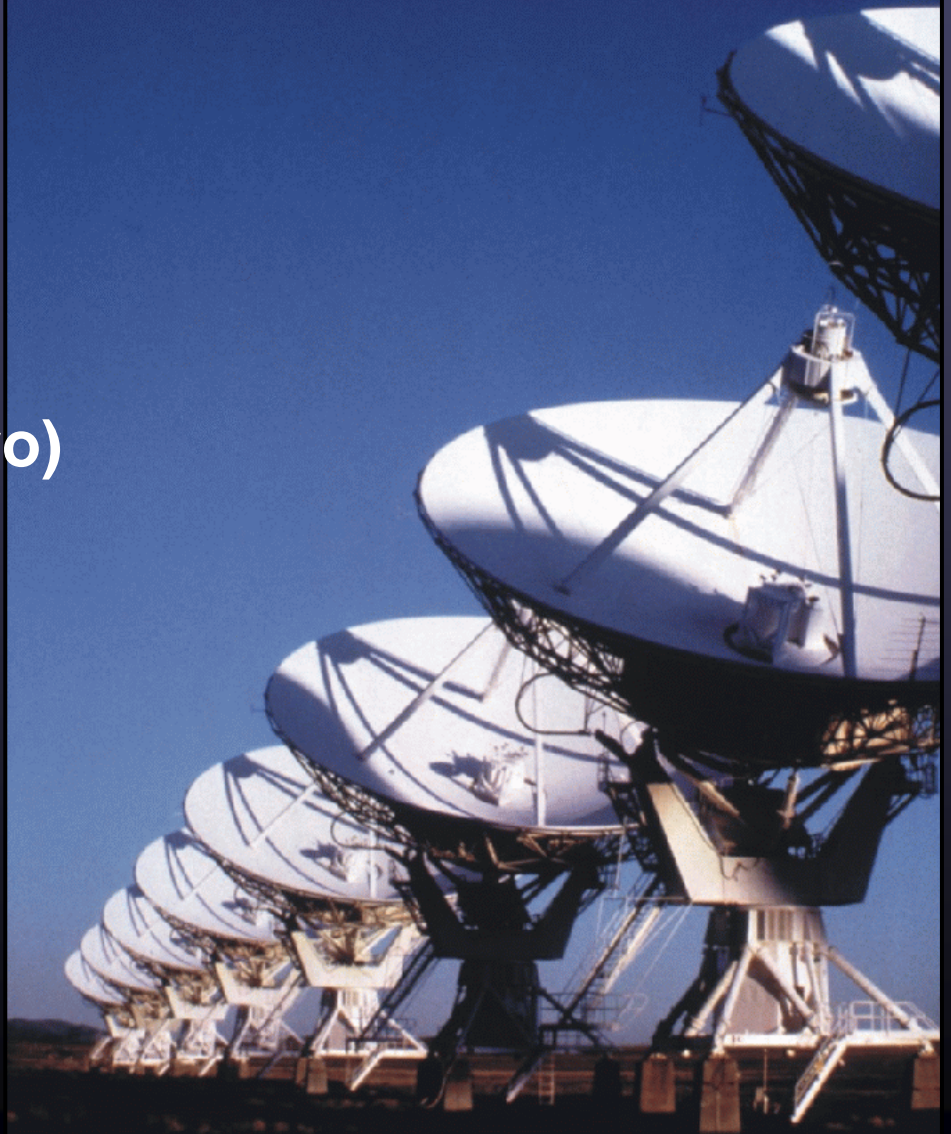


# Polarization in Interferometry

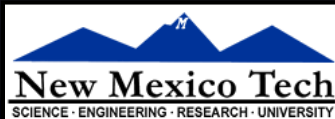
Steven T. Myers (NRAO-Socorro)

*Eleventh Synthesis Imaging Workshop  
Socorro, June 10-17, 2008*



# Polarization in interferometry

- Astrophysics of Polarization
- Physics of Polarization
- Antenna Response to Polarization
- Interferometer Response to Polarization
- Polarization Calibration & Observational Strategies
- Polarization Data & Image Analysis



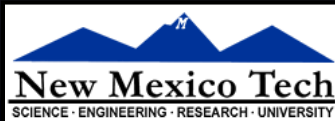
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# WARNING!

- This is tough stuff. Difficult concepts, hard to explain without complex mathematics.
- I will illustrate the concepts with figures and ‘handwaving’.
- Many good references:
  - Synthesis Imaging II: Lecture 6, also parts of 1, 3, 5, 32
  - Born and Wolf: Principle of Optics, Chapters 1 and 10
  - Rofls and Wilson: Tools of Radio Astronomy, Chapter 2
  - Thompson, Moran and Swenson: Interferometry and Synthesis in Radio Astronomy, Chapter 4
  - Tinbergen: Astronomical Polarimetry. All Chapters.
  - J.P. Hamaker et al., A&A, 117, 137 (1996) and series of papers
- Great care must be taken in studying these – conventions vary between them.

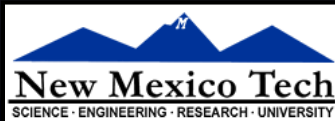
**DON'T PANIC !**



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# Polarization Astrophysics



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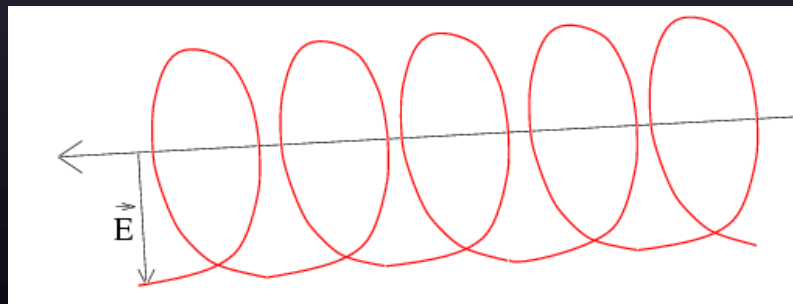


# What is Polarization?

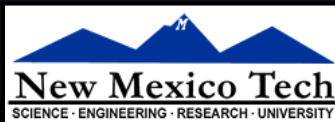
- Electromagnetic field is a vector phenomenon – it has both direction and magnitude.
- From Maxwell's equations, we know a propagating EM wave (in the far field) has no component in the direction of propagation – it is a transverse wave.

$$\mathbf{k} \cdot \mathbf{E} = 0$$

- The characteristics of the transverse component of the electric field,  $\mathbf{E}$ , are referred to as the polarization properties. The  $\mathbf{E}$ -vector follows a (elliptical) helical path as it propagates:

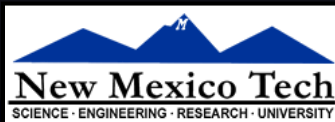


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# Why Measure Polarization?

- Electromagnetic waves are intrinsically polarized
  - monochromatic waves are fully polarized
- Polarization state of radiation can tell us about:
  - the origin of the radiation
    - intrinsic polarization
  - the medium through which it traverses
    - propagation and scattering effects
  - unfortunately, also about the purity of our optics
    - you may be forced to observe polarization even if you do not want to!

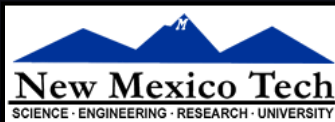


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# Astrophysical Polarization

- Examples:
  - Processes which generate polarized radiation:
    - Synchrotron emission: Up to ~80% linearly polarized, with no circular polarization. Measurement provides information on strength and orientation of magnetic fields, level of turbulence.
    - Zeeman line splitting: Presence of B-field splits RCP and LCP components of spectral lines by by  $2.8 \text{ Hz}/\mu\text{G}$ . Measurement provides direct measure of B-field.
  - Processes which modify polarization state:
    - Free electron scattering: Induces a linear polarization which can indicate the origin of the scattered radiation.
    - Faraday rotation: Magnetoionic region rotates plane of linear polarization. Measurement of rotation gives B-field estimate.
    - Faraday conversion: Particles in magnetic fields can cause the polarization ellipticity to change, turning a fraction of the linear polarization into circular (possibly seen in cores of AGN)



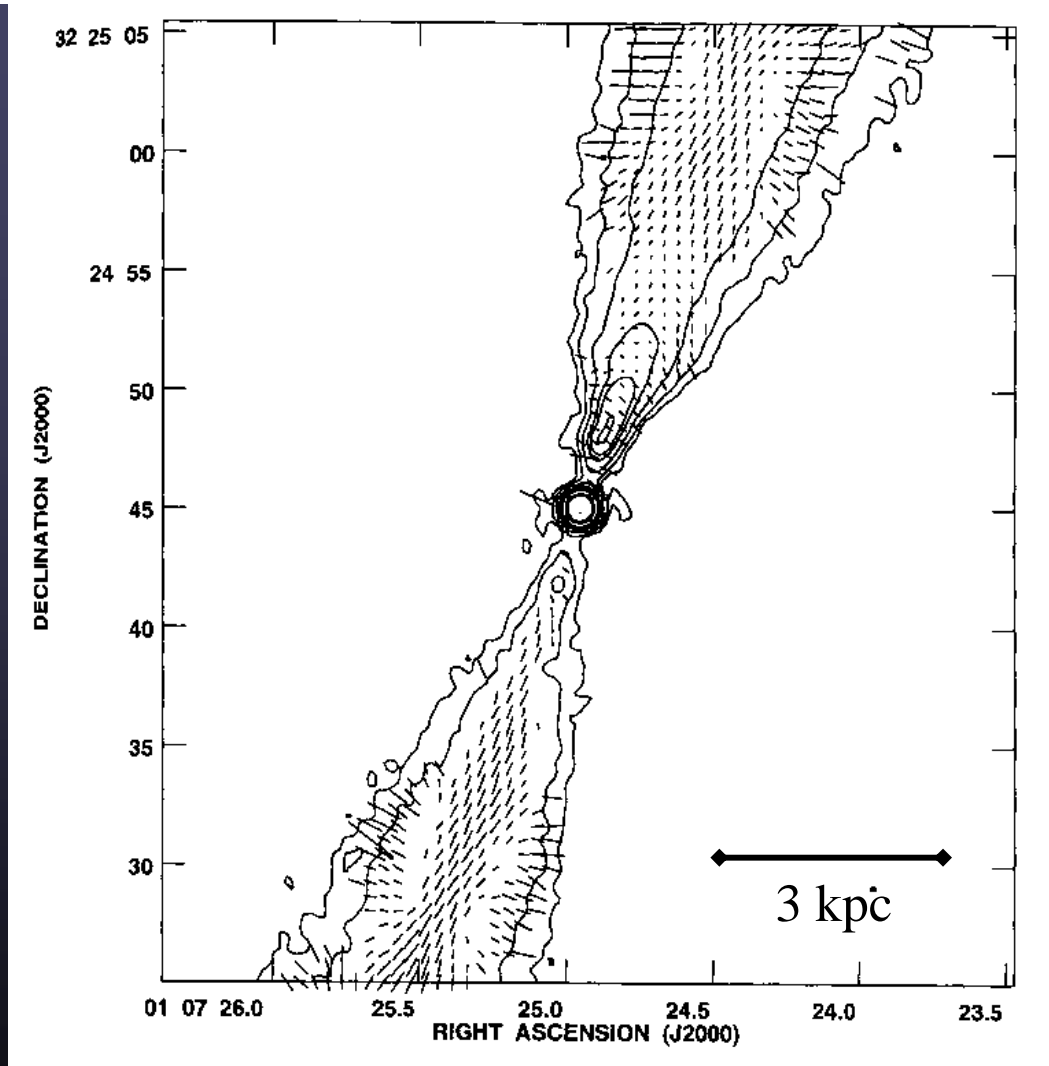
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# Example: Radio Galaxy 3C31

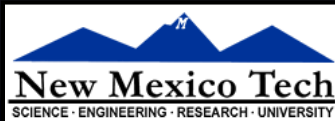
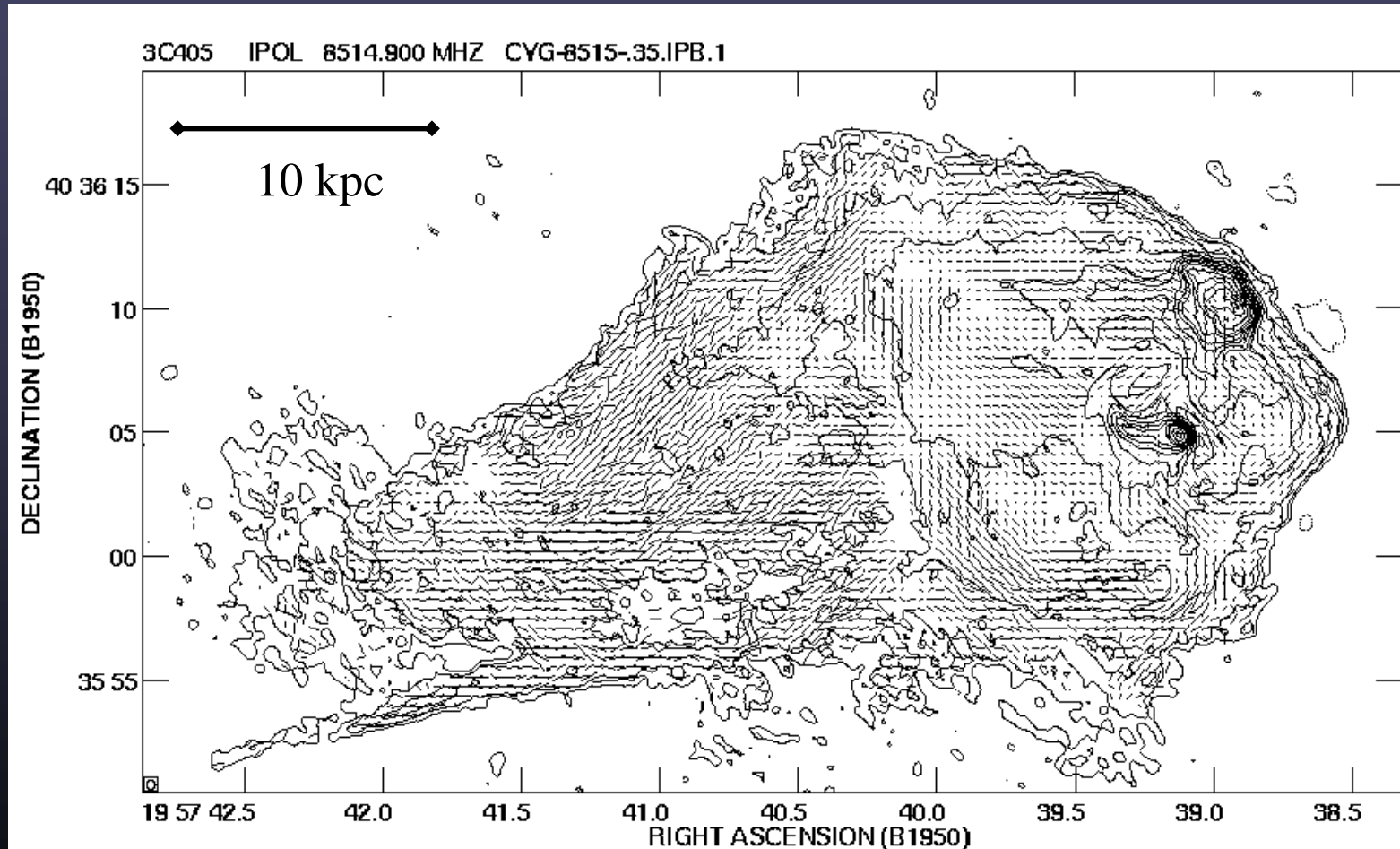
- VLA @ 8.4 GHz
- E-vectors
  - along core of jet
  - radial to jet at edge
- Laing (1996)





# Example: Radio Galaxy Cygnus A

- VLA @ 8.5 GHz B-vectors Perley & Carilli (1996)

