



Antennas and Receivers in Radio Astronomy

Mark McKinnon

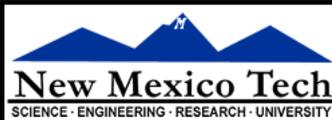
*Eleventh Synthesis Imaging Workshop
Socorro, June 10-17, 2008*



Outline

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- Context
- Types of antennas
- Antenna fundamentals
- Reflector antennas
 - Mounts
 - Optics
- Antenna performance
 - Aperture efficiency
 - Pointing
 - Polarization
- Receivers



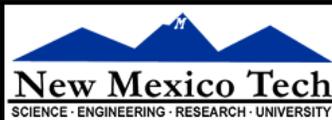
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Importance of the Antenna Elements

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- Antenna amplitude pattern causes amplitude to vary across the source.
- Antenna phase pattern causes phase to vary across the source.
- Polarization properties of the antenna modify the apparent polarization of the source.
- Antenna pointing errors can cause time varying amplitude and phase errors.
- Variation in noise pickup from the ground can cause time variable amplitude errors.
- Deformations of the antenna surface can cause amplitude and phase errors, especially at short wavelengths.



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VLA @ 4.8 GHz (C-band)

Antenna

Front End

IF

Back End

Correlator

Key



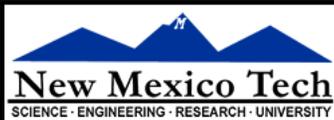
Amplifier



Mixer

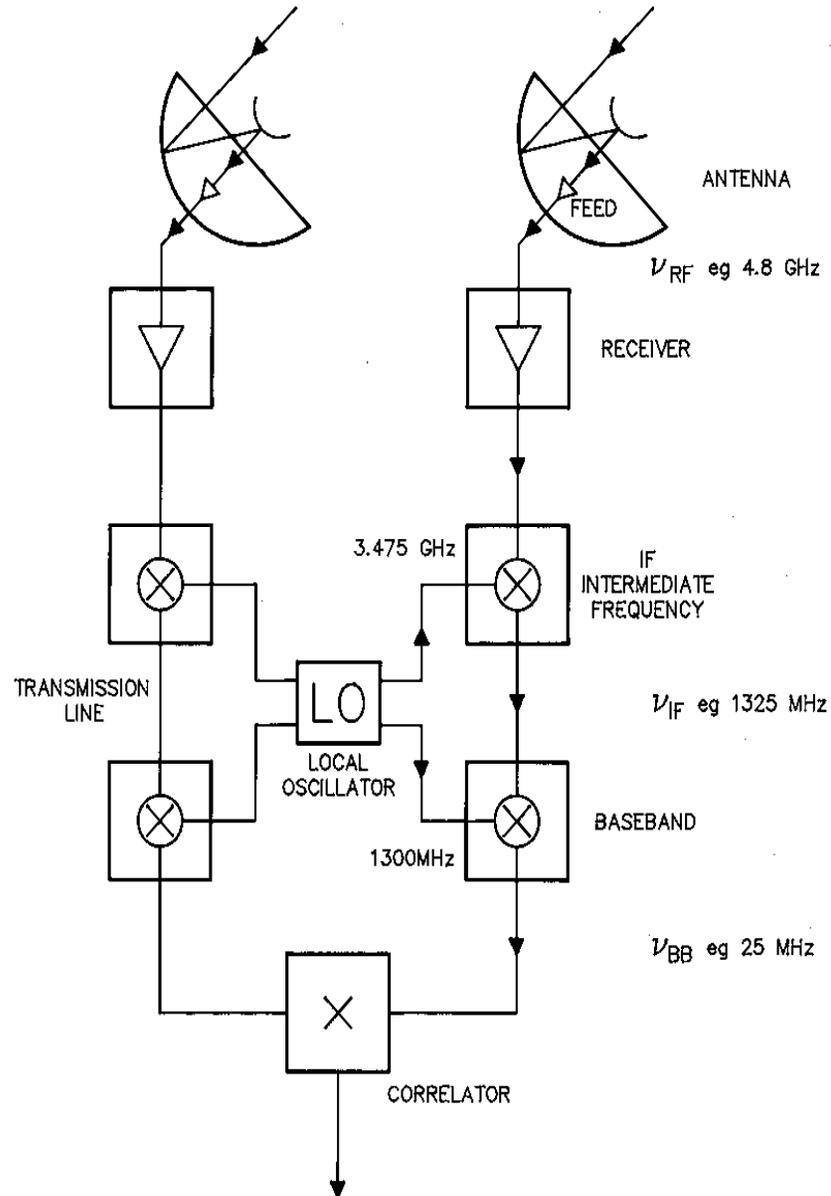


Correlator



Eleventh Syn

Interferometer Block Diagram



Types of Antennas

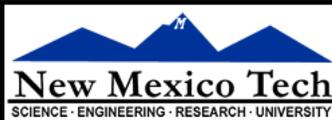
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- Wire antennas ($\lambda > 1\text{m}$)
 - Dipole
 - Yagi
 - Helix
 - Small arrays of the above
- Reflector antennas ($\lambda < 1\text{m}$)
- Hybrid antennas ($\lambda \approx 1\text{m}$)
 - Wire reflectors
 - Reflectors with dipole feeds

Yagi



Helix



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Basic Antenna Formulas

Effective collecting area $A(\nu, \theta, \phi)$ m²

On-axis response $A_0 = \eta A$
 η = aperture efficiency

Normalized pattern (primary beam)

