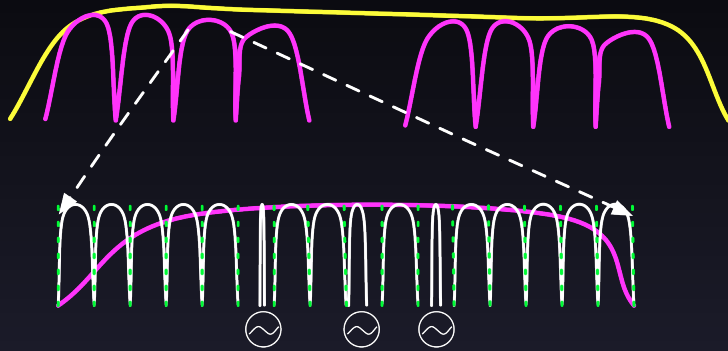
Hz-ish resolution

→ cannot cross 128 MHz  
boundaries

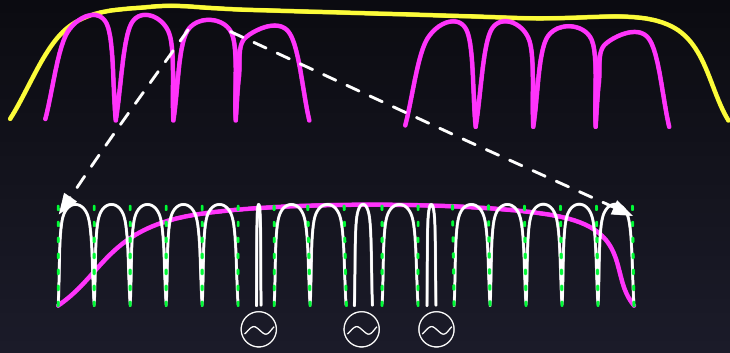
ALMA before all digital filtering,  
32.5 kHz resolution

→ ~no tuning restrictions –  
can overlap subbands even  
at full bandwidth

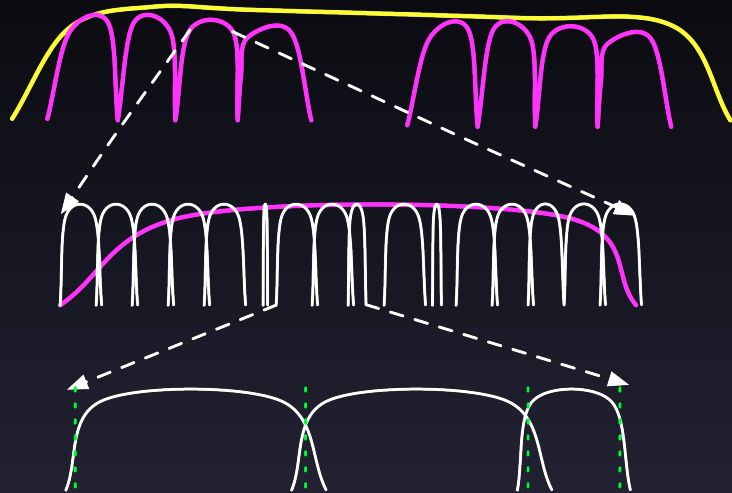
# Subbands: fine-tuning



# Subbands: fine-tuning



# Zooming in on subbands: sideband rejection

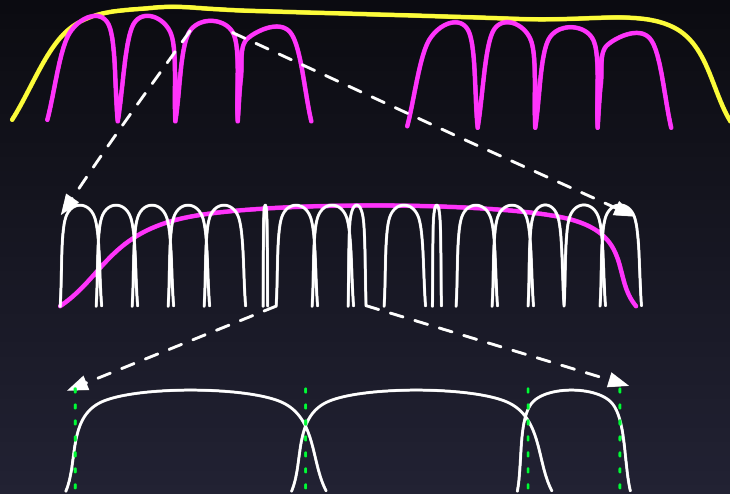


Even digital filters aren't perfect: they do not completely reject out-of-band signals, especially at the edges.