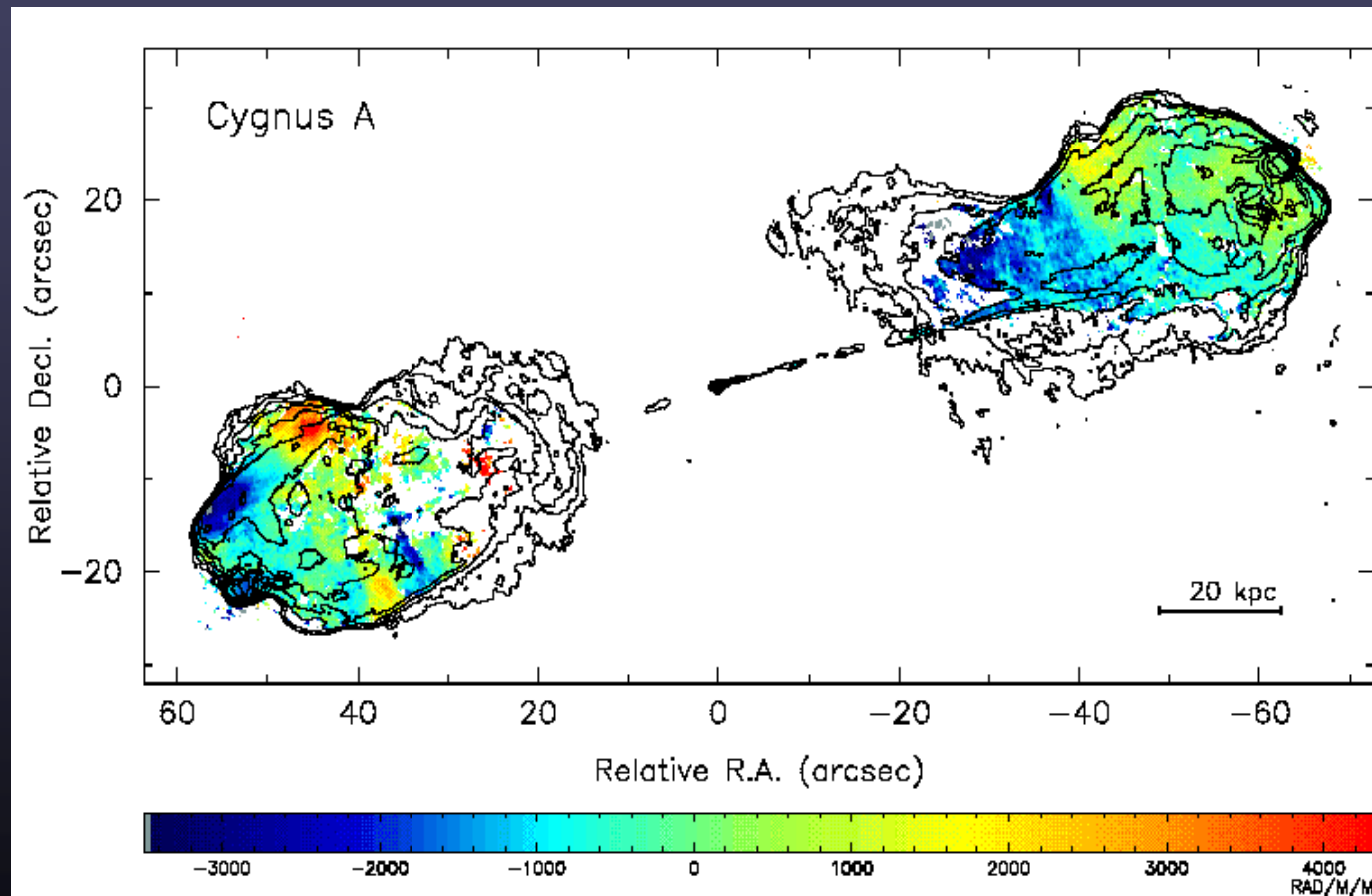


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# Example: Faraday rotation of CygA

- See review of “Cluster Magnetic Fields” by Carilli & Taylor 2002 (ARAA)



# Example: Zeeman effect

## Zeeman Effect

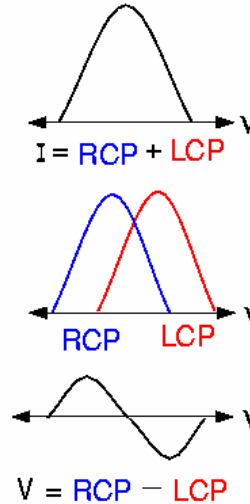
Atoms and molecules with a net magnetic moment will have their energy levels split in the presence of a magnetic field.

⇒ HI, OH, CN, H<sub>2</sub>O

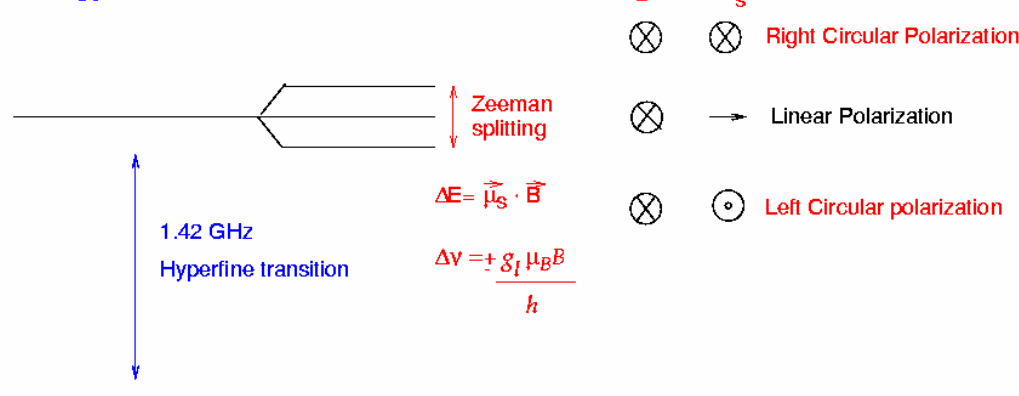
⇒ Detected by observing the frequency shift between right and left circularly polarized emission

⇒  $V = \text{RCP} - \text{LCP} \propto B_{\text{los}}$

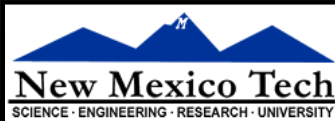
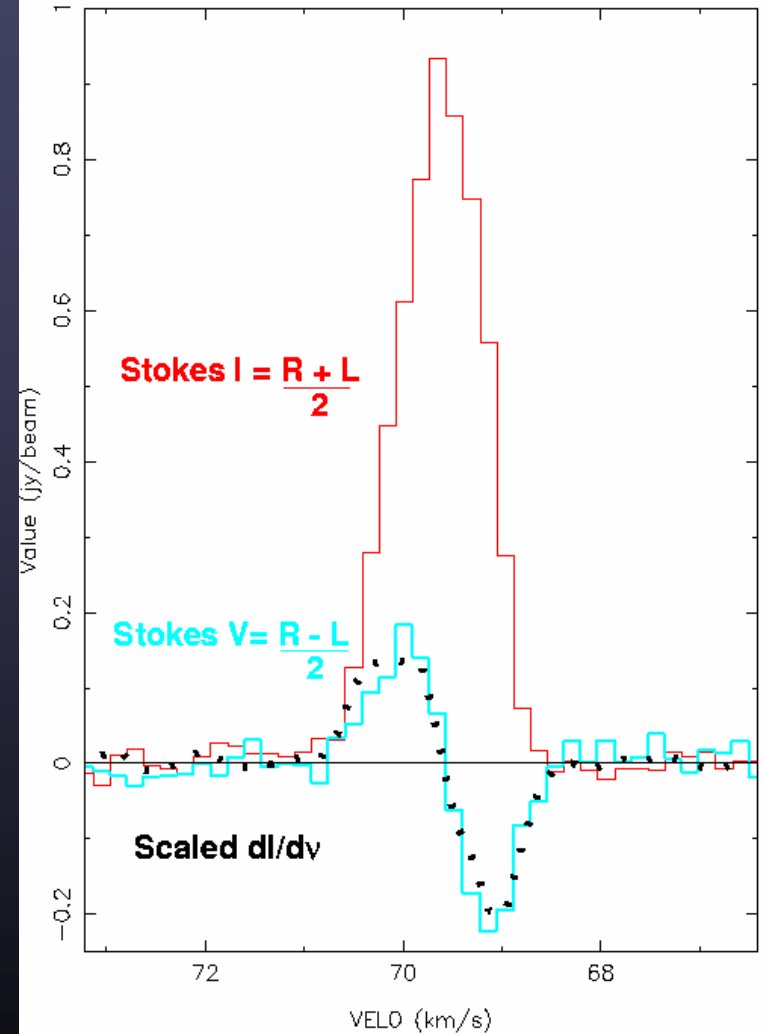
Spectral line profiles



## Energy Levels for HI Ground State



W51C (2-b)  $B_{\theta} = 2.5 \pm 0.2$  mG



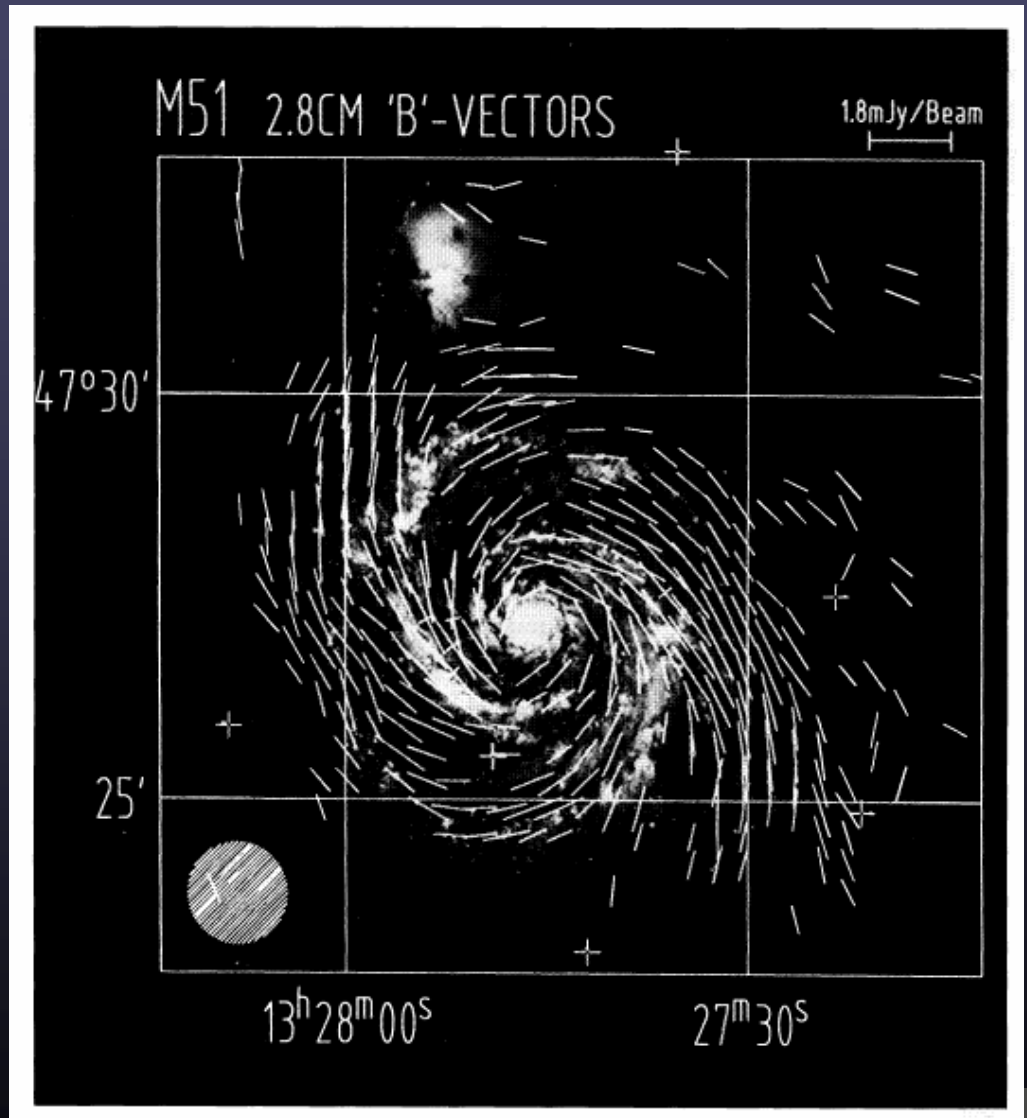
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# Example: the ISM of M51

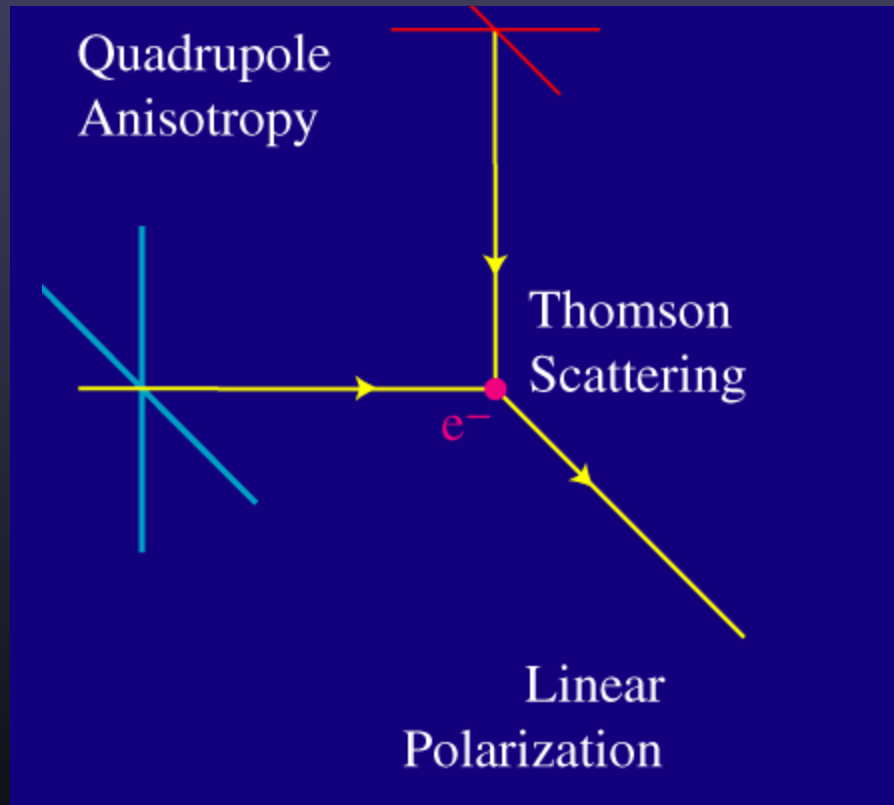
- Trace magnetic field structure in galaxies

*Neininger (1992)*

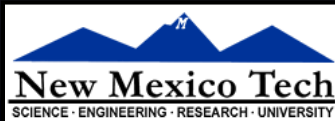
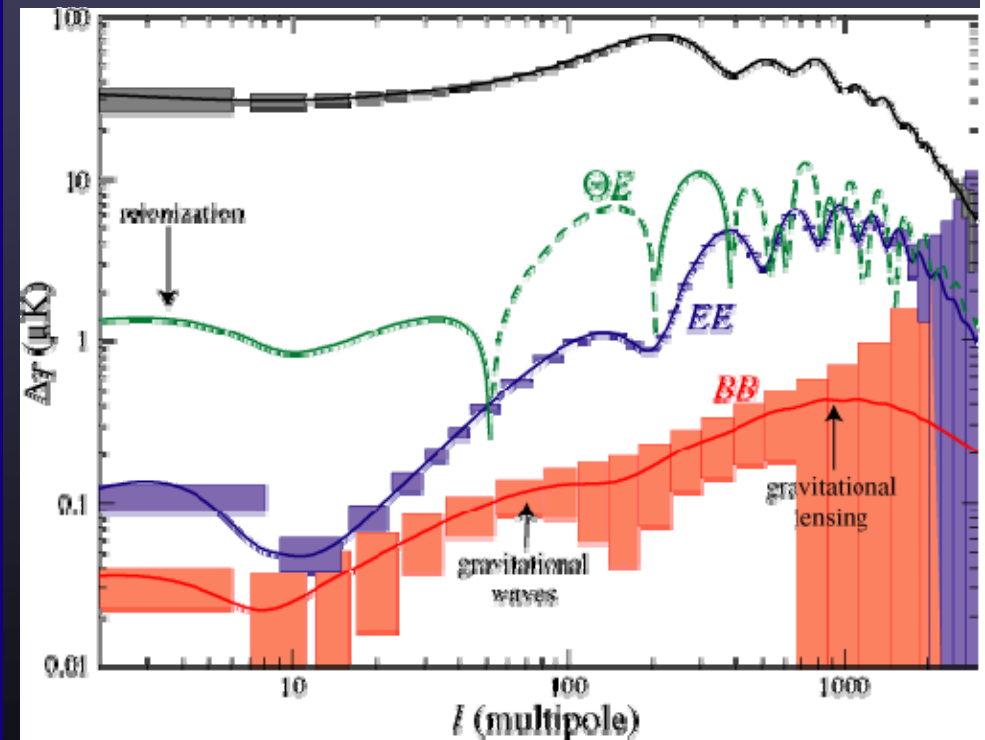


# Scattering

- Anisotropic Scattering induces Linear Polarization
  - electron scattering (e.g. in Cosmic Microwave Background)
  - dust scattering (e.g. in the millimeter-wave spectrum)



Planck predictions – Hu & Dodelson *ARA* 2002

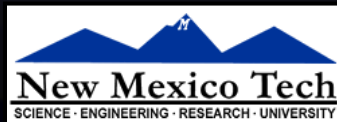


Animations from Wayne Hu

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# Polarization Fundamentals



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# The Polarization Ellipse

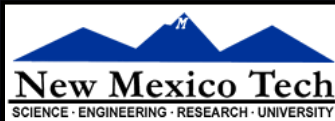
- From Maxwell's equations  $\mathbf{E} \cdot \mathbf{B} = 0$  (E and B perpendicular)
  - By convention, we consider the time behavior of the E-field in a fixed perpendicular plane, from the point of view of the receiver.