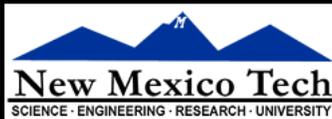
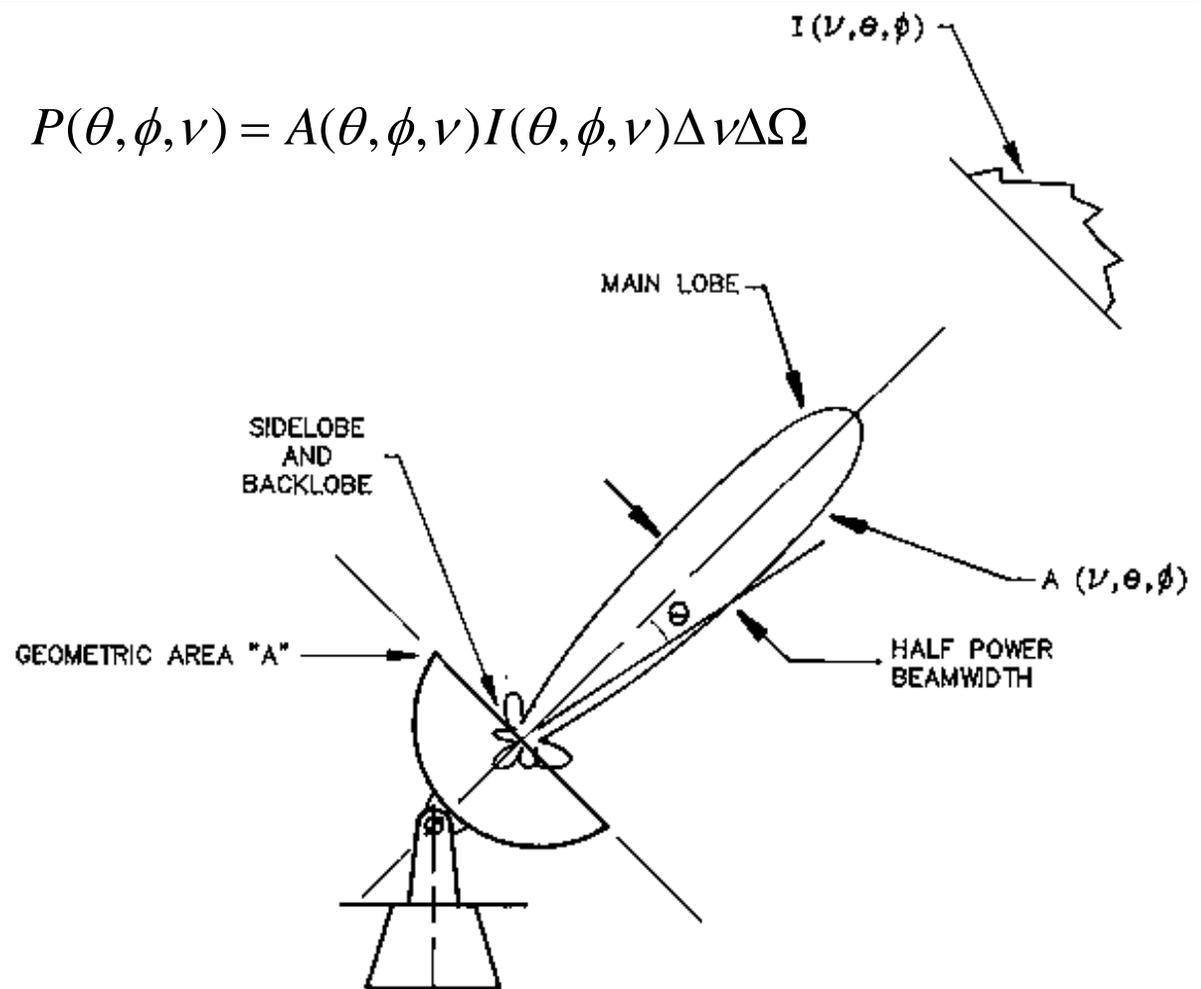
$$A(\nu, \theta, \phi) = A(\nu, \theta, \phi) / A_0$$

Beam solid angle

$$\Omega_A = \iint_{\text{all sky}} A(\nu, \theta, \phi) d\Omega$$

$$A_0 \Omega_A = \lambda^2$$

λ = wavelength, ν = frequency



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Aperture-Beam Fourier Transform Relationship 7

What determines the beam shape?

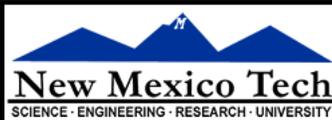
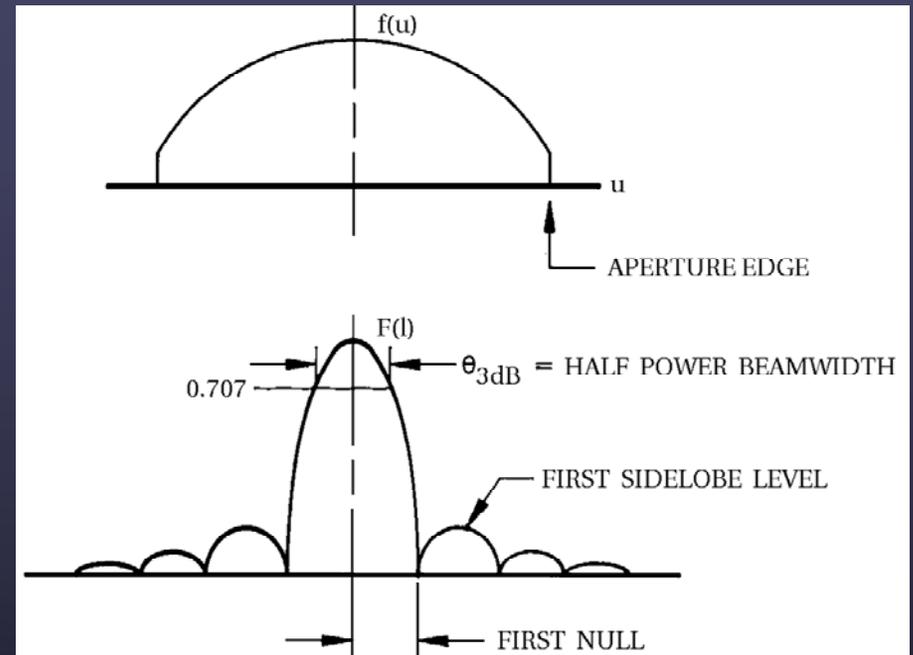
$f(u,v)$ = complex aperture field distribution
 u,v = aperture coordinates (wavelengths)

$F(l,m)$ = complex far-field voltage pattern
 $l = \sin\theta\cos\phi$, $m = \sin\theta\sin\phi$

$$F(l,m) = \iint_{\text{aperture}} f(u,v) \exp(2\pi i(ul+vm)) du dv$$

$$f(u,v) = \iint_{\text{hemisphere}} F(l,m) \exp(-2\pi i(ul+vm)) dl dm$$

For VLA: $\theta_{3\text{dB}} = 1.02/D$, First null = $1.22/D$,
 D = reflector diameter in wavelengths