This adds noise (which can't be avoided:  $\sqrt{2}$  in SNR) and unwanted signals (e.g., RFI).

Other nasty things creep in: e.g., sampler offsets.  
*Cf. VLA's transition system...*

# Zooming in on subbands: sideband rejection



So we filter out the unwanted sideband.

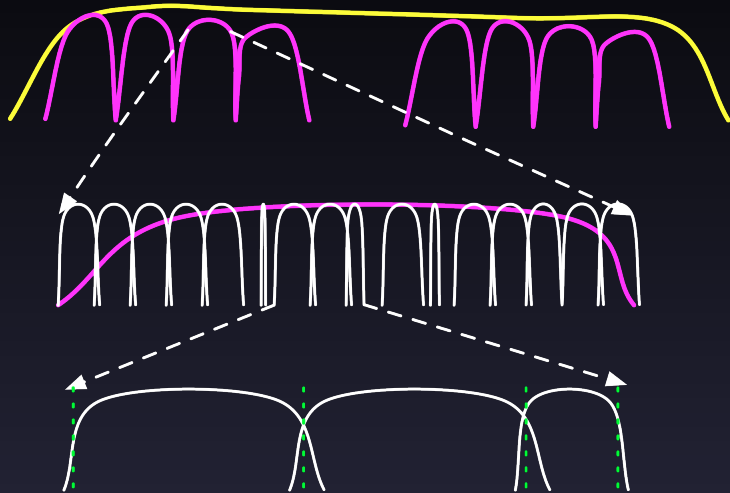
In the time domain: **Walsh function switching**

Examples: VLA, ALMA

In the frequency domain:  
*frequency offsets* put in at the antenna and removed in the correlator

Examples: EVLA (WIDAR's "fshift"), VLBA (Doppler offsets).

# Zooming in on subbands: sideband rejection

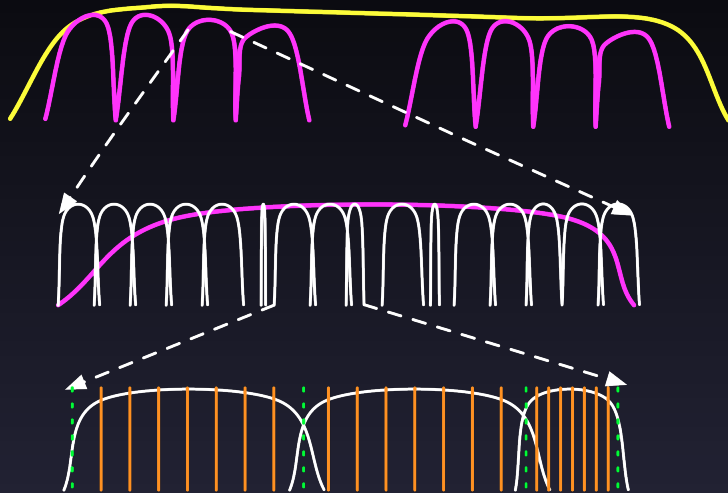


This knocks out the signals (at some level) but not the noise.

ALMA will overlap subbands to avoid this – at the expense of 10%-ish of the baseband.

EVLA cannot do so when using the widest bandwidth (i.e., 128 MHz subbands) → time multiplexing?

# At last, the actual correlator!



The correlator (FX or XF) gives a certain number of channels across each subband.

Examples:

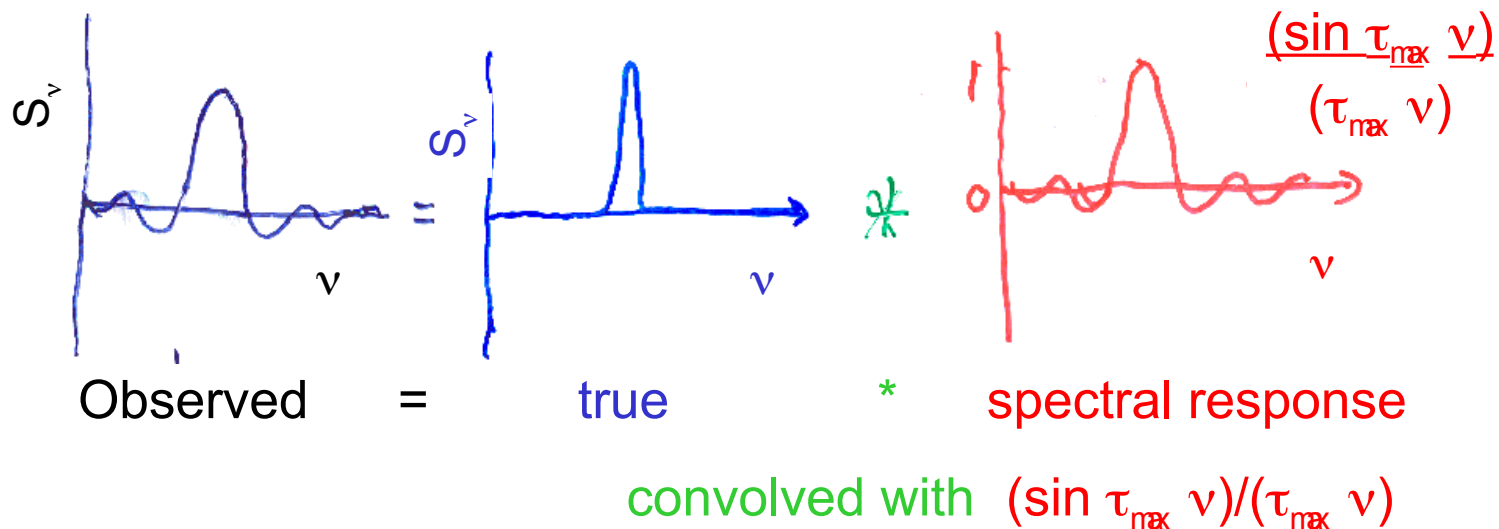
EVLA, ALMA:

256 channels/subband split amongst 1, 2, or 4 pol'n products (2 MHz for 4 pol'n products at max bandwidth)



# Spectral Response: XF Correlator

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# Spectral Response; Gibbs Ringing

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- **XF correlator:** limited number of lags  $N$ 
  - ⇒ 'uniform' coverage to max. lag  $N\Delta t$
  - ⇒ Fourier transform gives spectral response

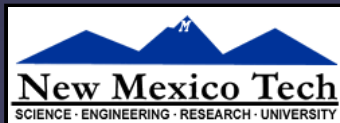
$$\frac{\sin(N\Delta\tau)\nu}{(N\Delta\tau)\nu}$$

- 22% sidelobes!
- Hanning smoothing

- **FX correlator:** as XF, but Fourier transform before multiplication
  - ⇒ spectral response is