- For a monochromatic wave of frequency  $\nu$ , we write

$$E_x = A_x \cos(2\pi\nu t + \phi_x)$$

$$E_y = A_y \cos(2\pi\nu t + \phi_y)$$

- These two equations describe an ellipse in the (x-y) plane.
- The ellipse is described fully by three parameters:
  - $A_x$ ,  $A_y$ , and the phase difference,  $\delta = \phi_y - \phi_x$ .
- The wave is **elliptically polarized**. If the E-vector is:
  - Rotating clockwise, the wave is 'Left Elliptically Polarized',
  - Rotating counterclockwise, it is 'Right Elliptically Polarized'.



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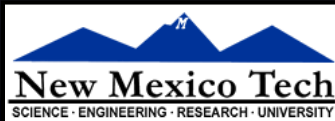
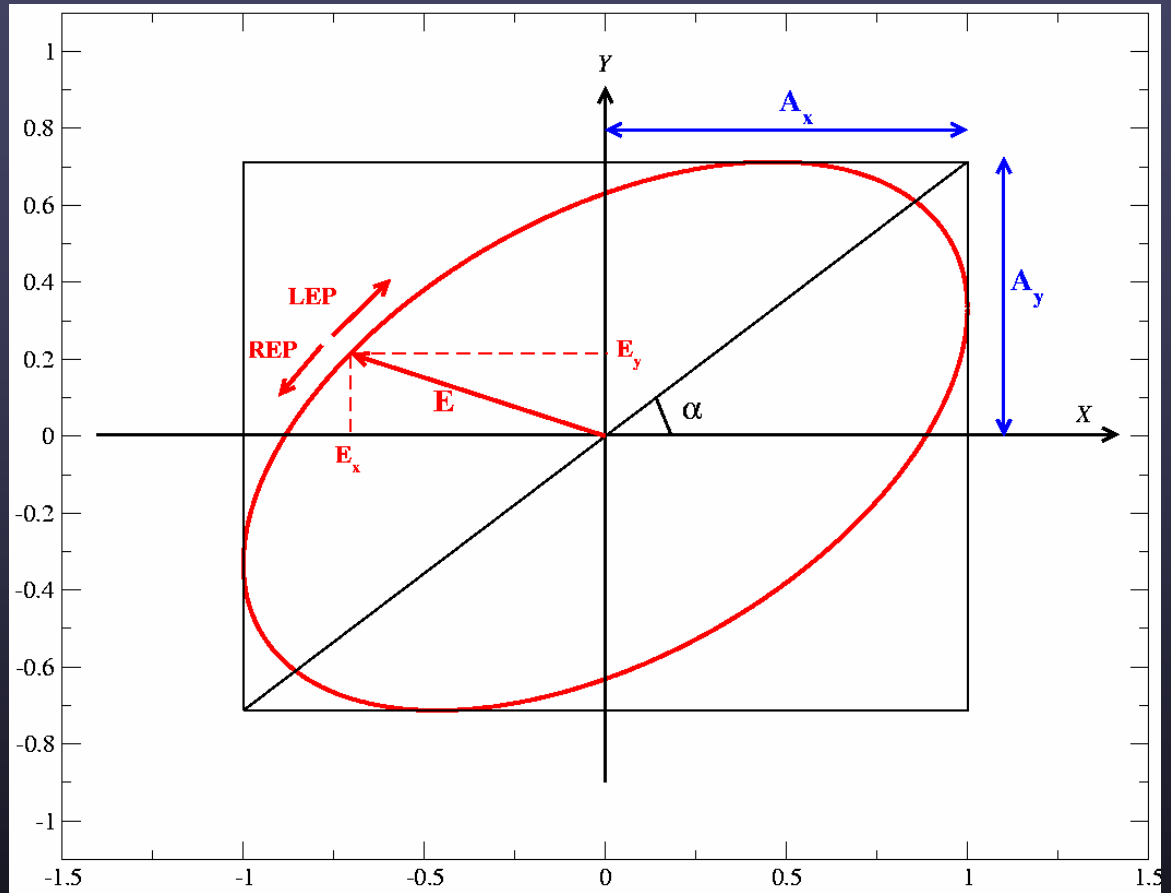


# Elliptically Polarized Monochromatic Wave

The simplest description of wave polarization is in a Cartesian coordinate frame.

In general, three parameters are needed to describe the ellipse.

The angle  $\alpha = \text{atan}(A_Y/A_X)$  is used later ...



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# Polarization Ellipse Ellipticity and P.A.

- A more natural description is in a frame  $(\xi, \eta)$ , rotated so the  $\xi$ -axis lies along the major axis of the ellipse.

- The three parameters of the ellipse are then:

$A_\eta$  : the major axis length

$\tan \chi = A_\xi / A_\eta$  : the axial ratio

$\Psi$  : the major axis p.a.

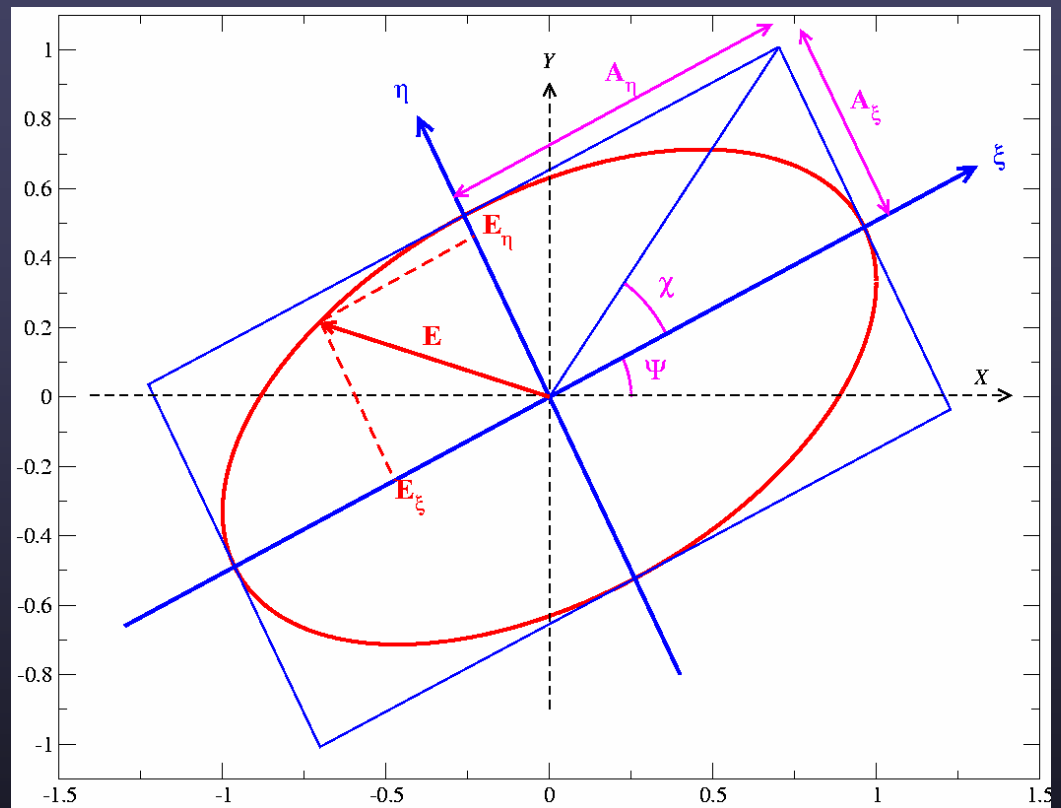
$$\tan 2\Psi = \tan 2\alpha \cos \delta$$

$$\sin 2\chi = \sin 2\alpha \sin \delta$$

- The ellipticity  $\chi$  is signed:

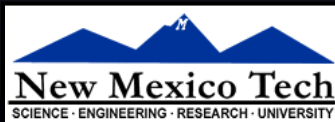
$\chi > 0 \rightarrow \text{REP}$

$\chi < 0 \rightarrow \text{LEP}$



$\chi = 0, 90^\circ \rightarrow \text{Linear } (\delta=0^\circ, 180^\circ)$

$\chi = \pm 45^\circ \rightarrow \text{Circular } (\delta=\pm 90^\circ)$



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# Circular Basis

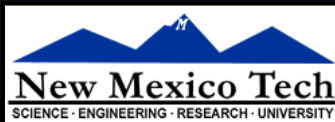
- We can decompose the E-field into a circular basis, rather than a (linear) Cartesian one:

$$\mathbf{E} = A_R \hat{e}_R + A_L \hat{e}_L$$

- where  $A_R$  and  $A_L$  are the amplitudes of two counter-rotating unit vectors,  $e_R$  (rotating counter-clockwise), and  $e_L$  (clockwise)
- NOTE: R,L are obtained from X,Y by  $\delta = \pm 90^\circ$  phase shift
- It is straightforward to show that:

$$A_R = \frac{1}{2} \sqrt{A_X^2 + A_Y^2 - 2 A_X A_Y \sin \delta_{XY}}$$

$$A_L = \frac{1}{2} \sqrt{A_X^2 + A_Y^2 + 2 A_X A_Y \sin \delta_{XY}}$$

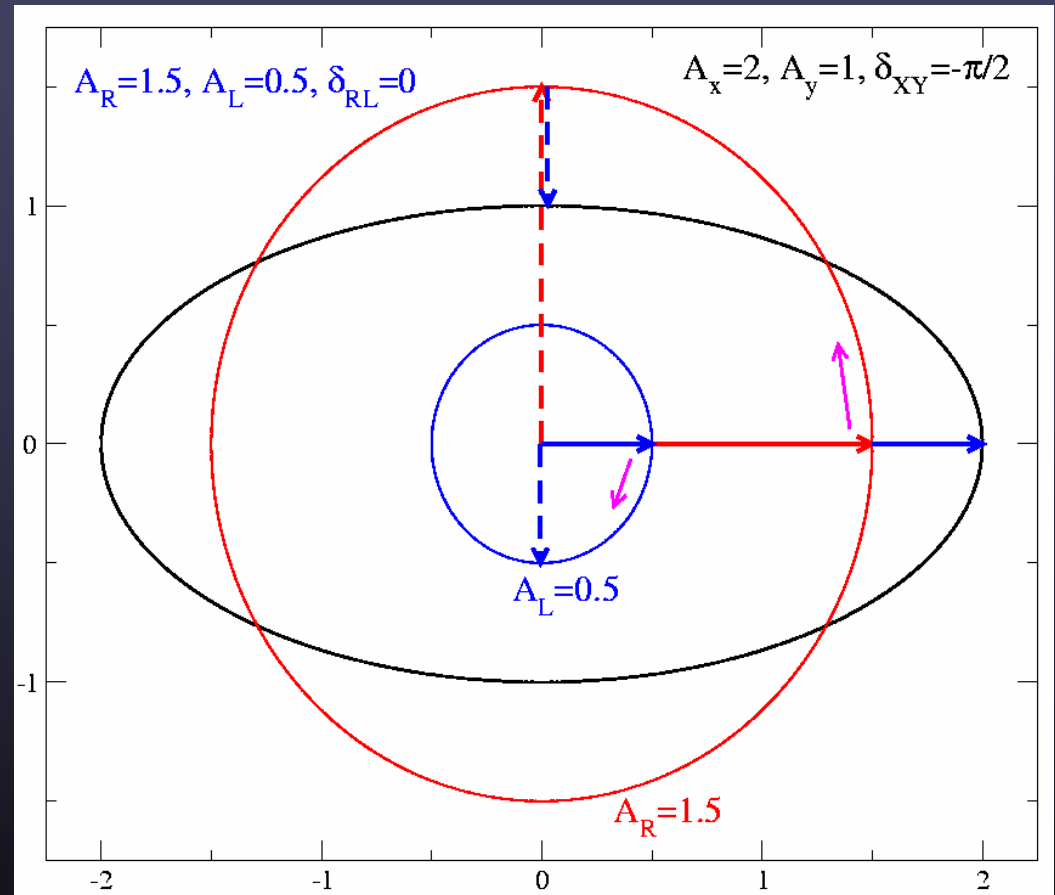


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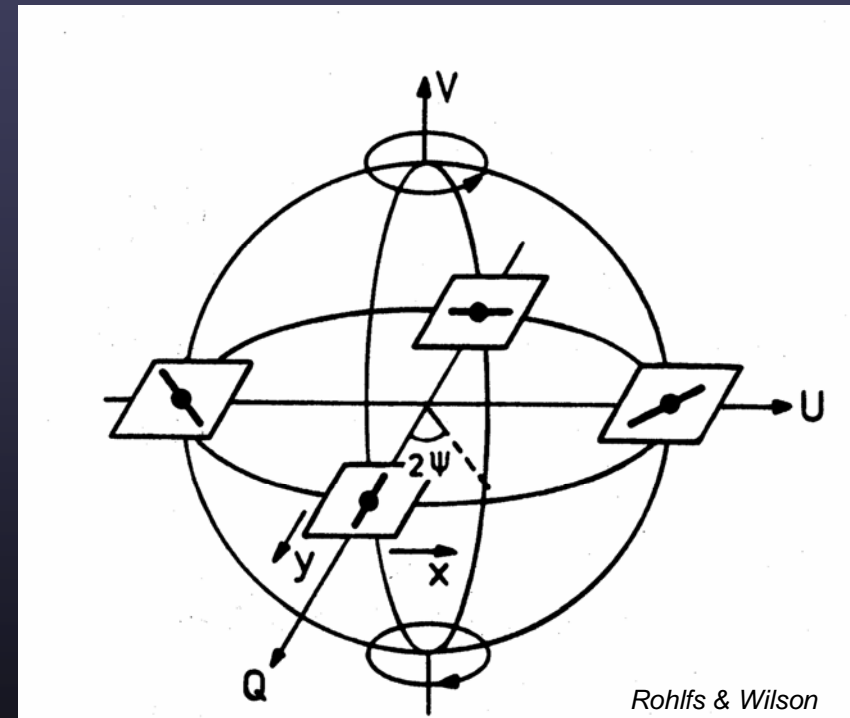
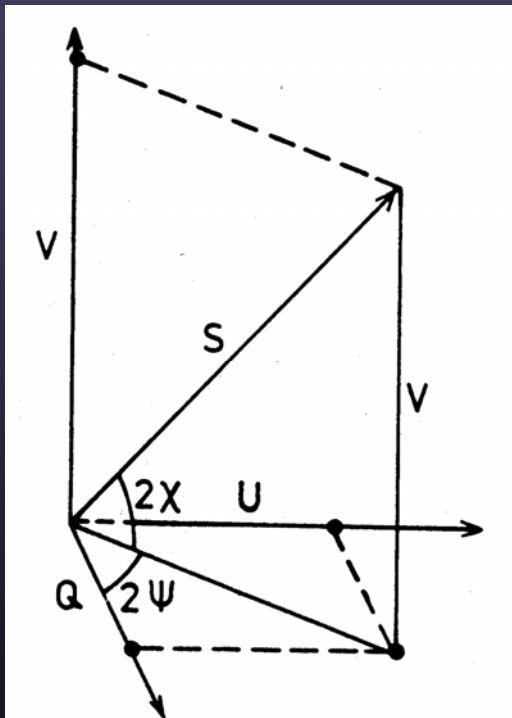
# Circular Basis Example

- The black ellipse can be decomposed into an x-component of amplitude 2, and a y-component of amplitude 1 which lags by  $\frac{1}{4}$  turn.
- It can alternatively be decomposed into a counterclockwise rotating vector of length 1.5 (red), and a clockwise rotating vector of length 0.5 (blue).