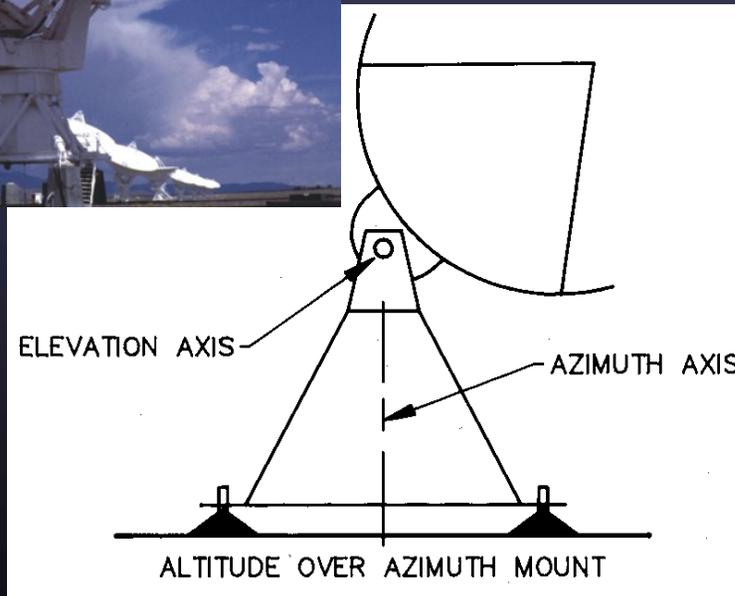


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Antenna Mounts: Altitude over Azimuth

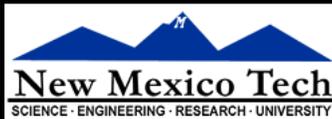
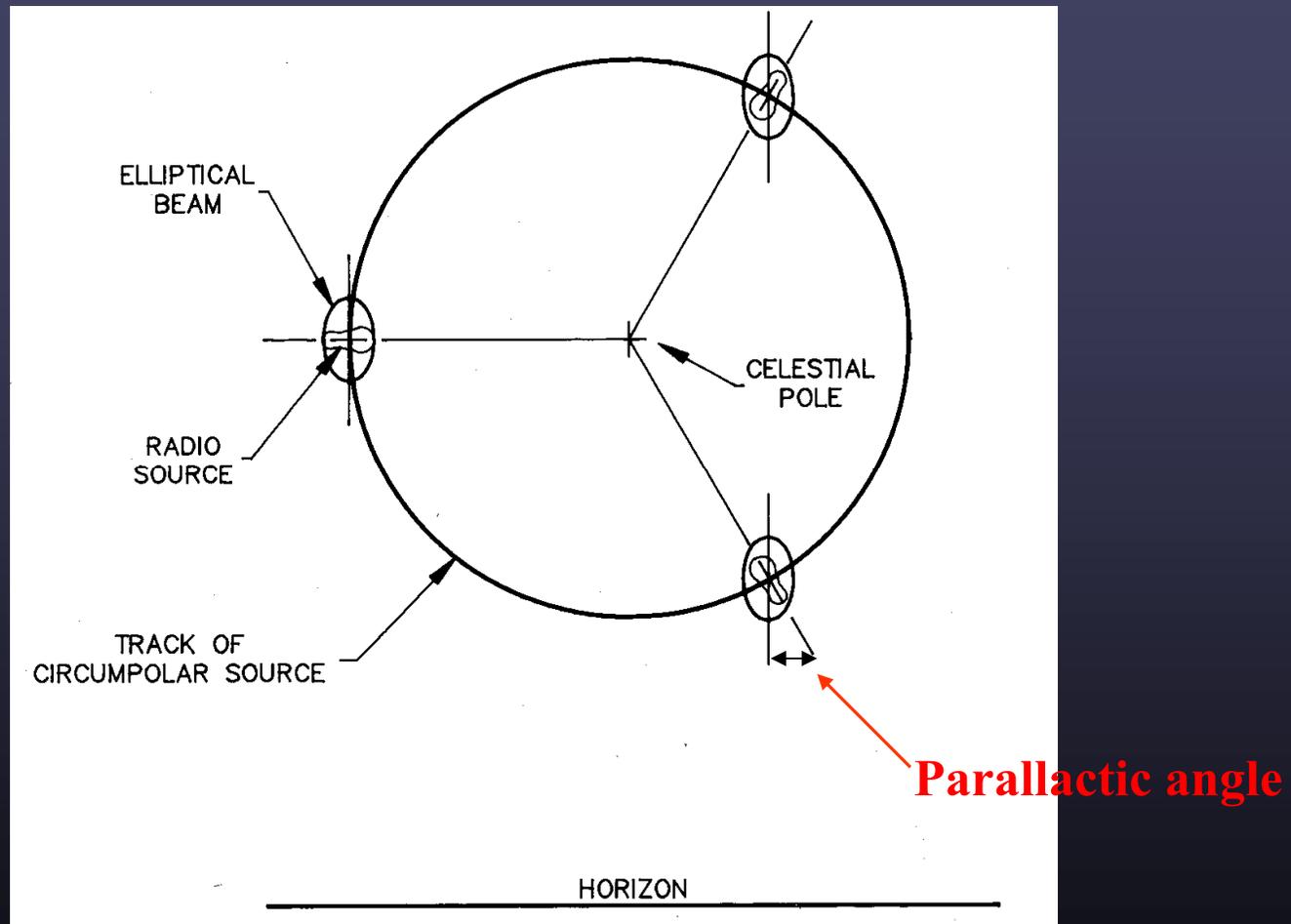
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- Advantages
 - Cost
 - Gravity performance
- Disadvantages
 - Zone of avoidance
 - Beam rotates on sky