$$\left(\frac{\sin(N\Delta\tau)\nu}{(N\Delta\tau)\nu}\right)^2$$

- 5% sidelobes

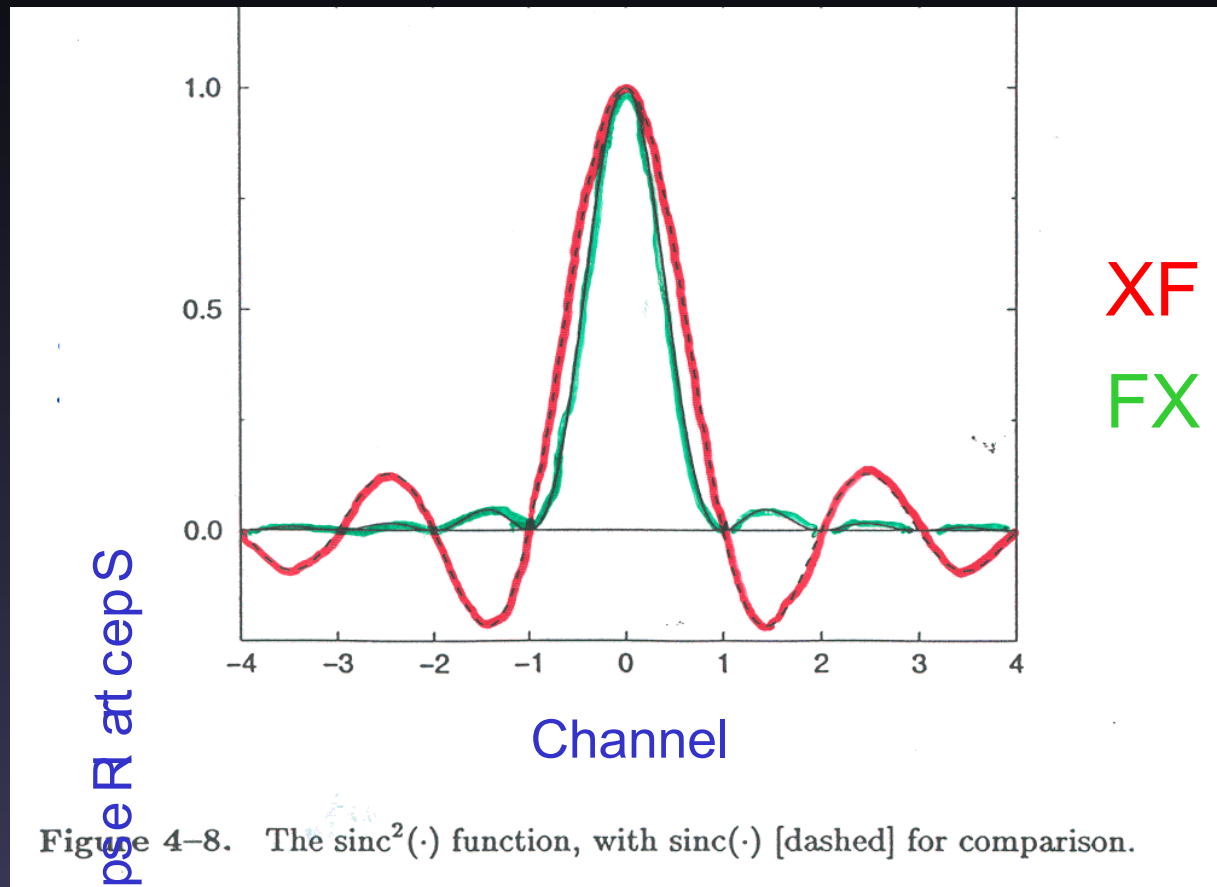


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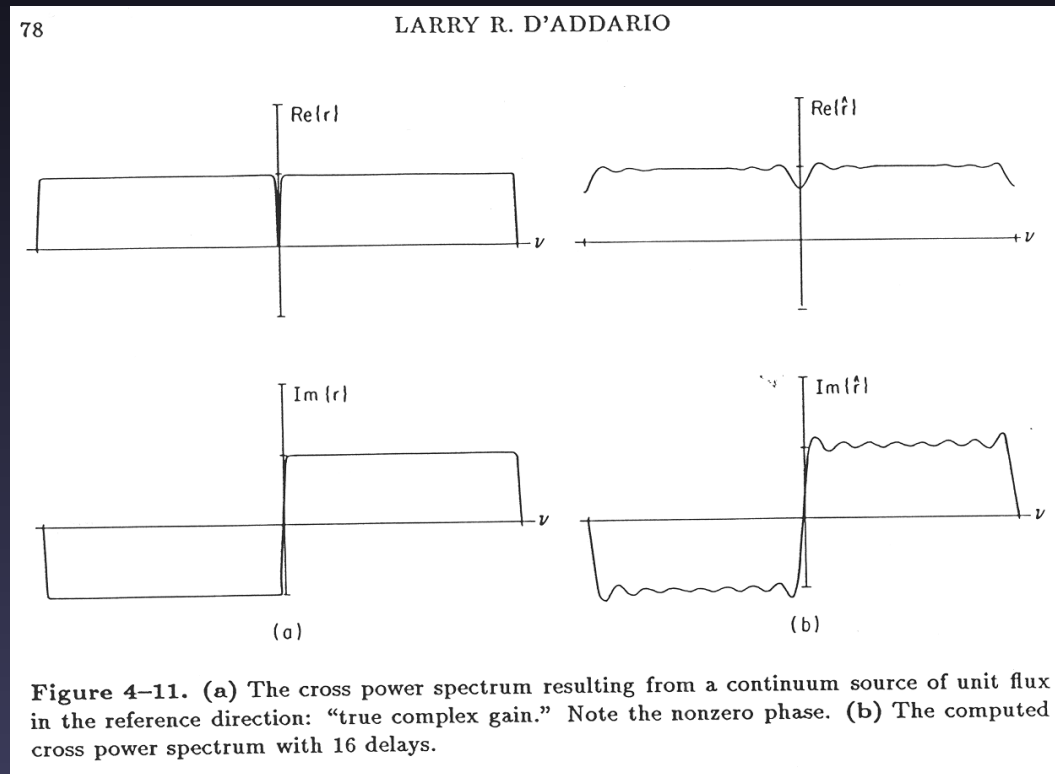
# $\text{sinc}(\cdot)$ vs. $\text{sinc}^2(\cdot)$