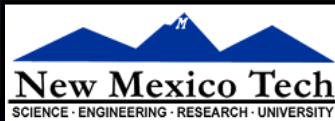
# The Poincare Sphere

- Treat  $2\psi$  and  $2\chi$  as longitude and latitude on sphere of radius  $A=E^2$



# Stokes parameters

- Spherical coordinates: radius  $I$ , axes  $Q, U, V$ 
  - $I = \sqrt{E_X^2 + E_Y^2} = \sqrt{E_R^2 + E_L^2}$
  - $Q = I \cos 2\chi \cos 2\Psi = E_X^2 - E_Y^2 = 2 E_R E_L \cos \delta_{RL}$
  - $U = I \cos 2\chi \sin 2\Psi = 2 E_X E_Y \cos \delta_{XY} = 2 E_R E_L \sin \delta_{RL}$
  - $V = I \sin 2\chi = 2 E_X E_Y \sin \delta_{XY} = E_R^2 - E_L^2$
- Only 3 independent parameters:
  - wave polarization confined to surface of Poincare sphere
  - $I^2 = Q^2 + U^2 + V^2$
- Stokes parameters  $I, Q, U, V$ 
  - defined by George Stokes (1852)
  - form complete description of wave polarization
  - NOTE: above true for 100% polarized monochromatic wave!



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# Linear Polarization

- Linearly Polarized Radiation:  $V = 0$

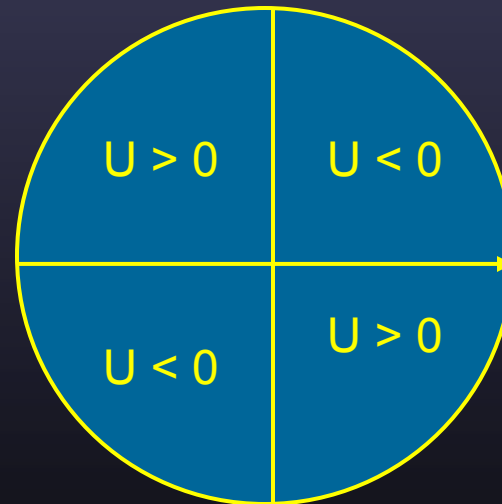
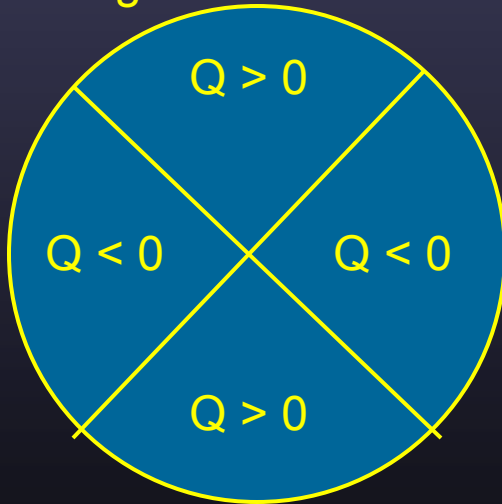
- Linearly polarized flux:

$$P = \sqrt{Q^2 + U^2}$$

- $Q$  and  $U$  define the linear polarization position angle:

$$\tan 2\psi = U / Q$$

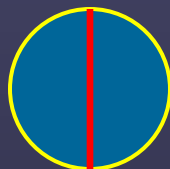
- Signs of  $Q$  and  $U$ :





# Simple Examples

- If  $V = 0$ , the wave is linearly polarized. Then,
  - If  $U = 0$ , and  $Q$  positive, then the wave is vertically polarized,  $\Psi = 0^\circ$



- If  $U = 0$ , and  $Q$  negative, the wave is horizontally polarized,  $\Psi = 90^\circ$



- If  $Q = 0$ , and  $U$  positive, the wave is polarized at  $\Psi = 45^\circ$

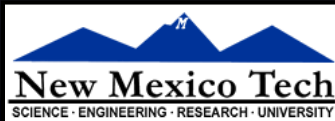
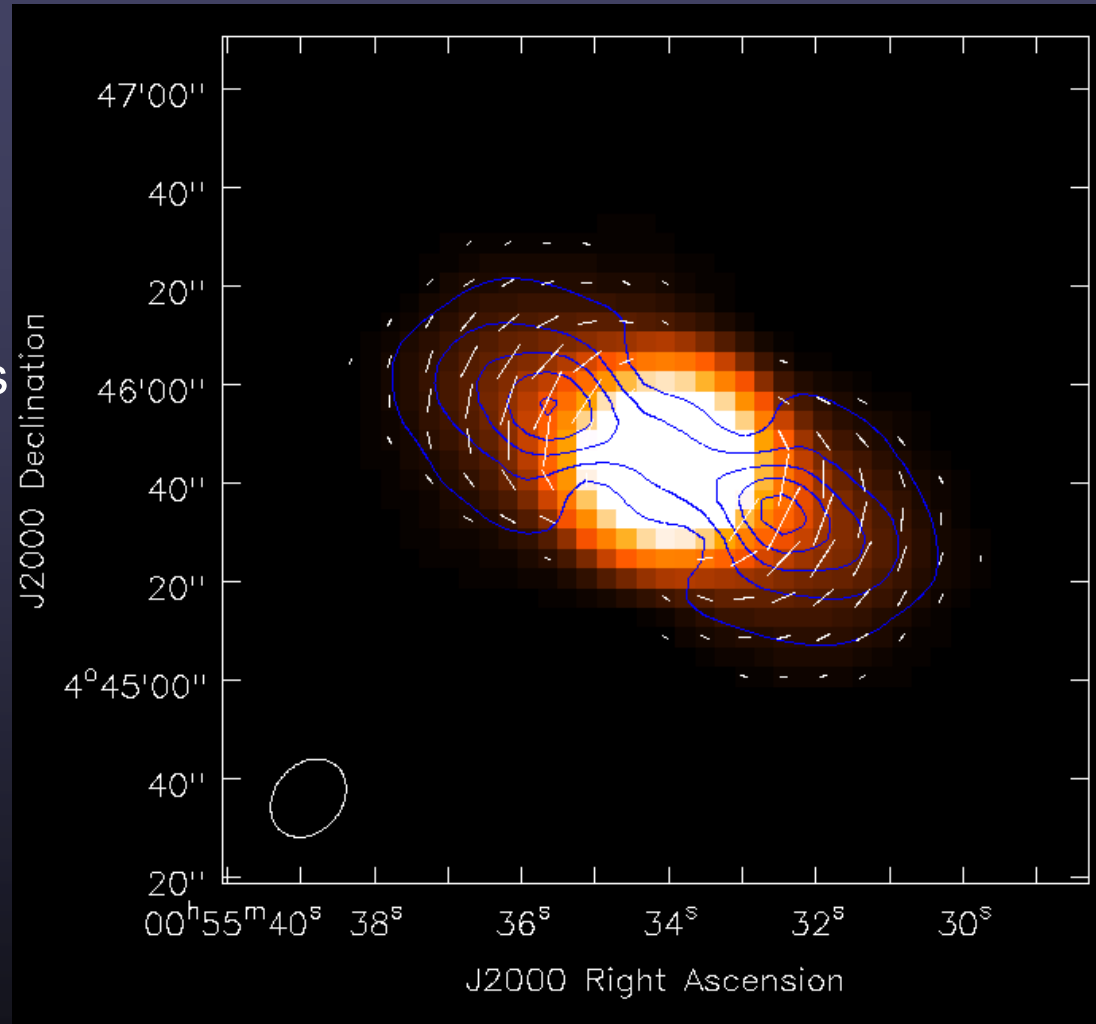


- If  $Q = 0$ , and  $U$  negative, the wave is polarized at  $\Psi = -45^\circ$ .



# Illustrative Example: Non-thermal Emission from Jupiter

- Apr 1999 VLA 5 GHz data
- D-config resolution is  $14''$
- Jupiter emits thermal radiation from atmosphere, plus polarized synchrotron radiation from particles in its magnetic field
- Shown is the I image (intensity) with polarization vectors rotated by  $90^\circ$  (to show B-vectors) and polarized intensity (blue contours)
- The polarization vectors trace Jupiter's dipole
- Polarized intensity linked to the Io plasma torus

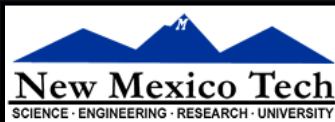


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# Why Use Stokes Parameters?

- Tradition
- They are scalar quantities, independent of basis XY, RL
- They have units of power (flux density when calibrated)
- They are simply related to actual antenna measurements.
- They easily accommodate the notion of partial polarization of non-monochromatic signals.
- We can (as I will show) make images of the I, Q, U, and V intensities directly from measurements made from an interferometer.
- These I,Q,U, and V images can then be combined to make images of the linear, circular, or elliptical characteristics of the radiation.

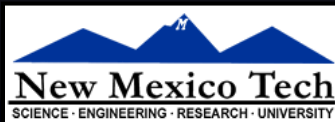


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# Non-Monochromatic Radiation, and Partial Polarization

- Monochromatic radiation is a myth.
- No such entity can exist (although it can be closely approximated).
- In real life, radiation has a finite bandwidth.
- Real astronomical emission processes arise from randomly placed, independently oscillating emitters (electrons).
- We observe the summed electric field, using instruments of finite bandwidth.
- Despite the chaos, polarization still exists, but is not complete – partial polarization is the rule.
- Stokes parameters defined in terms of mean quantities:



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# Stokes Parameters for Partial Polarization

$$I = \langle E_x^2 \rangle + \langle E_y^2 \rangle = \langle E_r^2 \rangle + \langle E_l^2 \rangle$$

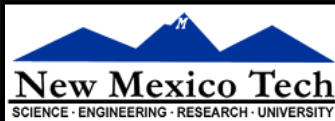
$$Q = \langle E_x^2 \rangle - \langle E_y^2 \rangle = 2\langle E_r E_l \cos \delta_{rl} \rangle$$

$$U = 2\langle E_x E_y \cos \delta_{xy} \rangle = 2\langle E_r E_l \sin \delta_{rl} \rangle$$

$$V = 2\langle E_x E_y \sin \delta_{xy} \rangle = \langle E_r^2 \rangle - \langle E_l^2 \rangle$$

Note that now, unlike monochromatic radiation, the radiation is not necessarily 100% polarized.

$$I^2 \geq Q^2 + U^2 + V^2$$

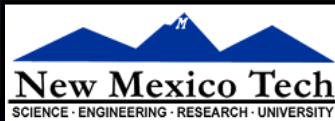


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# Summary – Fundamentals

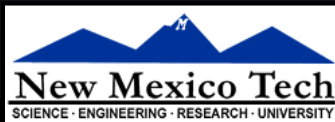
- Monochromatic waves are polarized
- Expressible as 2 orthogonal independent transverse waves
  - elliptical cross-section → polarization ellipse
  - 3 independent parameters
  - choice of basis, e.g. linear or circular
- Poincare sphere convenient representation
  - Stokes parameters I, Q, U, V
  - I intensity; Q,U linear polarization, V circular polarization
- Quasi-monochromatic “waves” in reality
  - can be partially polarized
  - still represented by Stokes parameters



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# Antenna Polarization



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# Measuring Polarization on the sky

- Coordinate system dependence:

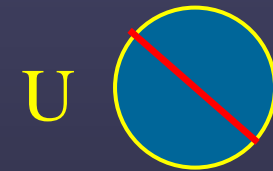
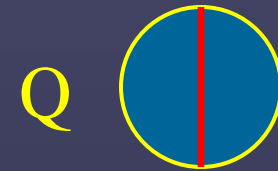
- I independent

- V depends on choice of “handedness”

- $V > 0$  for RCP

- Q,U depend on choice of “North” (plus handedness)

- Q “points” North, U 45 toward East



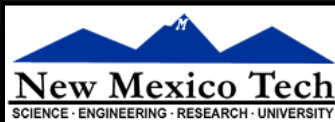
- Polarization Angle  $\Psi$

$$\Psi = \frac{1}{2} \tan^{-1} (U/Q) \quad (\text{North through East})$$

- also called the “electric vector position angle” (EVPA)

- by convention, traces E-field vector (e.g. for synchrotron)

- B-vector is perpendicular to this

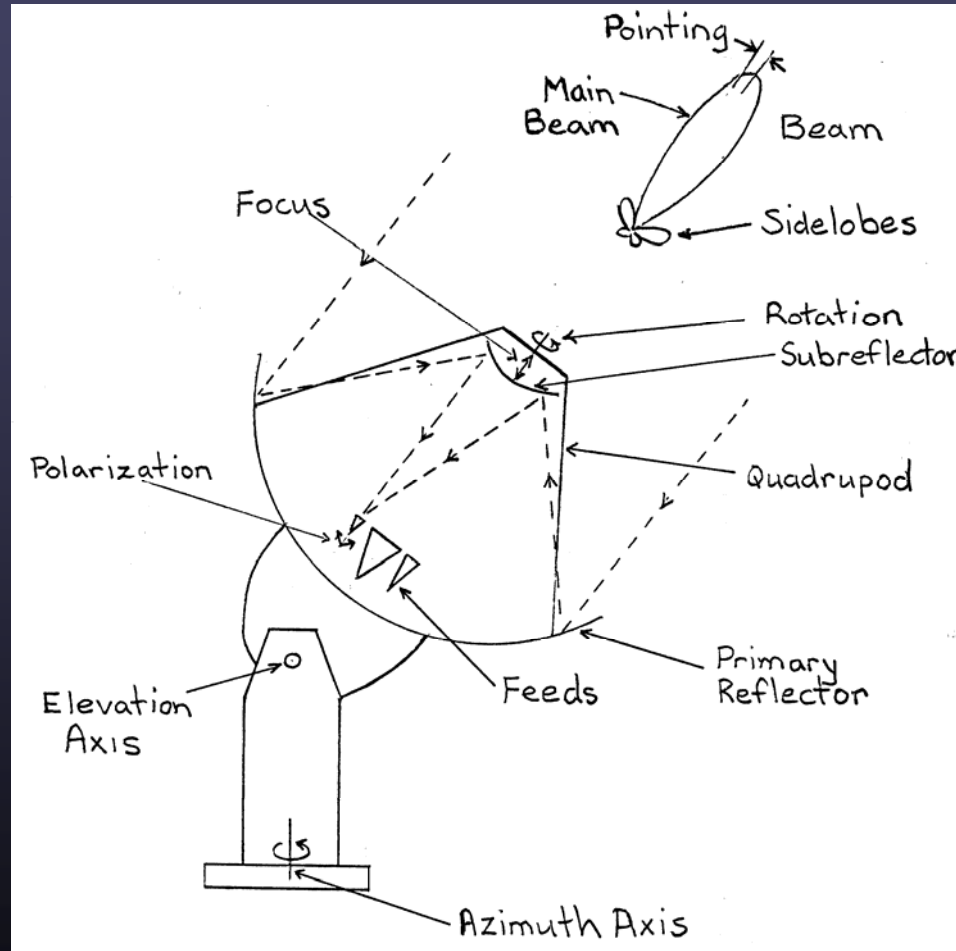


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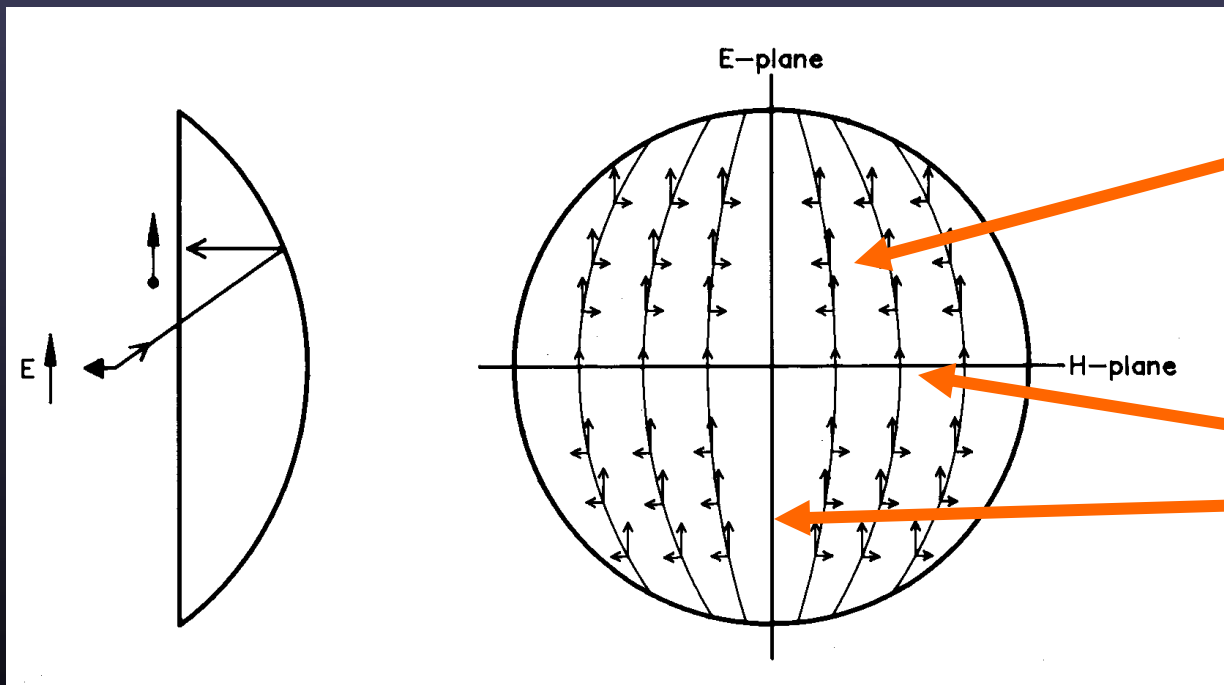
# Optics – Cassegrain radio telescope