Beam Rotation on the Sky

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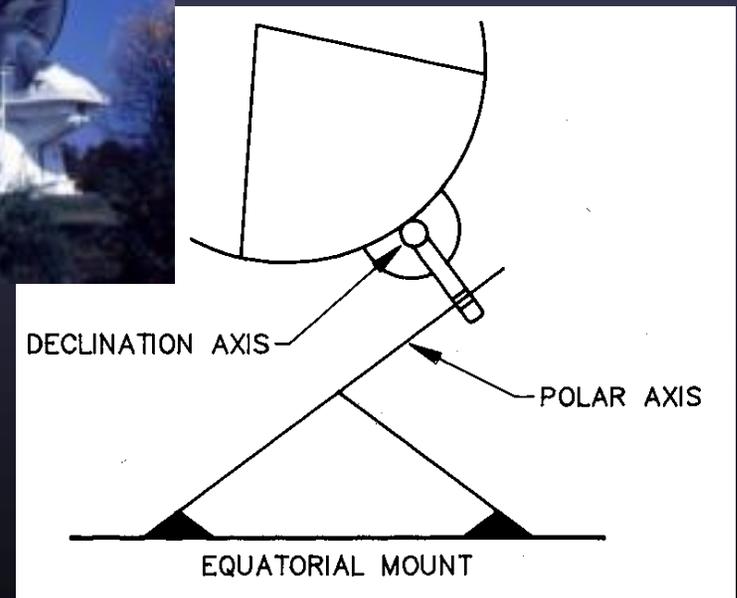
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Antenna Mounts: Equatorial

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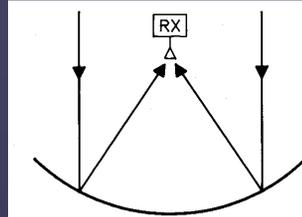
- Advantages
 - Tracking accuracy
 - Beam doesn't rotate
- Disadvantages
 - Cost
 - Gravity performance
 - Sources on horizon at pole



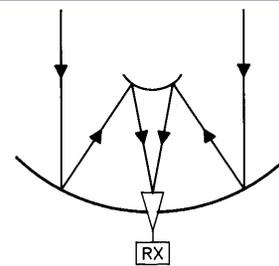
Reflector Optics

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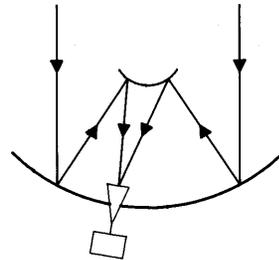
Prime focus



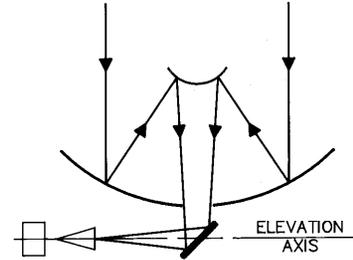
Cassegrain focus



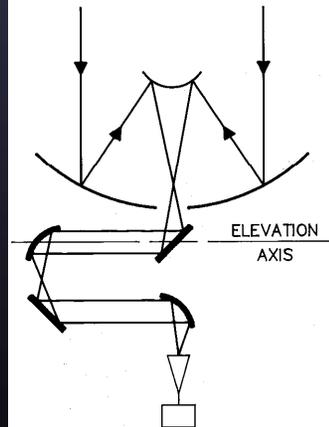
Offset Cassegrain



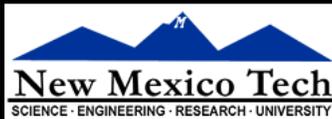
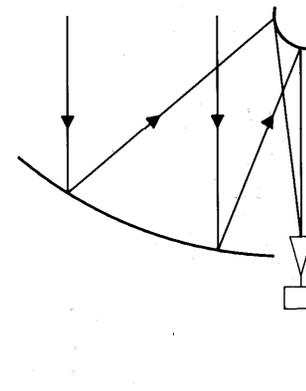
Naysmith



Beam Waveguide



Dual Offset



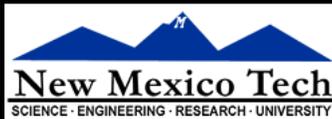
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Reflector Optics: Limitations

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- Prime focus
 - Over-illumination (spillover) can increase system temperature due to ground pick-up
 - Number of receivers, and access to them, is limited
- Subreflector systems
 - Can limit low frequency capability. Feed horn too large.
 - Over-illumination by feed horn can exceed gain of reflector's diffraction limited sidelobes
 - Strong sources a few degrees away may limit image dynamic range
- Offset optics
 - Support structure of offset feed is complex and expensive



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Reflector Optics: Examples

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Prime focus
(GMRT)



Cassegrain focus
(AT)



Offset Cassegrain
(VLA)



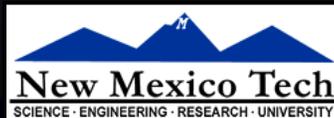
Naysmith
(OVRO)



Beam Waveguide
(NRO)



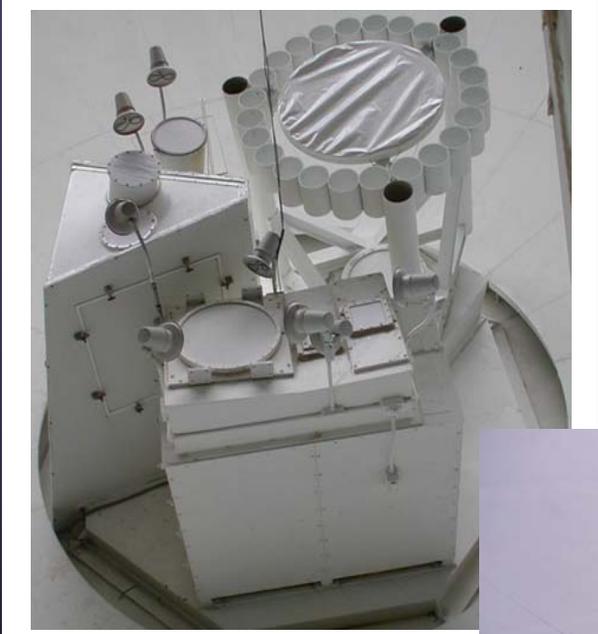
Dual Offset
(GBT)