75

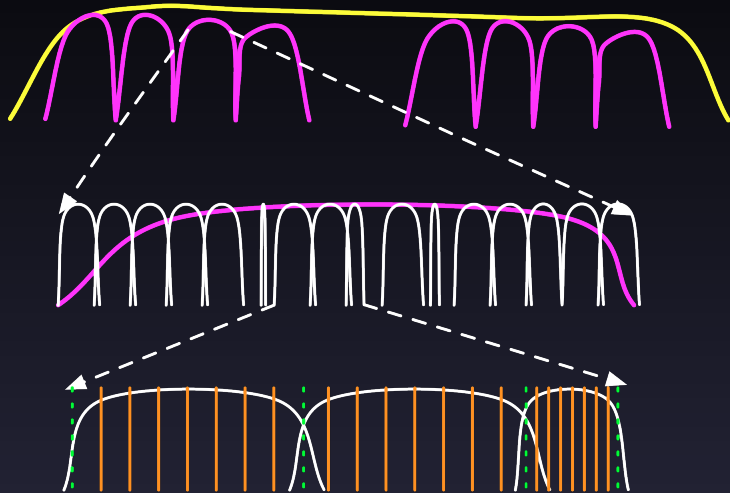


esnope R at cepS

- *n.b.* radio frequency interference is spread across frequency by the spectral response
- **Gibbs phenomenon:** ‘ringing’ off the band edges



# Higher spectral resolution 1: narrow subbands

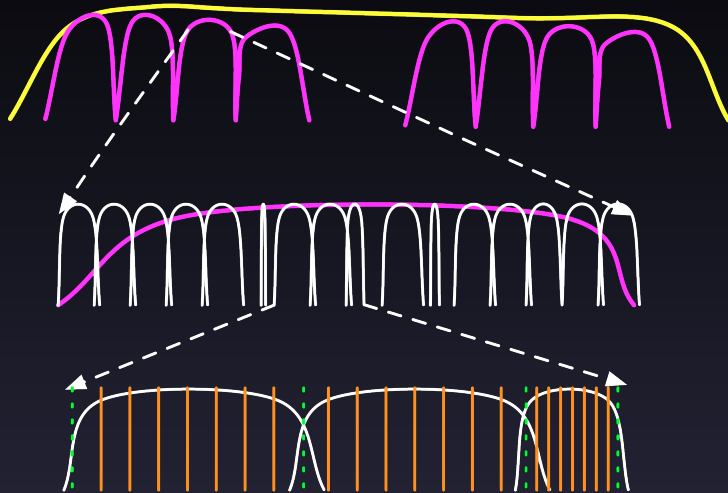


Same number of channels  
regardless of bandwidth –  
just choose the lags  
carefully

Example:

EVLA 31.25 kHz subband, dual  
pol'n → 244 Hz channels

## Higher spectral resolution 2: fewer subbands



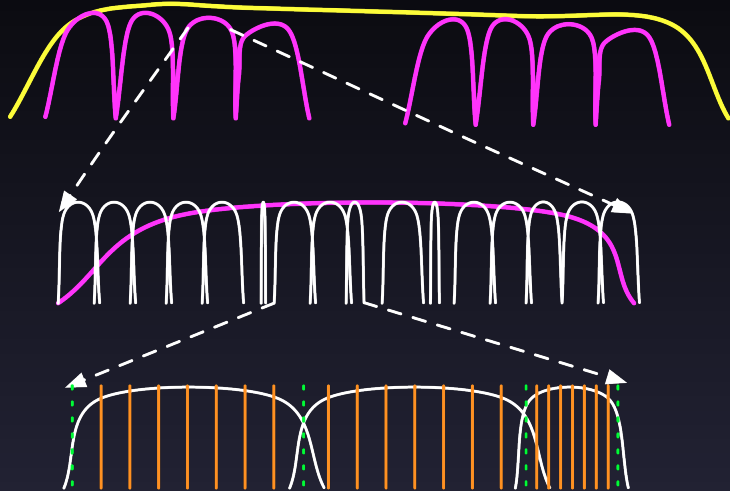
With appropriate interconnects one can trade subbands for channels.