- Paraboloid illuminated by feedhorn:



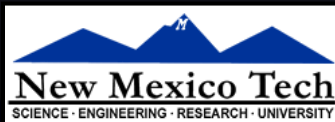
# Optics – telescope response

- Reflections
  - turn RCP  $\Leftrightarrow$  LCP
  - E-field (currents) allowed only in plane of surface
- “Field distribution” on aperture for E and H planes:



Cross-polarization  
at  $45^\circ$

No cross-polarization  
on axes

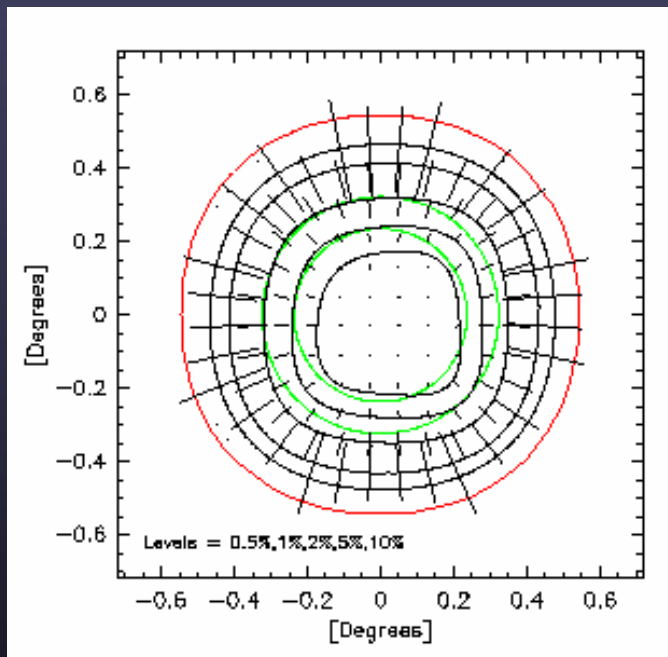


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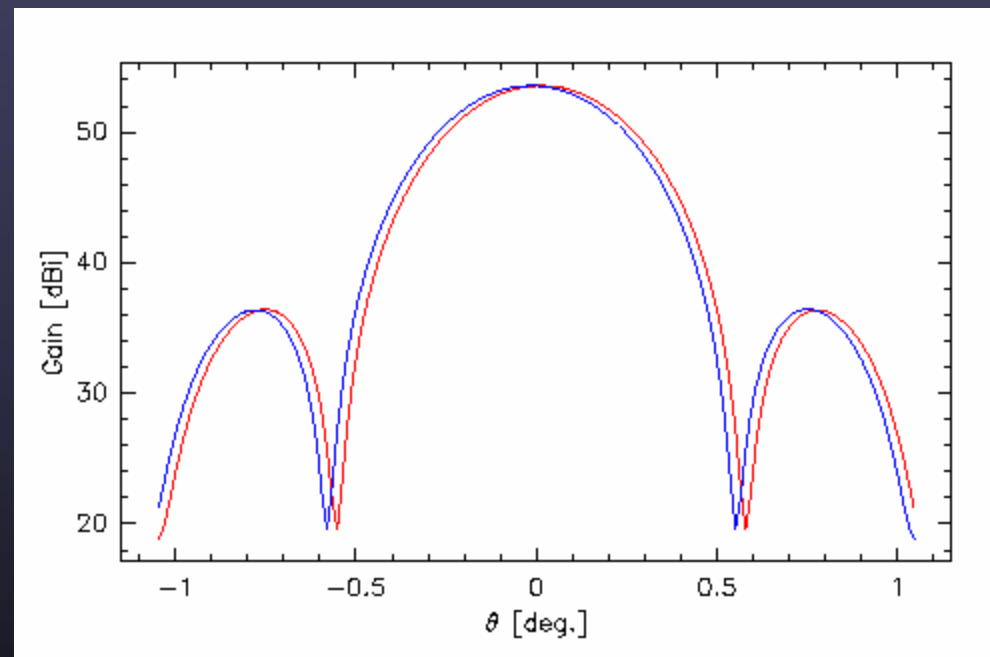


# Example – simulated VLA patterns

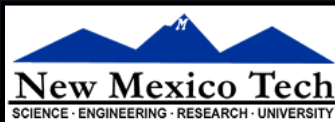
- EVLA Memo 58 “Using Grasp8 to Study the VLA Beam” W. Bricken



Linear Polarization



Circular Polarization cuts in R & L

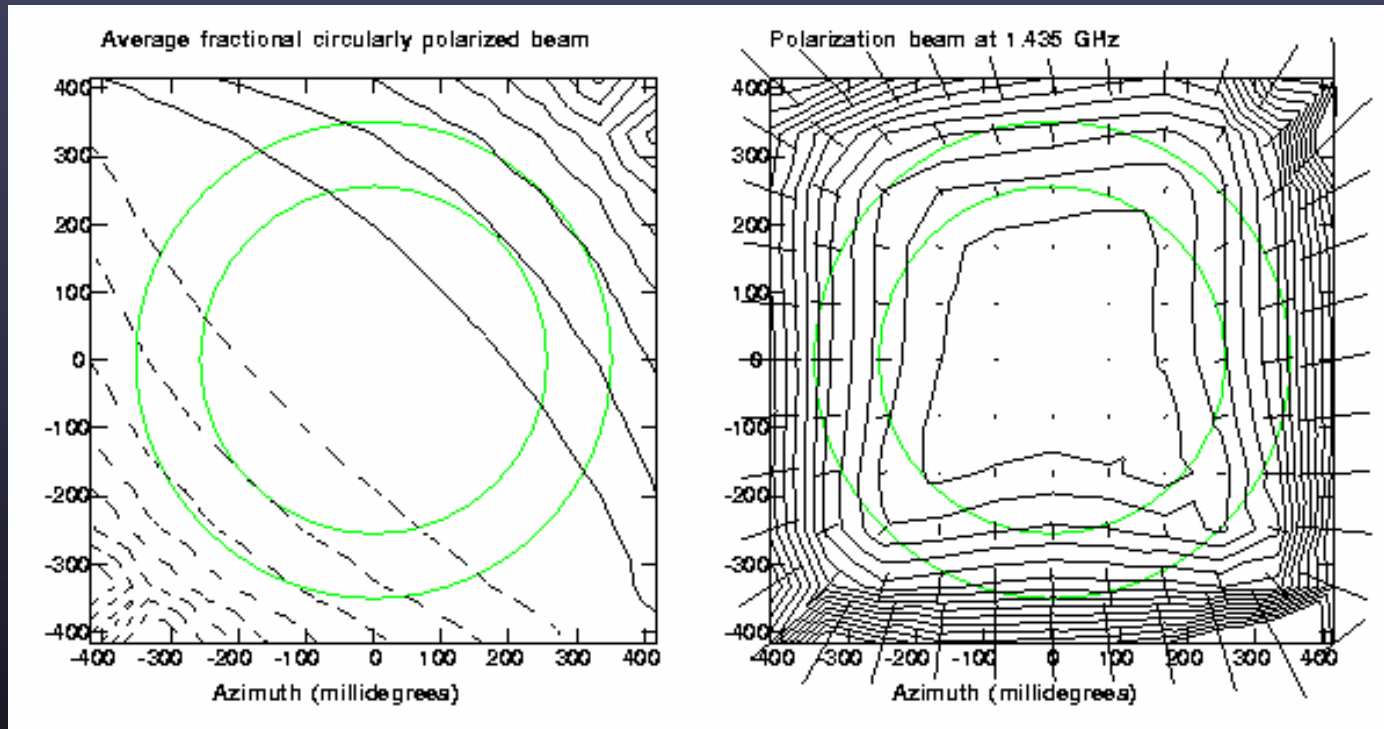


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# Example – measured VLA patterns

- AIPS Memo 86 “Widefield Polarization Correction of VLA Snapshot Images at 1.4 GHz” W. Cotton (1994)

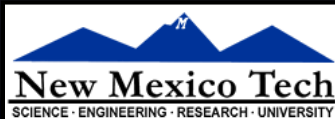


Circular Polarization

Linear Polarization

# Polarization Receiver Outputs

- To do polarimetry (measure the polarization state of the EM wave), the antenna must have two outputs which respond differently to the incoming elliptically polarized wave.
- It would be most convenient if these two outputs are proportional to either:
  - The two linear orthogonal Cartesian components,  $(E_x, E_y)$  as in ATCA and ALMA
  - The two circular orthogonal components,  $(E_R, E_L)$  as in VLA
- Sadly, this is not the case in general.
  - In general, each port is elliptically polarized, with its own polarization ellipse, with its p.a. and ellipticity.
- However, as long as these are different, polarimetry can be done.

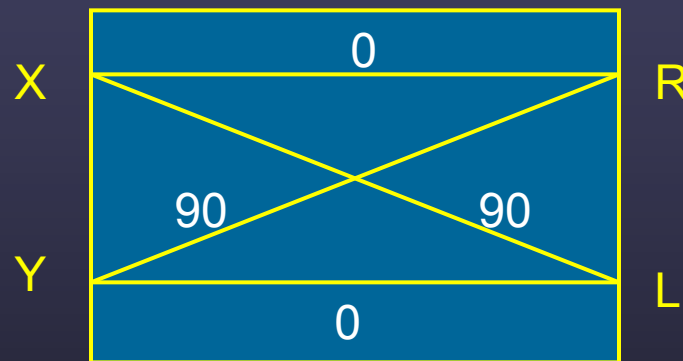


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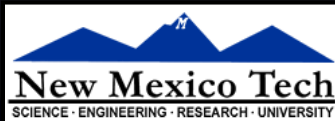
# Polarizers: Quadrature Hybrids

- We've discussed the two bases commonly used to describe polarization.
- It is quite easy to transform signals from one to the other, through a real device known as a 'quadrature hybrid'.



Four Port Device:  
2 port input  
2 ports output  
mixing matrix

- To transform correctly, the phase shifts must be exactly 0 and 90 for all frequencies, and the amplitudes balanced.
- Real hybrids are imperfect – generate errors (mixing/leaking)
- Other polarizers (e.g. waveguide septum, grids) equivalent

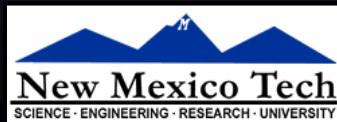


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# Polarization Interferometry

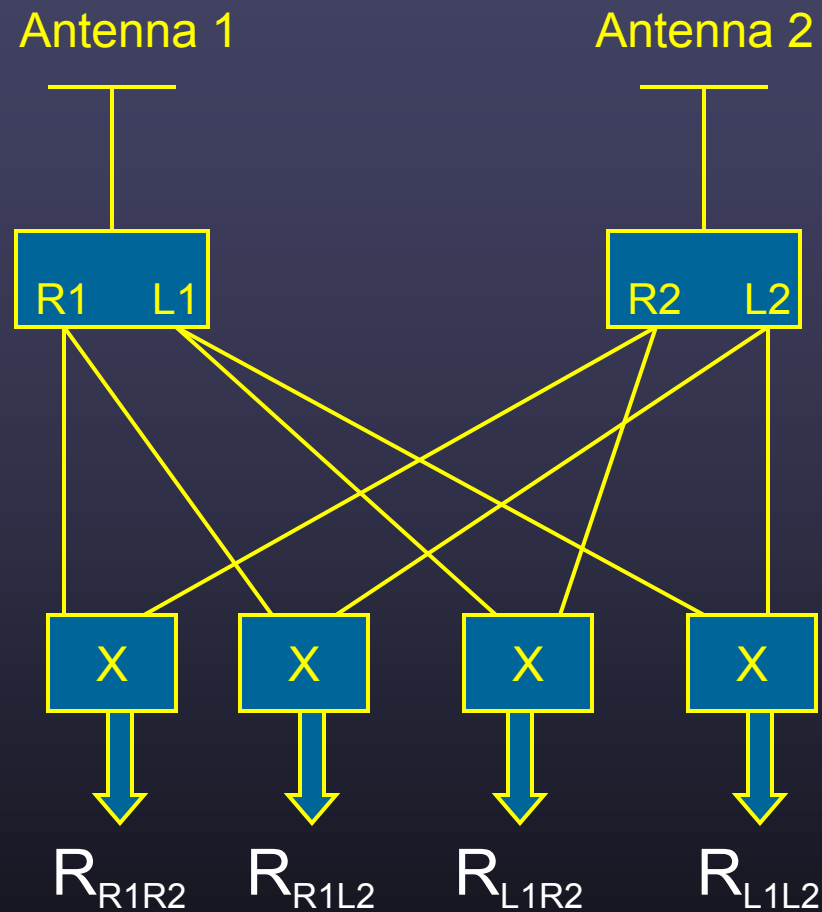


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# Four Complex Correlations per Pair

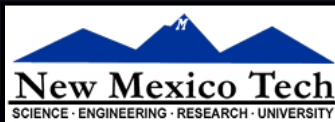
- Two antennas, each with two differently polarized outputs, produce four complex correlations.
- From these four outputs, we want to make four Stokes Images.