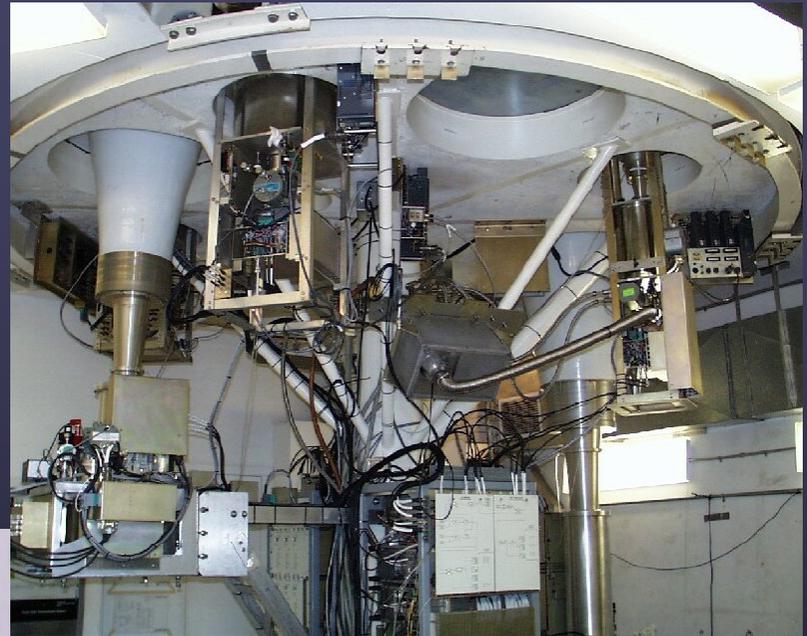
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Feed Systems



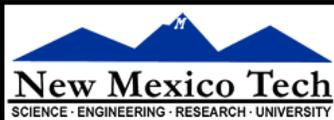
VLA



GBT



EVLA



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Antenna Performance: Aperture Efficiency

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On axis response: $A_0 = \eta A$

Efficiency: $\eta = \eta_{sf} \times \eta_{bl} \times \eta_s \times \eta_t \times \eta_{misc}$

η_{sf} = Reflector surface efficiency

Due to imperfections in reflector surface

$$\eta_{sf} = \exp(-4\pi\sigma/\lambda)^2 \quad \text{e.g., } \sigma = \lambda/16, \eta_{sf} = 0.5$$

η_{bl} = Blockage efficiency

Caused by subreflector and its support structure

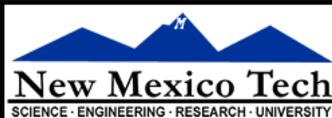
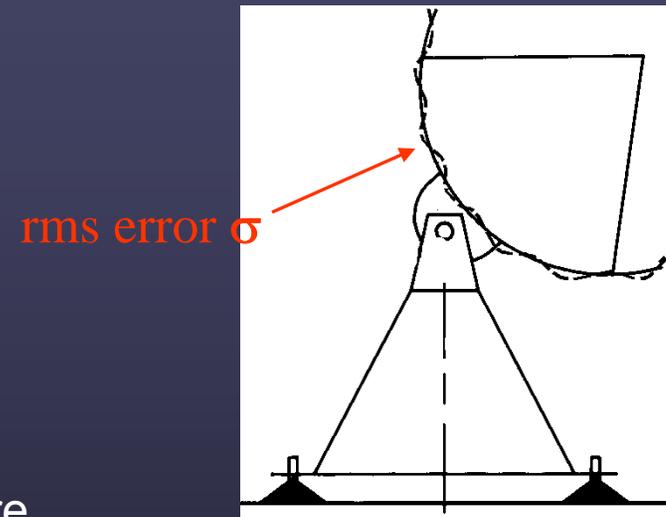
η_s = Feed spillover efficiency

Fraction of power radiated by feed intercepted by subreflector

η_t = Feed illumination efficiency

Outer parts of reflector illuminated at lower level than inner part

η_{misc} = Reflector diffraction, feed position phase errors, feed match and loss



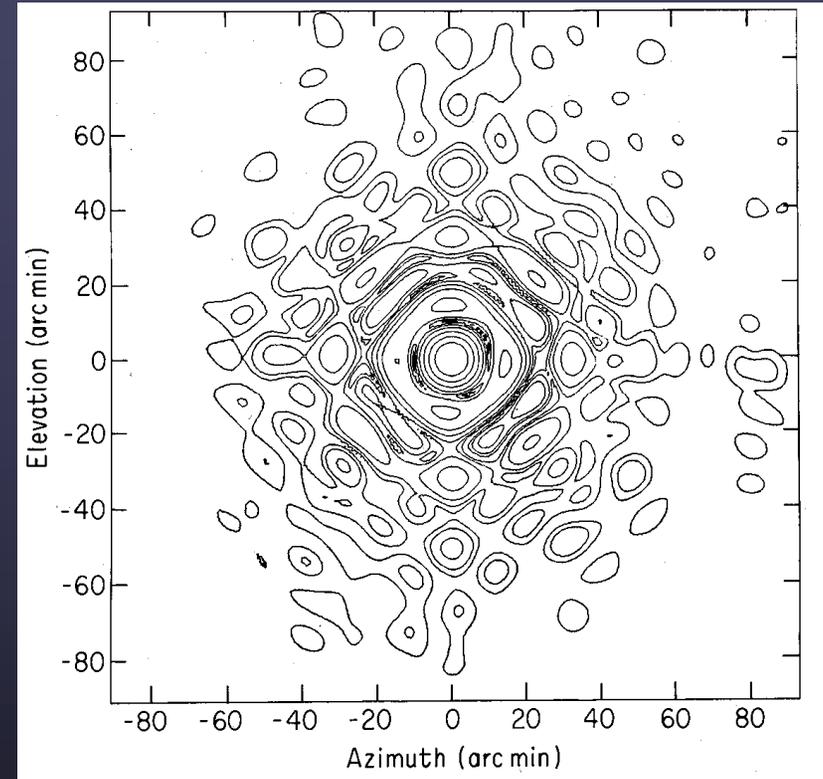
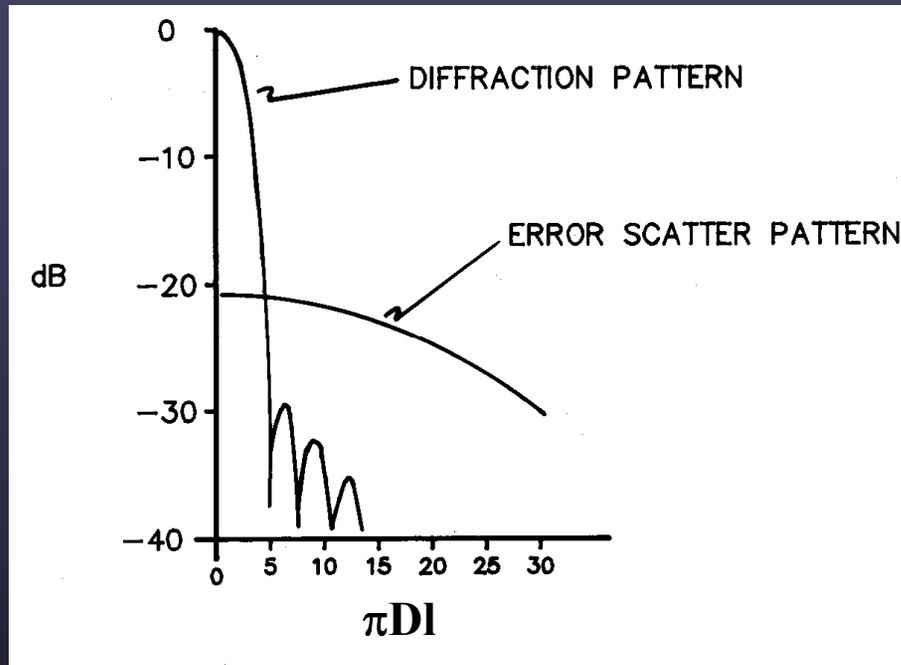
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Antenna Performance: Aperture Efficiency