This is the prime mode for ALMA.

Example:

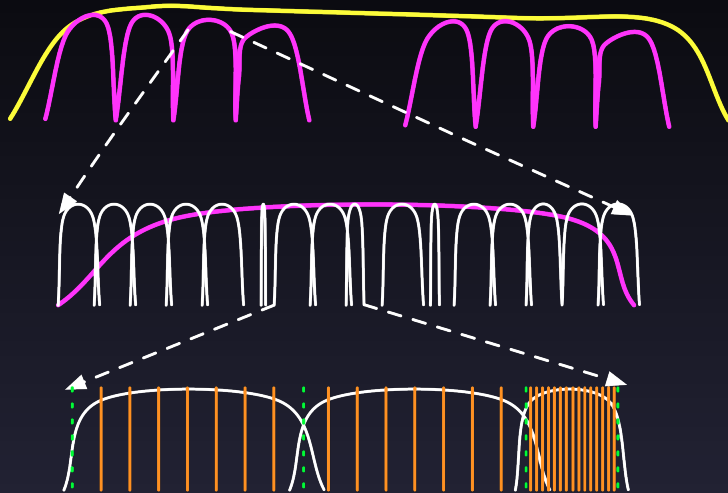
ALMA 2 x 62.5 MHz subbands  
with 8192 channels, rather  
than 32 x 62.5 MHz  
→ 15 rather than 244 kHz  
channels

## Higher spectral resolution 3: pol'n products



Avoid correlating unwanted pol'n products (e.g., RL&LR) for corresponding gain in spectral resolution.

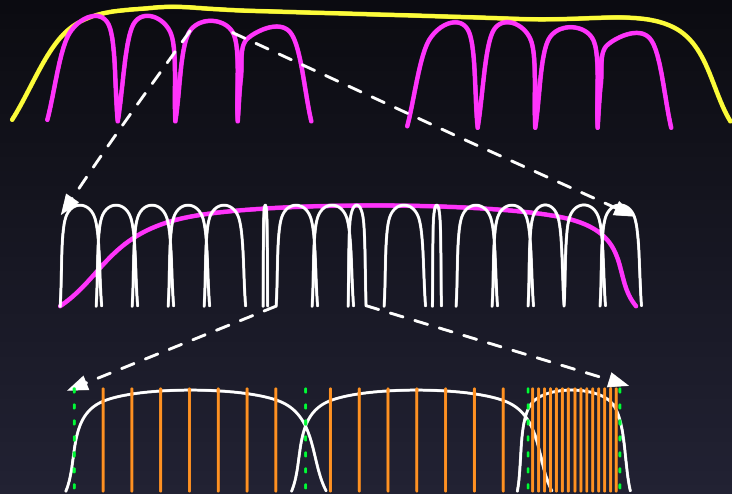
## Higher spectral resolution 4: recirculation



For narrow bandwidths the correlator chips are sitting idle much of the time. Add memory & pipe the same data to the chips over and over, asking for different lags each time. This gives a factor  $N$  more channels for subbands of bandwidth  $BW_{max}/N$ .