# Outputs: Polarization Vectors

- Each telescope receiver has two outputs
  - should be orthogonal, close to X,Y or R,L
  - even if single pol output, convenient to consider both possible polarizations (e.g. for leakage)
  - put into vector

$$\vec{E}(t) = \begin{pmatrix} E_R(t) \\ E_L(t) \end{pmatrix} \quad \text{or} \quad \vec{E}(t) = \begin{pmatrix} E_X(t) \\ E_Y(t) \end{pmatrix}$$



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# Correlation products: coherency vector

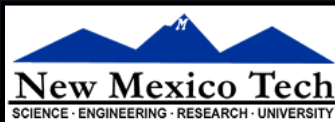
- Coherency vector: outer product of 2 antenna vectors as averaged by correlator

$$\vec{v}_{ij} = \left\langle \vec{E}_i \otimes \vec{E}_j^* \right\rangle = \left\langle \begin{pmatrix} E^p \\ E^q \end{pmatrix}_i \otimes \begin{pmatrix} E^p \\ E^q \end{pmatrix}_j^* \right\rangle = \begin{pmatrix} \left\langle E_i^p \cdot E_j^{*p} \right\rangle \\ \left\langle E_i^p \cdot E_j^{*q} \right\rangle \\ \left\langle E_i^q \cdot E_j^{*p} \right\rangle \\ \left\langle E_i^q \cdot E_j^{*q} \right\rangle \end{pmatrix} = \begin{pmatrix} v^{pp} \\ v^{pq} \\ v^{qp} \\ v^{qq} \end{pmatrix}_{ij}$$

– these are essentially the uncalibrated *visibilities*  $\mathbf{v}$

- circular products RR, RL, LR, LL
- linear products XX, XY, YX, YY

– need to include corruptions before and after correlation



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# Polarization Products: General Case

$$v^{pq} = \frac{1}{2} G_{pq} \{ I [\cos(\Psi_p - \Psi_q) \cos(\chi_p - \chi_q) + i \sin(\Psi_p - \Psi_q) \sin(\chi_p + \chi_q)] \\ + Q [\cos(\Psi_p + \Psi_q) \cos(\chi_p + \chi_q) + i \sin(\Psi_p + \Psi_q) \sin(\chi_p - \chi_q)] \\ - i U [\cos(\Psi_p + \Psi_q) \sin(\chi_p - \chi_q) + i \sin(\Psi_p + \Psi_q) \cos(\chi_p + \chi_q)] \\ - V [\cos(\Psi_p - \Psi_q) \sin(\chi_p + \chi_q) + i \sin(\Psi_p - \Psi_q) \cos(\chi_p - \chi_q)] \}$$

What are all these symbols?

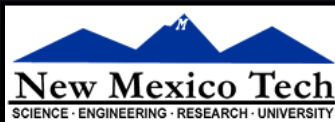
$v^{pq}$  is the complex output from the interferometer, for polarizations p and q from antennas 1 and 2, respectively.

$\Psi$  and  $\chi$  are the antenna polarization major axis and ellipticity for states p and q.

I, Q, U, and V are the **Stokes Visibilities** describing the polarization state of the astronomical signal.

G is the gain, which falls out in calibration.

**WE WILL ABSORB FACTOR 1/2 INTO GAIN!!!!!!!**



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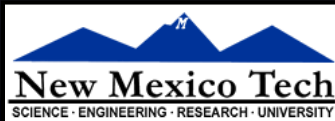
# Coherency vector and Stokes vector

- Maps (perfect) visibilities to the Stokes vector  $\mathbf{s}$
- Example: circular polarization (e.g. VLA)

$$\vec{v}_{circ} = \mathbf{S}_{circ} \vec{S} = \begin{pmatrix} v^{RR} \\ v^{RL} \\ v^{LR} \\ v^{LL} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & i & 0 \\ 0 & 1 & -i & 0 \\ 1 & 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} = \begin{pmatrix} I+V \\ Q+iU \\ Q-iU \\ I-V \end{pmatrix}$$

- Example: linear polarization (e.g. ALMA, ATCA)

$$\vec{v}_{lin} = \mathbf{S}_{lin} \vec{S} = \begin{pmatrix} v^{XX} \\ v^{XY} \\ v^{YX} \\ v^{YY} \end{pmatrix} = \begin{pmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & i \\ 0 & 0 & 1 & -i \\ 1 & -1 & 0 & 0 \end{pmatrix} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} = \begin{pmatrix} I+Q \\ U+iV \\ U-iV \\ I-Q \end{pmatrix}$$



# Corruptions: Jones Matrices

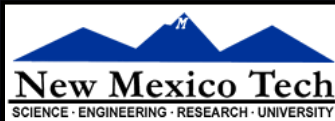
- Antenna-based corruptions
  - pre-correlation polarization-dependent effects act as a matrix multiplication. This is the Jones matrix:

$$\vec{E}^{\text{out}} = \mathbf{J} \vec{E}^{\text{in}} \quad \mathbf{J} = \begin{pmatrix} J_{11} & J_{12} \\ J_{21} & J_{22} \end{pmatrix} \quad \vec{E} = \begin{pmatrix} E_1 \\ E_2 \end{pmatrix}$$

- form of  $\mathbf{J}$  depends on basis (RL or XY) and effect
  - off-diagonal terms  $J_{12}$  and  $J_{21}$  cause corruption (mixing)
- total  $\mathbf{J}$  is a string of Jones matrices for each effect

$$\mathbf{J} = \mathbf{J}_F \mathbf{J}_E \mathbf{J}_D \mathbf{J}_P$$

- Faraday, polarized beam, leakage, parallactic angle



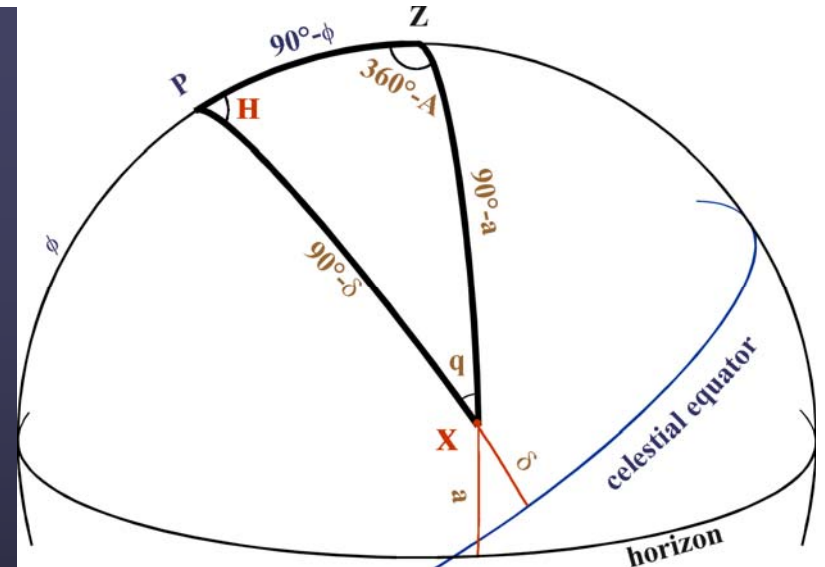
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# Parallactic Angle, $P$

- Orientation of sky in telescope's field of view
  - Constant for equatorial telescopes
  - Varies for alt-az telescopes
  - Rotates the position angle of linearly polarized radiation (R-L phase)

$$\mathbf{J}_P^{RL} = \begin{pmatrix} e^{i\phi} & 0 \\ 0 & e^{-i\phi} \end{pmatrix}; \quad \mathbf{J}_P^{XY} = \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix}$$

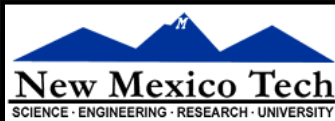


- defined per antenna (often same over array)

$$\phi(t) = \arctan \left( \frac{\cos(l) \sin(h(t))}{\sin(l) \cos(\delta) - \cos(l) \sin(\delta) \cos(h(t))} \right)$$

$l$  = latitude,  $h(t)$  = hour angle,  $\delta$  = declination

- $P$  modulation can be used to aid in calibration



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## Visibilities to Stokes on-sky: RL basis

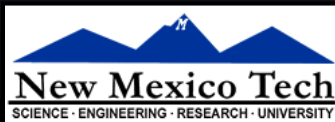
- the (outer) products of the parallactic angle (P) and the Stokes matrices gives

$$\vec{v} = \mathbf{J}_P \mathbf{S} \vec{s}$$

- this matrix maps a sky Stokes vector to the coherence vector representing the four perfect (circular) polarization products:

$$\begin{pmatrix} v^{RR} \\ v^{RL} \\ v^{LR} \\ v^{LL} \end{pmatrix} = \begin{pmatrix} e^{-i(\phi_i - \phi_j)} & 0 & 0 & e^{-i(\phi_i - \phi_j)} \\ 0 & e^{-i(\phi_i + \phi_j)} & ie^{-i(\phi_i + \phi_j)} & 0 \\ 0 & e^{i(\phi_i + \phi_j)} & -ie^{i(\phi_i + \phi_j)} & 0 \\ e^{i(\phi_i - \phi_j)} & 0 & 0 & -e^{i(\phi_i - \phi_j)} \end{pmatrix} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} \xrightarrow{\phi_i = \phi_j = \phi} \begin{pmatrix} I + V \\ (Q + iU)e^{-i2\phi} \\ (Q - iU)e^{i2\phi} \\ I - V \end{pmatrix}$$

Circular Feeds: linear polarization in cross hands, circular in parallel-hands



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# Visibilities to Stokes on-sky: XY basis

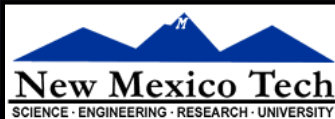
- we have

$$\begin{pmatrix} v^{XX} \\ v^{XY} \\ v^{YX} \\ v^{YY} \end{pmatrix} = \begin{pmatrix} \cos(\phi_i - \phi_j) & \cos(\phi_i + \phi_j) & -\sin(\phi_i + \phi_j) & i \sin(\phi_i - \phi_j) \\ -\sin(\phi_i - \phi_j) & \sin(\phi_i + \phi_j) & \cos(\phi_i + \phi_j) & i \cos(\phi_i - \phi_j) \\ \sin(\phi_i - \phi_j) & \sin(\phi_i + \phi_j) & \cos(\phi_i + \phi_j) & -i \cos(\phi_i - \phi_j) \\ \cos(\phi_i - \phi_j) & -\cos(\phi_i + \phi_j) & -\sin(\phi_i + \phi_j) & i \sin(\phi_i - \phi_j) \end{pmatrix} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix}$$

- and for identical parallactic angles  $\phi$  between antennas:

$$\begin{pmatrix} v^{XX} \\ v^{XY} \\ v^{YX} \\ v^{YY} \end{pmatrix} \xrightarrow{\phi_i = \phi_j = \phi} \begin{pmatrix} I + Q \cos 2\phi - U \sin 2\phi \\ Q \sin 2\phi + U \cos 2\phi + iV \\ Q \sin 2\phi + U \cos 2\phi - iV \\ I - Q \cos 2\phi + U \sin 2\phi \end{pmatrix}$$

Linear Feeds:  
linear polarization  
in all hands, circular  
only in cross-hands



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# Basic Interferometry equations

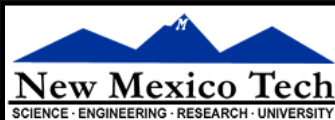
- An interferometer naturally measures the transform of the sky intensity in  $uv$ -space convolved with aperture
  - cross-correlation of aperture voltage patterns in  $uv$ -plane
  - its transform on sky is the primary beam  $\mathbf{A}$  with FWHM  $\sim \lambda/D$

$$\begin{aligned} V(\mathbf{u}) &= \int d^2\mathbf{x} A(\mathbf{x} - \mathbf{x}_p) I(\mathbf{x}) e^{-2\pi i \mathbf{u} \cdot (\mathbf{x} - \mathbf{x}_p)} + \mathbf{n} \\ &= \int d^2\mathbf{v} \tilde{A}(\mathbf{u} - \mathbf{v}) \tilde{I}(\mathbf{v}) e^{2\pi i \mathbf{v} \cdot \mathbf{x}_p} + \mathbf{n} \end{aligned}$$

- The “tilde” quantities are Fourier transforms, with convention:

$$\tilde{T}(\mathbf{u}) = \int d^2\mathbf{x} e^{-i2\pi\mathbf{u}\cdot\mathbf{x}} T(\mathbf{x}) \quad \mathbf{x} = (l, m) \leftrightarrow \mathbf{u} = (u, v)$$

$$T(\mathbf{x}) = \int d^2\mathbf{u} e^{i2\pi\mathbf{u}\cdot\mathbf{x}} \tilde{T}(\mathbf{u})$$



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# Polarization Interferometry : Q & U

- Parallel-hand & Cross-hand correlations (circular basis)
  - visibility  $k$  (antenna pair  $ij$ , time, pointing  $x$ , channel  $v$ , noise  $n$ ):

$$V_k^{RR}(\mathbf{u}_k) = \int d^2\mathbf{v} \tilde{A}_k^{RR}(\mathbf{u}_k - \mathbf{v}) [\tilde{I}_v(\mathbf{v}) + \tilde{V}_v(\mathbf{v})] e^{2\pi i \mathbf{v} \cdot \mathbf{x}_k} + \mathbf{n}_k^{RR}$$

$$V_k^{RL}(\mathbf{u}_k) = \int d^2\mathbf{v} \tilde{A}_k^{RL}(\mathbf{u}_k - \mathbf{v}) [\tilde{Q}_v(\mathbf{v}) + i\tilde{U}_v(\mathbf{v})] e^{-i2\phi_k} e^{2\pi i \mathbf{v} \cdot \mathbf{x}_k} + \mathbf{n}_k^{RL}$$

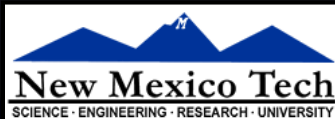
$$V_k^{LR}(\mathbf{u}_k) = \int d^2\mathbf{v} \tilde{A}_k^{LR}(\mathbf{u}_k - \mathbf{v}) [\tilde{Q}_v(\mathbf{v}) - i\tilde{U}_v(\mathbf{v})] e^{i2\phi_k} e^{2\pi i \mathbf{v} \cdot \mathbf{x}_k} + \mathbf{n}_k^{LR}$$

$$V_k^{LL}(\mathbf{u}_k) = \int d^2\mathbf{v} \tilde{A}_k^{LL}(\mathbf{u}_k - \mathbf{v}) [\tilde{I}_v(\mathbf{v}) - \tilde{V}_v(\mathbf{v})] e^{2\pi i \mathbf{v} \cdot \mathbf{x}_k} + \mathbf{n}_k^{LL}$$

- where kernel  $A$  is the aperture cross-correlation function,  $\phi$  is the parallactic angle, and  $\mathbf{Q} + i\mathbf{U} = \mathbf{P}$  is the complex linear polarization

$$\tilde{\mathbf{P}}(\mathbf{v}) = \tilde{\mathbf{Q}}(\mathbf{v}) + i\tilde{\mathbf{U}}(\mathbf{v}) = |\tilde{\mathbf{P}}(\mathbf{v})| e^{i2\phi(\mathbf{v})}$$

- the phase of  $\mathbf{P}$  is  $\phi$  (the R-L phase difference)

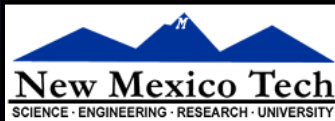


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# Example: RL basis imaging

- Parenthetical Note:
  - can make a pseudo-I image by gridding RR+LL on the Fourier half-plane and inverting to a real image
  - can make a pseudo-V image by gridding RR-LL on the Fourier half-plane and inverting to real image
  - can make a pseudo-(Q+iU) image by gridding RL to the full Fourier plane (with LR as the conjugate) and inverting to a complex image
  - does not require having full polarization RR,RL,LR,LL for every visibility
- More on imaging ( & deconvolution ) tomorrow!