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Primary Beam



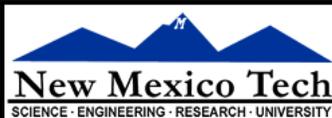
$l = \sin(\theta)$, D = antenna diameter in wavelengths

$\text{dB} = 10\log(\text{power ratio}) = 20\log(\text{voltage ratio})$

VLA: $\theta_{3\text{dB}} = 1.02/D$, First null = $1.22/D$

contours: -3, -6, -10, -15, -20, -25, -30, -35, -40 dB

Voltage radiation pattern, $|F(l,m)|$



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Antenna Pointing: Practical Considerations

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Reflector structure

Subreflector mount

EI encoder

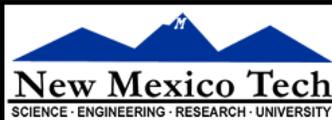
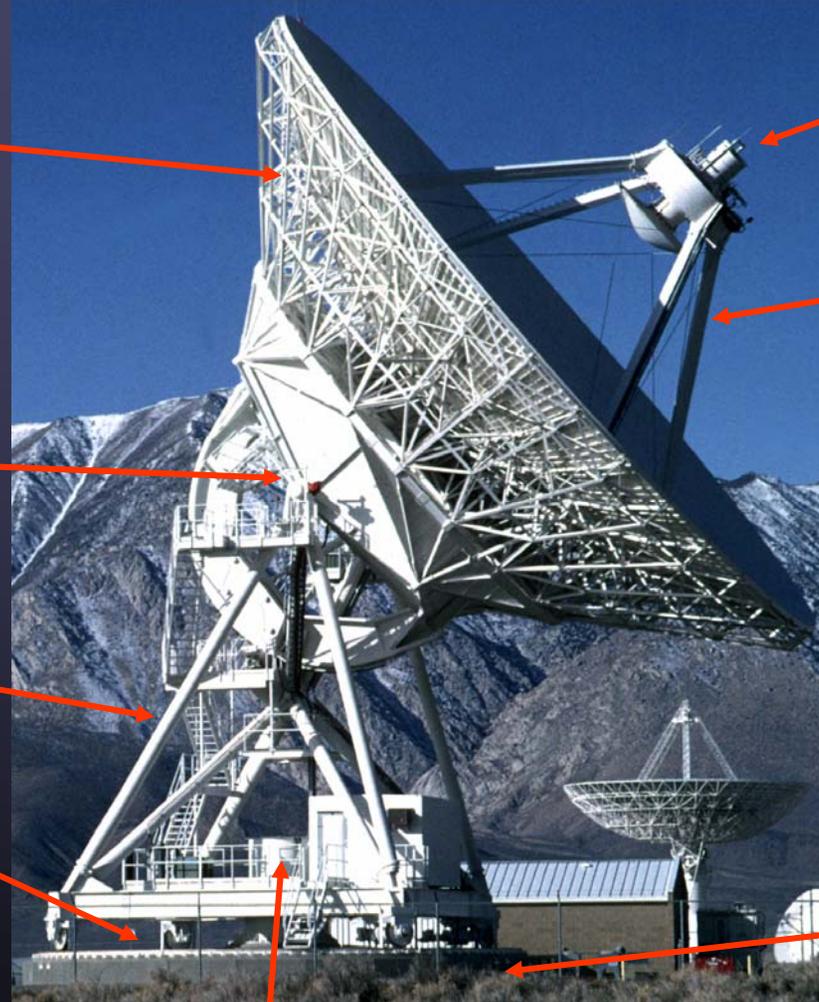
Quadrupod

Alidade structure

Rail flatness

Foundation

Az encoder



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Antenna Performance: Pointing