# Higher spectral resolution 4: recirculation



Example: EVLA, 1 pp

$BW_{max} = 128 \text{ MHz}$

256 ch.  $\rightarrow$  500 kHz/ch

Select BW= 2 MHz

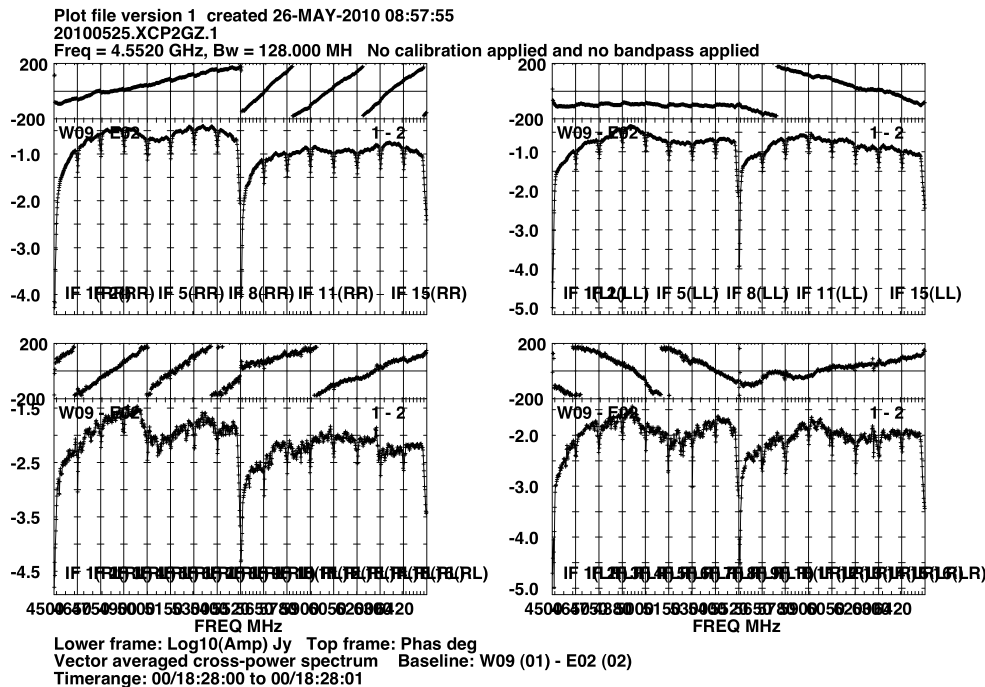
256 ch.  $\rightarrow$  7.8 kHz/ch

Recirculation:

$256 * 128/2 = 16384 \text{ ch!}$

$\rightarrow$  0.12 kHz/ch

# Data rates & volumes



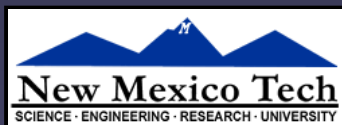
EVLA “RSRO” spectrum  
 2x1 GHz (16x128 MHz)  
 64 ch/pp/sb → 4096 ch  
 2 MHz channels  
 This is *one baseline, one dump*  
 EVLA: 27 ant → 351 bl  
 10 B/vis  
 → 14 MB/dump  
 8 GHz/poln  
 → 55 MB/dump

## Current VLA

## EVLA/WIDAR

Bandwidth MHz	Single Pol. Prod.		Two Pol.Prod.		Four Pol.Prod.	
	No. Channels	Freq. Separ. kHz	No. Channels per pol	Freq. Separ. kHz	No. Channels per pol	Freq. Separ. kHz
100	16	6250	8	12500	2	50000
50	16	3125	8	6250	4	12500
25	32	781.25	16	1562.5	8	3125
12.5	64	195.313	32	390.625	16	781.25
6.25	128	48.828	64	97.656	32	195.313
3.125	256	12.207	128	24.414	64	48.828
1.5625	512	3.052	256	6.104	128	12.207
0.78125	512	1.526	256	3.052	128	6.104
0.19531	512	0.381	256	0.763	128	1.526

Bandwidth MHz	Single Pol. Prod.		Two Pol.Prod.		Four Pol.Prod.	
	No. Channels	Freq. Separ. kHz	No. Channels per pol	Freq. Separ. kHz	No. Channels per pol	Freq. Separ. kHz
8192	16,384	500	8,192	1000	4,096	2000
4096	16,384	250	8,192	500	4,096	1000
2048	32,768	62.5	16,384	31.25	8,192	250
1024	65,536	15.625	32,768	31.25	16,384	62.5
512	131,072	3.906	65,536	7.813	32,768	15.625
256	262,144	0.977	131,072	1.953	65,536	3.906
128	262,144	0.488	131,072	0.977	65,536	1.953
64	262,144	0.244	131,072	0.488	65,536	0.977
32	262,144	0.122	131,072	0.244	65,536	0.488
16	262,144	0.061	131,072	0.122	65,536	0.244
8	262,144	0.031	131,072	0.061	65,536	0.122
4	262,144	0.015	131,072	0.031	65,536	0.061
2	262,144	0.008	131,072	0.015	65,536	0.031
1	262,144	3.8 Hz	131,072	7.6 Hz	65,536	0.015
0.5	262,144	1.9 Hz	131,072	3.8 Hz	65,536	7.6 Hz
0.25	262,144	0.95 Hz	131,072	1.9 Hz	65,536	3.8 Hz
0.125	262,144	0.48 Hz	131,072	0.95 Hz	65,536	1.9 Hz
0.0625	262,144	0.24 Hz	131,072	0.48 Hz	65,536	0.95 Hz
0.03125	262,144	0.12 Hz	131,072	0.24 Hz	65,536	0.48 Hz



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