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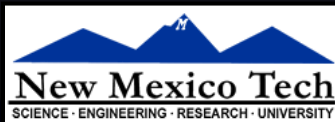


# Polarization Leakage, $D$

- Polarizer is not ideal, so orthogonal polarizations not perfectly isolated
  - Well-designed systems have  $d < 1-5\%$  (but some systems  $>10\%$  ☹ )
  - A geometric property of the antenna, feed & polarizer design
    - frequency dependent (e.g. quarter-wave at center  $\nu$ )
    - direction dependent (in beam) due to antenna
  - For  $R,L$  systems
    - parallel hands affected as  $d \cdot Q + d \cdot U$  , so only important at high dynamic range (because  $Q, U \sim d$ , typically)
    - cross-hands affected as  $d \cdot I$  so almost always important

$$\mathbf{J}_D^{pq} = \begin{pmatrix} 1 & d^p \\ d^q & 1 \end{pmatrix}$$

Leakage of  $q$  into  $p$   
(e.g. L into R)



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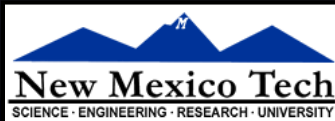


# Leakage revisited...

- Primary on-axis effect is “leakage” of one polarization into the measurement of the other (e.g.  $R \Leftrightarrow L$ )
  - but, direction dependence due to polarization beam!
- Customary to factor out on-axis leakage into D and put direction dependence in “beam”
  - example: expand RL basis with on-axis leakage

$$\hat{V}_{ij}^{RR} = V_{ij}^{RR} + d_i^R V_{ij}^{LR} + d_j^{*R} V_{ij}^{RL} + d_i^R d_j^{*R} V_{ij}^{LL}$$
$$\hat{V}_{ij}^{RL} = V_{ij}^{RL} + d_i^R V_{ij}^{LL} + d_j^{*L} V_{ij}^{RR} + d_i^R d_j^L V_{ij}^{LR}$$

– similarly for XY basis



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# Example: RL basis leakage

- In full detail:

$$\begin{aligned}
 V_{ij}^{RR} &= \int_{sky} E_{ij}^{RR}(l, m) [(I + V)e^{i(\chi_i - \chi_j)} \\
 &\quad + d_i^R e^{-i(\chi_i + \chi_j)} (Q - iU) + d_j^{*R} e^{i(\chi_i + \chi_j)} (Q + iU) \\
 &\quad + \cancel{d_i^R d_j^{*R} e^{-i(\chi_i - \chi_i)} (I - V)}](l, m) e^{-i2\pi(u_{ij}l + v_{ij}m)} dldm \\
 V_{ij}^{RL} &= \int_{sky} E_{ij}^{RL}(l, m) [(Q + iU)e^{i(\chi_i + \chi_j)} \\
 &\quad + d_i^R (I - V)e^{-i(\chi_i - \chi_j)} + d_j^{*L} (I + V)e^{i(\chi_i - \chi_j)} \\
 &\quad + \cancel{d_i^R d_j^{*L} (Q - iU) e^{-i(\chi_i + \chi_j)}}](l, m) e^{-i2\pi(u_{ij}l + v_{ij}m)} dldm
 \end{aligned}$$

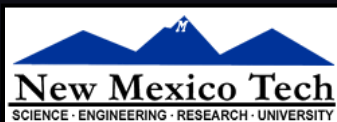
"true" signal

2<sup>nd</sup> order:  
D•P into I

2<sup>nd</sup> order:  
D<sup>2</sup>•I into I

1<sup>st</sup> order:  
D•I into P

3<sup>rd</sup> order:  
D<sup>2</sup>•P\* into P



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# Example: linearized leakage

- RL basis, keeping only terms linear in I, Q±iU, d:

$$V_{ij}^{RL} = (Q + iU)e^{-i(\phi_i + \phi_j)} + I(d_i^R e^{i(\phi_i - \phi_j)} + d_j^{*L} e^{-i(\phi_i - \phi_j)})$$

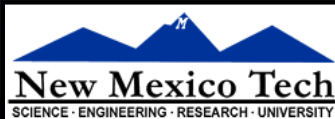
$$V_{ij}^{LR} = (Q - iU)e^{i(\phi_i + \phi_j)} - I(d_i^L e^{-i(\phi_i - \phi_j)} + d_j^{*R} e^{i(\phi_i - \phi_j)})$$

- Likewise for XY basis, keeping linear in I, Q, U, V, d, sin(φ<sub>i</sub>-φ<sub>j</sub>)

$$V_{ij}^{XY} = Q\sin(\phi_i + \phi_j) + U\cos(\phi_i + \phi_j) + iV + [(d_i^X + d_j^{*Y})\cos(\phi_i - \phi_j) - \sin(\phi_i - \phi_j)]I$$

$$V_{ij}^{YX} = Q\sin(\phi_i + \phi_j) + U\cos(\phi_i + \phi_j) + iV + [(d_i^Y + d_j^{*X})\cos(\phi_i - \phi_j) + \sin(\phi_i - \phi_j)]I$$

**WARNING: Using linear order will limit dynamic range!**



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# Ionospheric Faraday Rotation, $F$

- Birefringency due to magnetic field in ionospheric plasma

$$\mathbf{J}_F^{RL} = \begin{pmatrix} e^{i\Delta\phi} & 0 \\ 0 & e^{-i\Delta\phi} \end{pmatrix}$$

$$\mathbf{J}_F^{XY} = \begin{pmatrix} \cos \Delta\phi & -\sin \Delta\phi \\ \sin \Delta\phi & \cos \Delta\phi \end{pmatrix}$$

is direction-dependent

$$\Delta\phi \approx 0.15^\circ \lambda^2 \int B_{\parallel} n_e ds$$

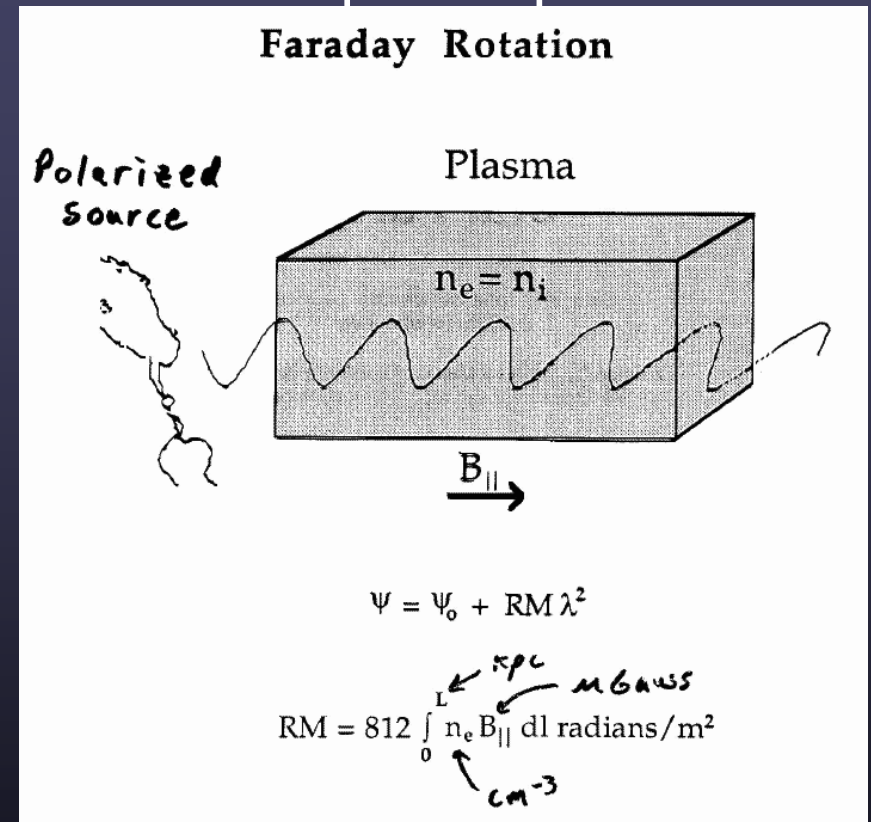
( $\lambda$  in cm,  $n_e ds$  in  $10^{14} \text{ cm}^{-2}$ ,  $B_{\parallel}$  in G)

$$TEC = \int n_e ds \sim 10^{14} \text{ cm}^{-2}; \quad B_{\parallel} \sim 1\text{G};$$

$$\lambda = 20\text{cm} \rightarrow \Delta\phi \sim 60^\circ$$

– also present in ISM, IGM and intrinsic to radio sources!

- can come from different Faraday depths  $\rightarrow$  tomography

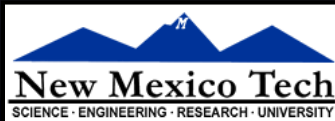


# Antenna voltage pattern, $E$

- Direction-dependent gain and polarization
  - includes primary beam
    - Fourier transform of cross-correlation of antenna voltage patterns
    - includes polarization asymmetry (squint)

$$\mathbf{J}_E^{pq} = \begin{pmatrix} e^{pp}(l', m') & e^{pq}(l', m') \\ e^{qp}(l', m') & e^{qq}(l', m') \end{pmatrix}$$

- includes off-axis cross-polarization (leakage)
  - convenient to reserve  $D$  for on-axis leakage
- important in wide-field imaging and mosaicing
  - when sources fill the beam (e.g. low frequency)

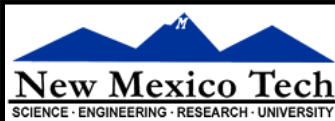


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# Summary – polarization interferometry

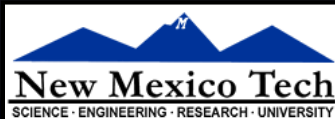
- Choice of basis: CP or LP feeds
  - usually a technology consideration
- Follow the signal path
  - ionospheric Faraday rotation  $F$  at low frequency
    - direction dependent (and antenna dependent for long baselines)
  - parallactic angle  $P$  for coordinate transformation to Stokes
    - antennas can have differing PA (e.g. VLBI)
  - “leakage”  $D$  varies with  $\nu$  and over beam (mix with  $E$ )
- Leakage
  - use full (all orders)  $D$  solver when possible
  - linear approximation OK for low dynamic range
  - beware when antennas have different parallactic angles



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# Polarization Calibration & Observation



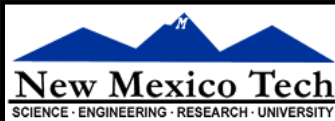
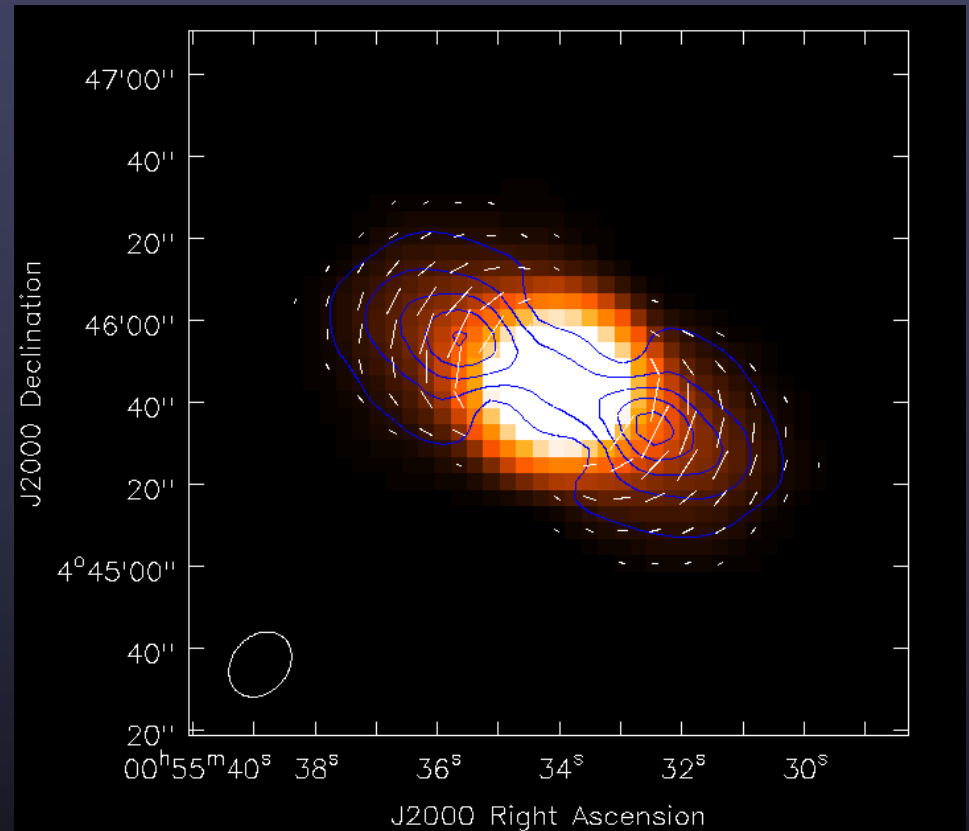
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# So you want to make a polarization image...

- Making polarization images
  - follow general rules for imaging
  - image & deconvolve I, Q, U, V planes
  - Q, U, V will be positive and negative
  - V image can often be used as check
- Polarization vector plots
  - EVPA calibrator to set angle (e.g. R-L phase difference)
    - $\Phi = \frac{1}{2} \tan^{-1} U/Q$  for E vectors
  - B vectors  $\perp$  E
  - plot E vectors (length given by P)
- Leakage calibration is essential
- See Tutorials on Friday

e.g Jupiter 6cm continuum

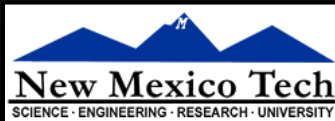


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# Strategies for leakage calibration

- Need a bright calibrator! Effects are low level...
  - determine antenna gains independently (mostly from parallel hands)
  - use cross-hands (mostly) to determine leakage
  - do matrix solution to go beyond linear order
- Calibrator is unpolarized
  - leakage directly determined (ratio to  $I$  model), but only to an overall complex constant (additive over array)
  - need way to fix phase  $\delta_p - \delta_q$  (*ie.* R-L phase difference), e.g. using another calibrator with known EVPA
- Calibrator of known (non-zero) linear polarization
  - leakage can be directly determined (for  $I, Q, U, V$  model)
  - unknown  $p-q$  phase can be determined (from  $U/Q$  etc.)

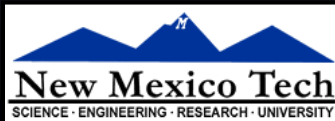


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# Other strategies

- Calibrator of unknown polarization
  - solve for model  $IQUV$  and  $D$  simultaneously or iteratively
  - need good parallactic angle coverage to modulate sky and instrumental signals
    - in instrument basis, sky signal modulated by  $e^{i2\chi}$
- With a very bright strongly polarized calibrator
  - can solve for leakages and polarization per baseline
  - can solve for leakages using parallel hands!
- With no calibrator
  - hope it averages down over parallactic angle
  - transfer  $D$  from a similar observation
    - usually possible for several days, better than nothing!
    - need observations at same frequency



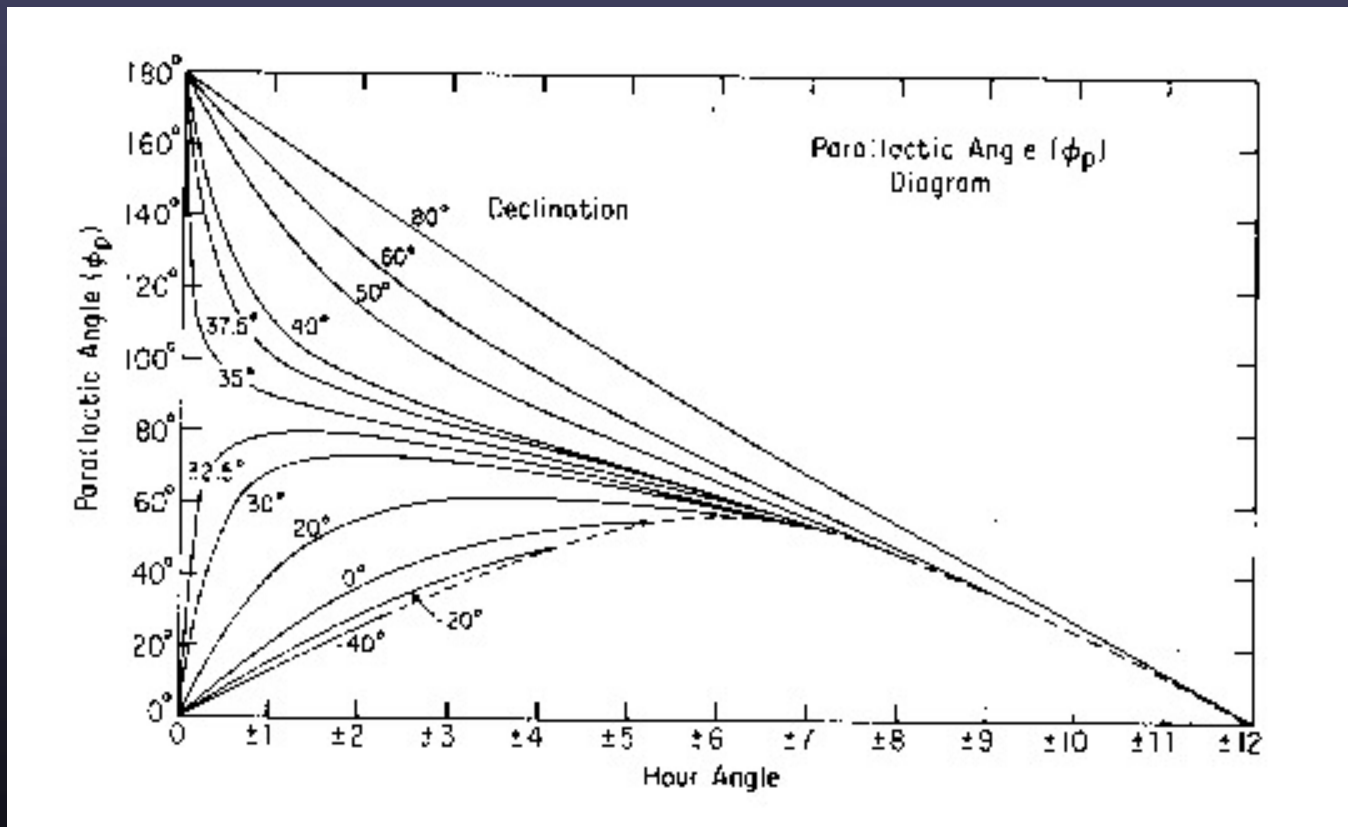
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# Parallactic Angle Coverage at VLA

- fastest PA swing for source passing through zenith
  - to get good PA coverage in a few hours, need calibrators between declination  $+20^\circ$  and  $+60^\circ$



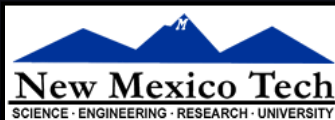
# Finding polarization calibrators

- Standard sources
  - planets (unpolarized if unresolved)
  - 3C286, 3C48, 3C147 (known IQU, stable)
  - sources monitored (e.g. by VLA)
  - other bright sources (bootstrap)

<http://www.vla.nrao.edu/astro/calib/polar/>

The screenshot shows the VLA/VLBA Polarization Calibration Page, which is a table of calibration sources. The table is organized into sections for different frequency bands: 2202+422 C BAND and 2253+161 C BAND. Each row represents a source, with columns for source name, polarization type (A, B, D), observation ID, and various polarization parameters (e.g.,  $10.129 \pm 0.021$ ,  $10124.86 \pm 13.68$ , etc.). The table is displayed in a web browser window.