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Pointing Accuracy

$\Delta\theta$ = rms pointing error

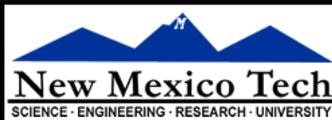
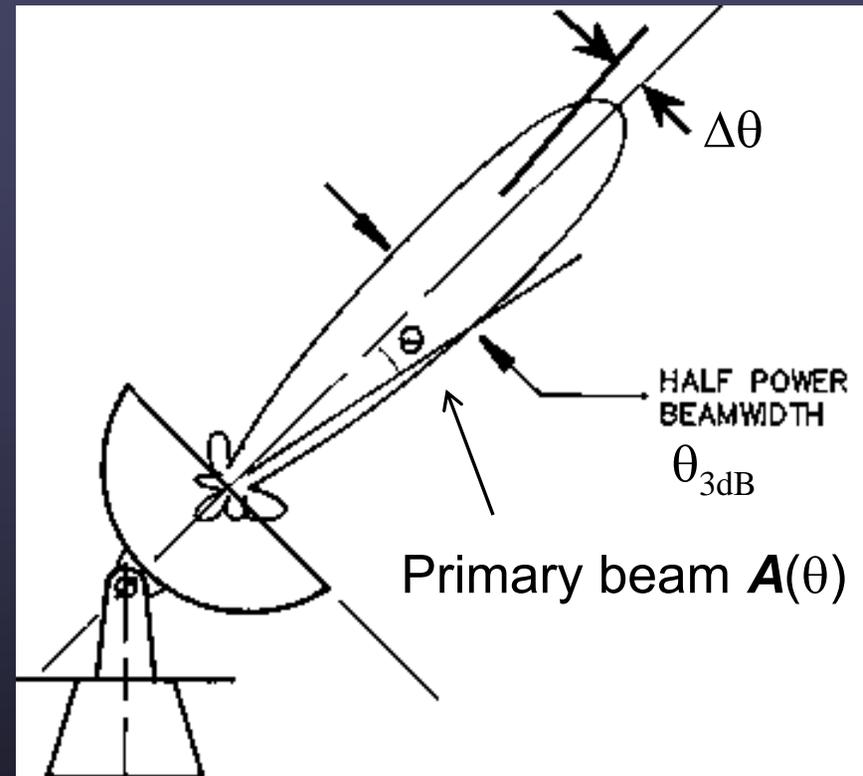
Often $\Delta\theta < \theta_{3\text{dB}} / 10$ acceptable,
because $A(\theta_{3\text{dB}} / 10) \sim 0.97$

BUT, at half power point in beam

$$A(\theta_{3\text{dB}} / 2 \pm \theta_{3\text{dB}} / 10) / A(\theta_{3\text{dB}} / 2) = \pm 0.3$$

For best VLA pointing use Reference Pointing.

$$\Delta\theta = 3 \text{ arcsec} = \theta_{3\text{dB}} / 17 @ 50 \text{ GHz}$$

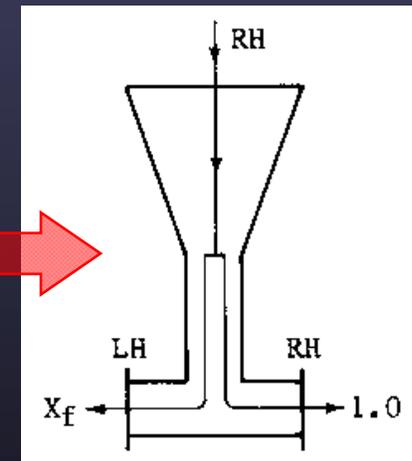


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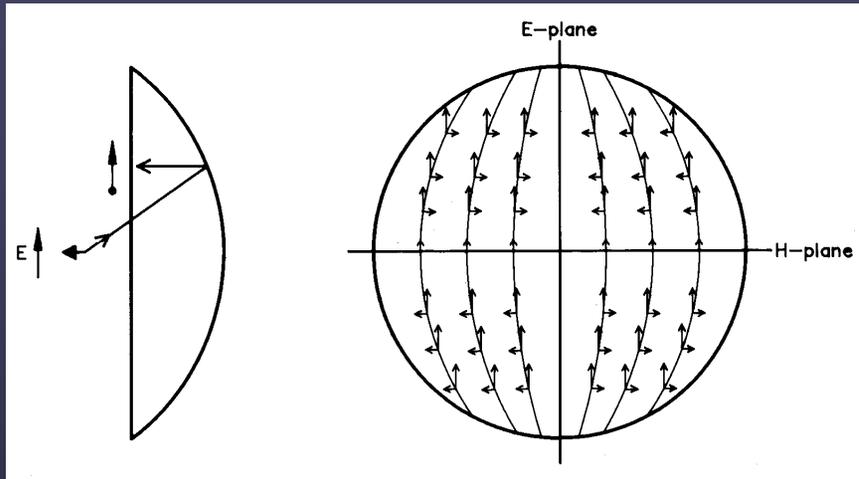


Antenna can modify the apparent polarization properties of the source:

- Antenna structure
 - Symmetry of the optics
 - Reflections in the optics
 - Curvature of the reflectors
- Quality of feed polarization splitter
 - Constant across the beam
- Circularity of feed radiation patterns
 - No instrumental polarization on-axis,
 - But cross-polarization varies across the beam ...

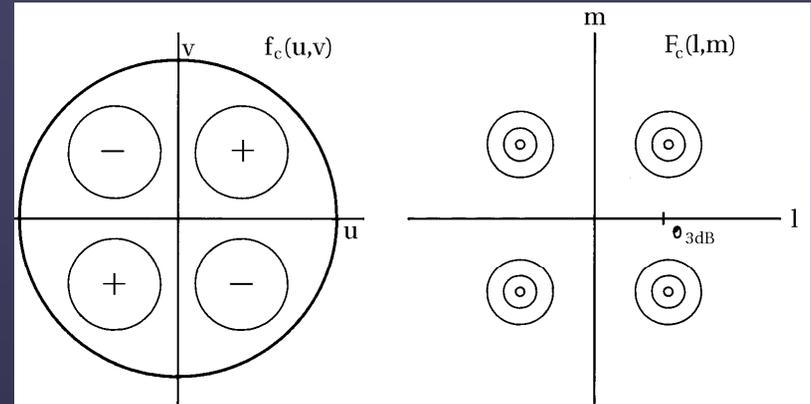


Off-Axis Cross Polarization



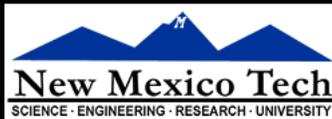
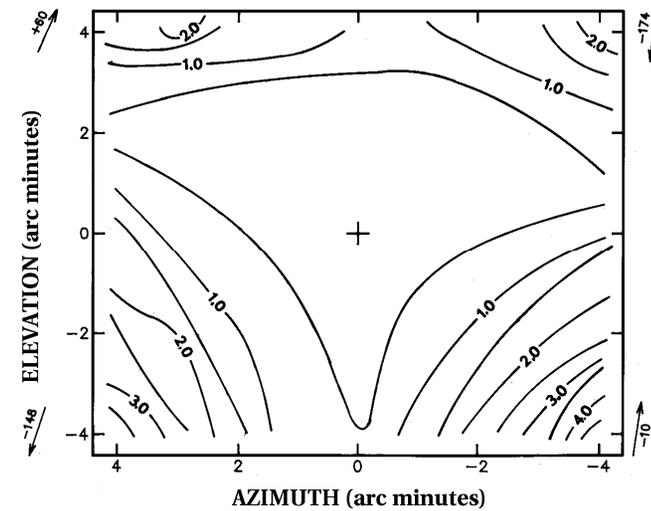
Field distribution in aperture of paraboloid fed by electric dipole

VLA 4.8 GHz cross-polarized primary beam



Cross-polarized aperture distribution

Cross-polarized primary beam



Receivers: Noise Temperature

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- Reference received power to the equivalent temperature of a matched load at the input to the receiver
- Rayleigh-Jeans approximation to Planck radiation law for a blackbody

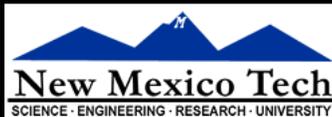
$$P_{in} = k_B T \Delta\nu \quad (\text{W})$$

Matched load
@ temp T ($^{\circ}\text{K}$)



k_B = Boltzman's constant ($1.38 \cdot 10^{-23}$ J/ $^{\circ}\text{K}$)

- When observing a radio source, $T_{total} = T_A + T_{sys}$
 - T_{sys} = system noise when not looking at a discrete radio source
 - T_A = source antenna temperature



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Receivers: SEFD

$$T_A = \eta AS / (2k_B) = KS$$

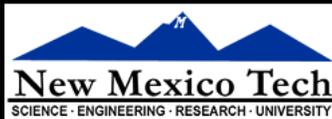
S = source flux (Jy)

SEFD = system equivalent flux density

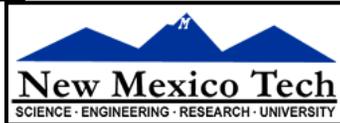
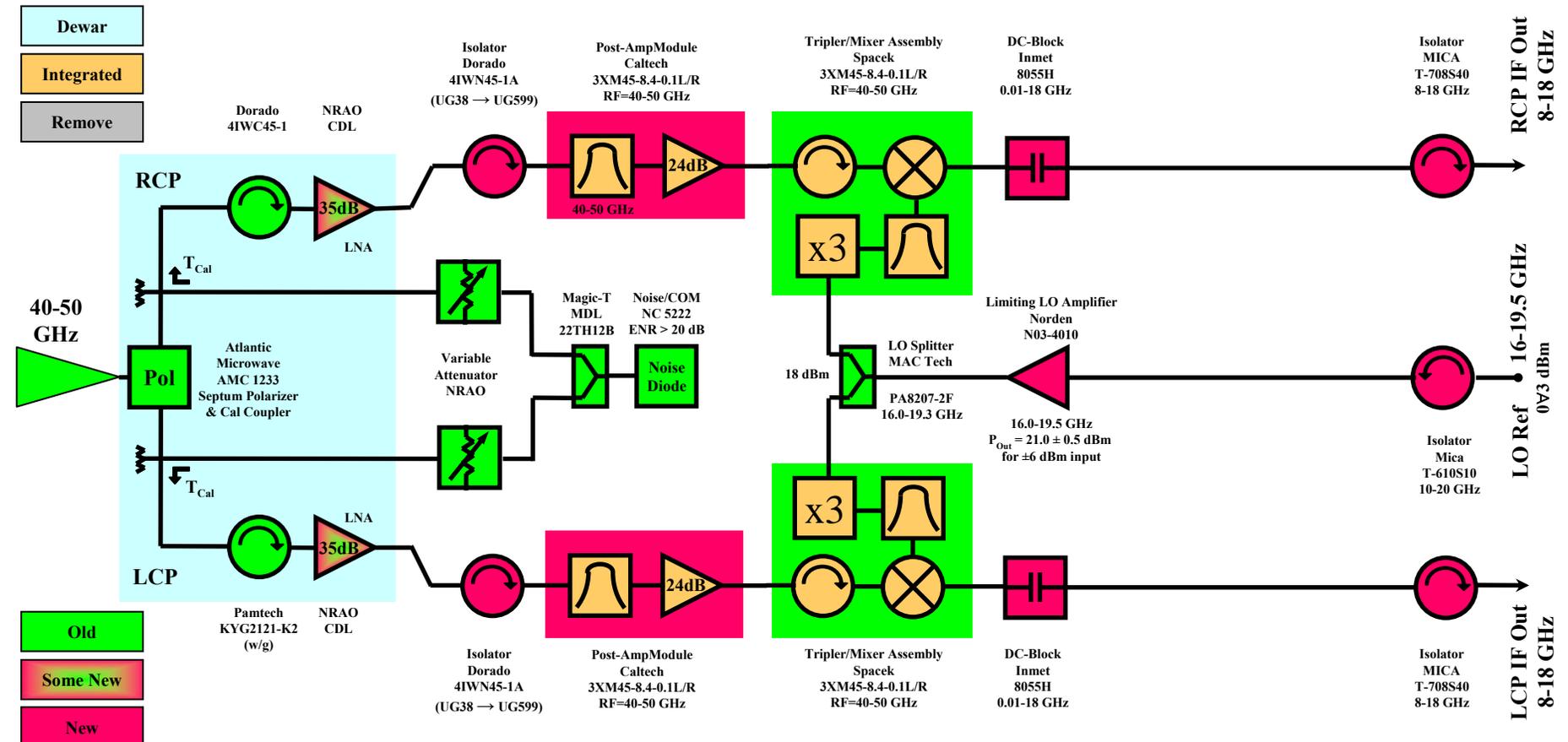
$$SEFD = T_{sys} / K \text{ (Jy)}$$

EVLA Sensitivities

Band (GHz)	η	T_{sys}	SEFD
1-2	.50	21	236
2-4	.62	27	245
4-8	.60	28	262
8-12	.56	31	311
12-18	.54	37	385
18-26	.51	55	606
26-40	.39	58	836
40-50	.34	78	1290



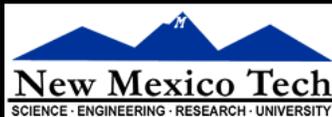
EVLA Q-Band (40-50 GHz) Receiver



Corrections to Chapter 3 of Synthesis Imaging in Radio Astronomy II

Equation 3-8: replace u,v with l,m

Figure 3-7: abscissa title should be $\pi D l$



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