Source	Type	Obs ID	Parameter 1	Parameter 2	Parameter 3	Parameter 4	Parameter 5	Parameter 6
2136+006	B	20031205	$10.003 \pm 0.014$	$10005.95 \pm 6.25$	$138.21 \pm 0.52$	$1.39 \pm 0.01$	$-154.90 \pm 0.15$	$0.859 \pm 0.001$
2136+006	B	20031219	$10.129 \pm 0.021$	$10124.86 \pm 13.68$	$102.56 \pm 1.52$	$1.01 \pm 0.02$	$-161.12 \pm 2.38$	$0.8791 \pm 0.001$
2136+006	MEAN	all	$10.122 \pm 0.113$	$10120.24 \pm 112.97$	$119.32 \pm 11.78$	$1.18 \pm 0.12$	$-155.36 \pm 5.36$	$0.8747 \pm 0.001$
<b>2202+422 C BAND</b>								
2202+422	D	20030206	$2.269 \pm 0.002$	$2268.28 \pm 8.43$	$125.50 \pm 1.22$	$5.53 \pm 0.03$	$-17.99 \pm 0.98$	$2.094 \pm 0.001$
2202+422	D	20030308	$2.044 \pm 0.002$	$2042.52 \pm 1.27$	$117.19 \pm 0.10$	$5.74 \pm 0.00$	$-21.31 \pm 1.22$	$0.000 \pm 0.001$
2202+422	D	20030419	$2.122 \pm 0.004$	$2120.92 \pm 10.57$	$99.93 \pm 0.00$	$4.71 \pm 0.02$	$-15.07 \pm 0.02$	$2.165 \pm 0.001$
2202+422	A	20030527	$2.016 \pm 0.003$	$2015.67 \pm 0.18$	$97.05 \pm 0.99$	$4.81 \pm 0.05$	$-22.52 \pm 0.01$	$2.062 \pm 0.001$
2202+422	A	20030609	$2.017 \pm 0.004$	$2016.40 \pm 1.76$	$96.02 \pm 0.85$	$4.76 \pm 0.04$	$-18.00 \pm 0.33$	$2.167 \pm 0.001$
2202+422	A	20030630	$2.081 \pm 0.003$	$2080.76 \pm 0.05$	$94.24 \pm 0.67$	$4.53 \pm 0.03$	$-17.84 \pm 0.60$	$2.362 \pm 0.001$
2202+422	A	20030707	$2.101 \pm 0.007$	$2100.35 \pm 1.64$	$104.18 \pm 0.61$	$4.96 \pm 0.03$	$-18.78 \pm 1.30$	$2.291 \pm 0.001$
2202+422	A	20030809	$2.381 \pm 0.002$	$2380.58 \pm 2.59$	$97.25 \pm 0.14$	$4.09 \pm 0.01$	$-0.64 \pm 2.18$	$2.750 \pm 0.001$
2202+422	A	20030821	$2.401 \pm 0.004$	$2400.15 \pm 0.32$	$94.36 \pm 0.14$	$3.93 \pm 0.01$	$-6.39 \pm 0.90$	$2.860 \pm 0.001$
2202+422	A	20030905	$2.341 \pm 0.007$	$2340.07 \pm 4.48$	$85.74 \pm 0.02$	$3.66 \pm 0.01$	$-0.42 \pm 1.56$	$2.873 \pm 0.001$
2202+422	A	20030914	$2.536 \pm 0.006$	$2534.40 \pm 2.73$	$89.88 \pm 0.71$	$3.55 \pm 0.02$	$-13.02 \pm 0.94$	$2.792 \pm 0.001$
2202+422	B	20031102	$2.450 \pm 0.002$	$2448.52 \pm 3.37$	$83.19 \pm 0.01$	$3.40 \pm 0.00$	$-9.12 \pm 0.39$	$2.645 \pm 0.001$
2202+422	B	20031117	$2.288 \pm 0.003$	$2286.56 \pm 0.36$	$97.28 \pm 0.44$	$4.25 \pm 0.02$	$-18.17 \pm 1.44$	$2.397 \pm 0.001$
2202+422	B	20031205	$2.514 \pm 0.004$	$2512.90 \pm 2.89$	$108.69 \pm 0.26$	$4.37 \pm 0.02$	$-15.73 \pm 0.11$	$2.814 \pm 0.001$
2202+422	B	20031219	$2.478 \pm 0.004$	$2474.81 \pm 0.29$	$127.94 \pm 0.12$	$5.17 \pm 0.01$	$-13.50 \pm 0.20$	$2.707 \pm 0.001$
2202+422	MEAN	all	$2.269 \pm 0.184$	$2268.19 \pm 183.41$	$101.30 \pm 12.93$	$4.50 \pm 0.68$	$-13.90 \pm 6.65$	$2.498 \pm 0.001$
<b>2253+161 C BAND</b>								
2253+161	D	20030206	$12.154 \pm 0.012$	$12148.38 \pm 31.90$	$488.79 \pm 2.39$	$4.02 \pm 0.01$	$2.54 \pm 0.74$	$10.751 \pm 0.001$
2253+161	D	20030308	$11.728 \pm 0.013$	$11721.95 \pm 14.16$	$455.86 \pm 4.89$	$3.89 \pm 0.05$	$3.21 \pm 2.32$	$0.000 \pm 0.001$
2253+161	D	20030419	$11.677 \pm 0.023$	$11669.28 \pm 34.96$	$449.99 \pm 4.89$	$3.86 \pm 0.05$	$-3.47 \pm 1.59$	$10.921 \pm 0.001$
2253+161	A	20030527	$11.240 \pm 0.025$	$11220.39 \pm 19.04$	$434.76 \pm 2.30$	$3.87 \pm 0.03$	$4.45 \pm 0.24$	$10.120 \pm 0.001$
2253+161	A	20030609	$11.124 \pm 0.031$	$11114.79 \pm 12.18$	$451.61 \pm 1.77$	$4.15 \pm 0.02$	$7.68 \pm 0.49$	$10.119 \pm 0.001$

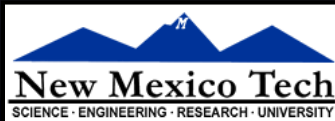
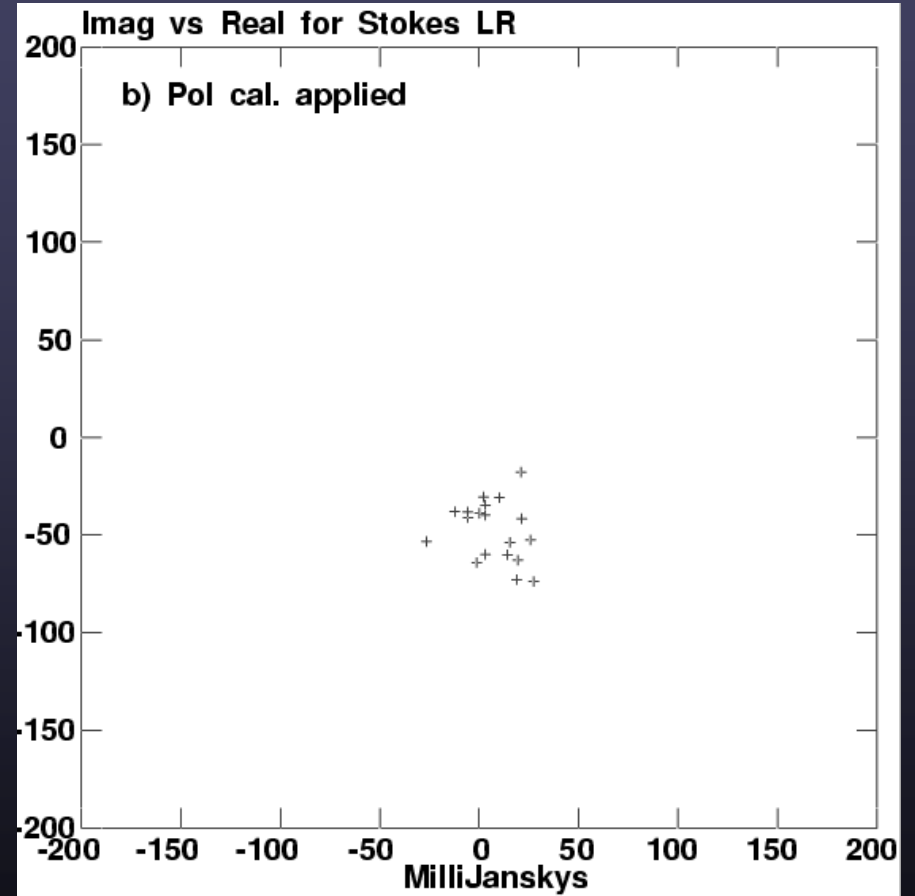
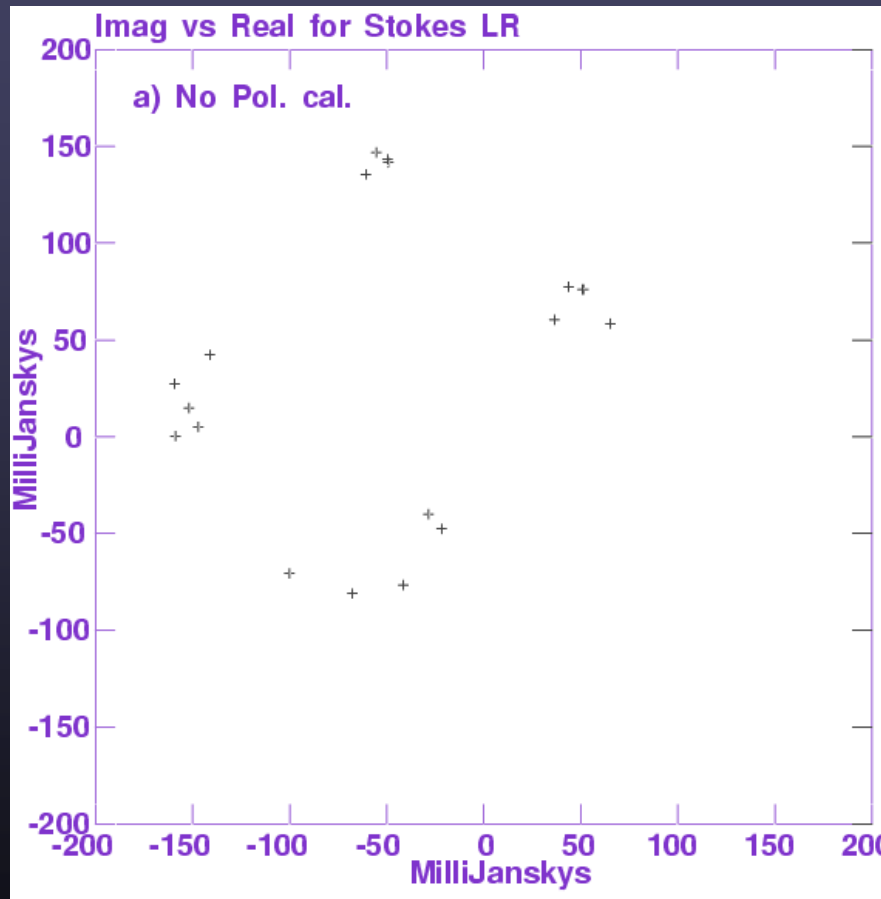


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# Example: D-term calibration

- D-term calibration effect on RL visibilities (should be  $Q+iU$ ):



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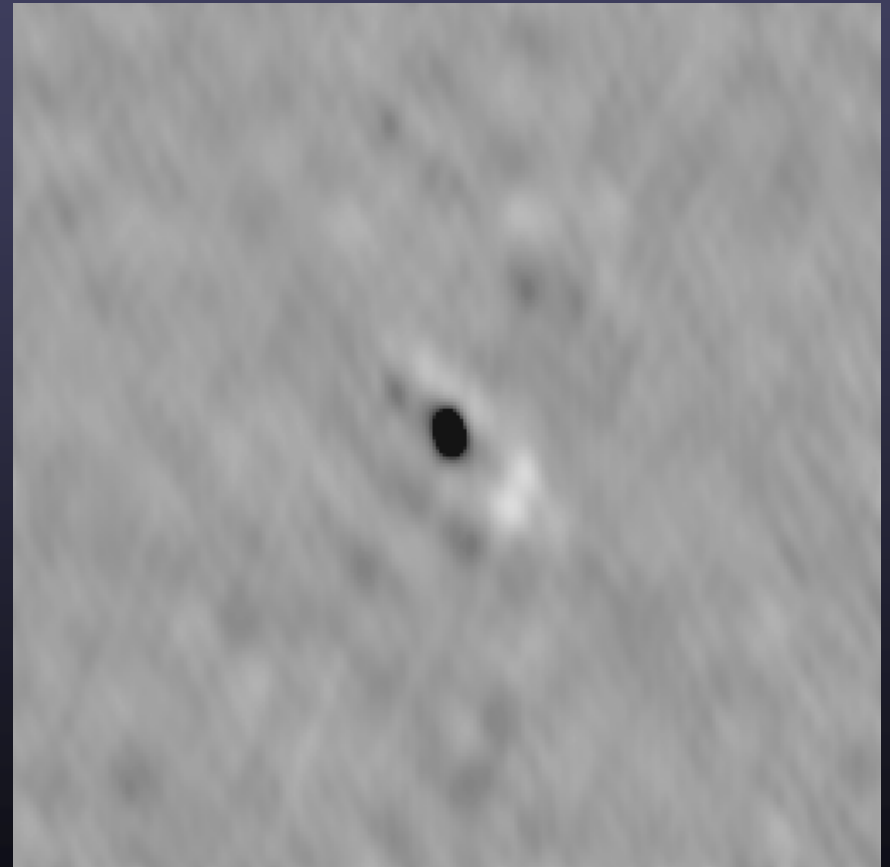
# Example: D-term calibration

- D-term calibration effect in image plane :

Bad D-term solution

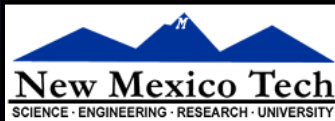


Good D-term solution



# Summary – Observing & Calibration

- Follow normal calibration procedure (previous lecture)
- Need bright calibrator for leakage D calibration
  - best calibrator has strong known polarization
  - unpolarized sources also useful
- Parallactic angle coverage useful
  - necessary for unknown calibrator polarization
- Need to determine unknown  $p$ - $q$  phase
  - CP feeds need EVPA calibrator for R-L phase
  - if system stable, can transfer from other observations
- Special Issues
  - observing CP difficult with CP feeds
  - wide-field polarization imaging (needed for EVLA & ALMA)



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