

# ERROR RECOGNITION & IMAGE ANALYSIS

Ed Fomalont (NRAO)

*Eleventh Synthesis Imaging Workshop  
Socorro, June 10-17, 2008*



## PREMABLE TO ERROR RECOGNITION and IMAGE ANALYSIS

- Why are these two topics in the same lecture?
  - **Error recognition** is used to determine defects in the data  
and image during and after the 'best' calibration, editing, etc.
  - **Image analysis** describes the almost infinite ways in which  
useful insight, information and parameters can be  
extracted from the image.
- Perhaps the two topics are related to the reaction one has  
when looking at an image after 'good' calibration,  
editing, self-calibration, etc.

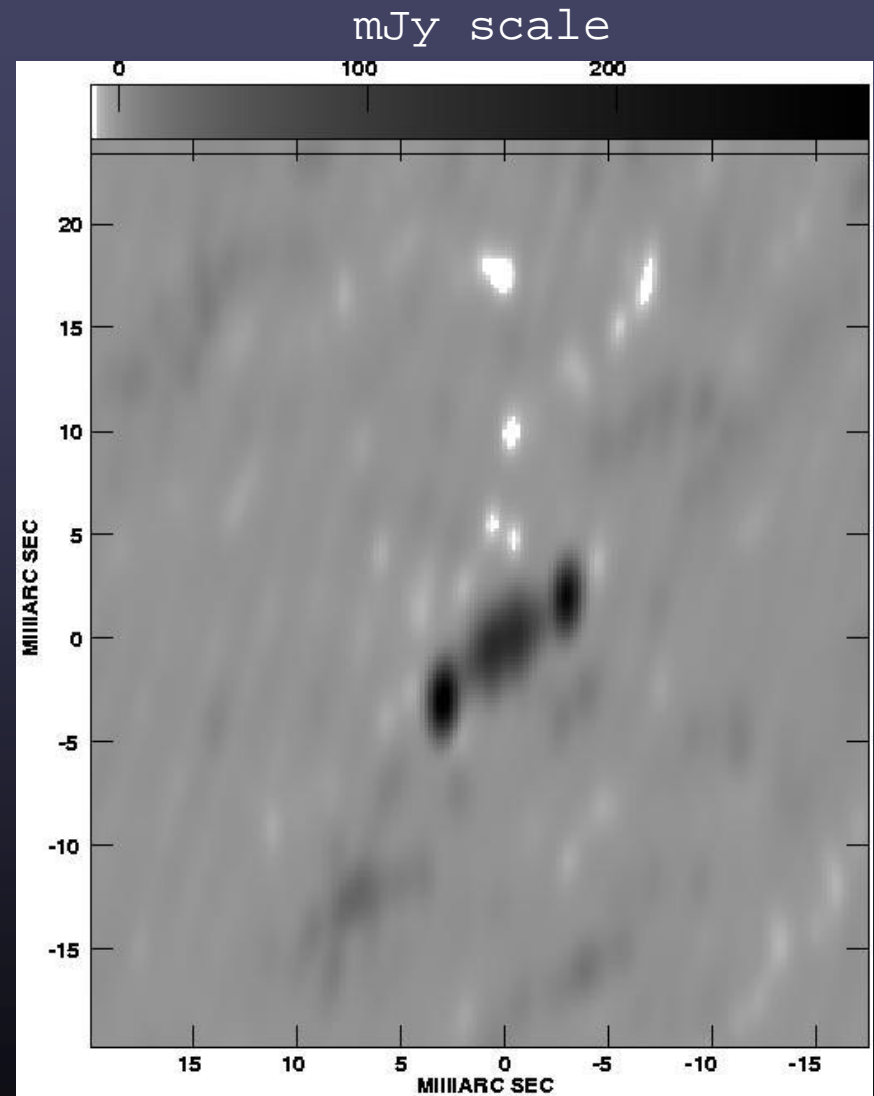
## OBVIOUS IMAGE PROBLEMS

### Rats!!

This can't be right.  
This is either the most remarkable radio source ever, or I have made an error in making the image.

Image rms, compared to the expected rms, unnatural features in the image, etc are clear signs of problems.

How can the problems be found and corrected?



milliarcsec

## HIGH QUALITY IMAGE

**Great!!**

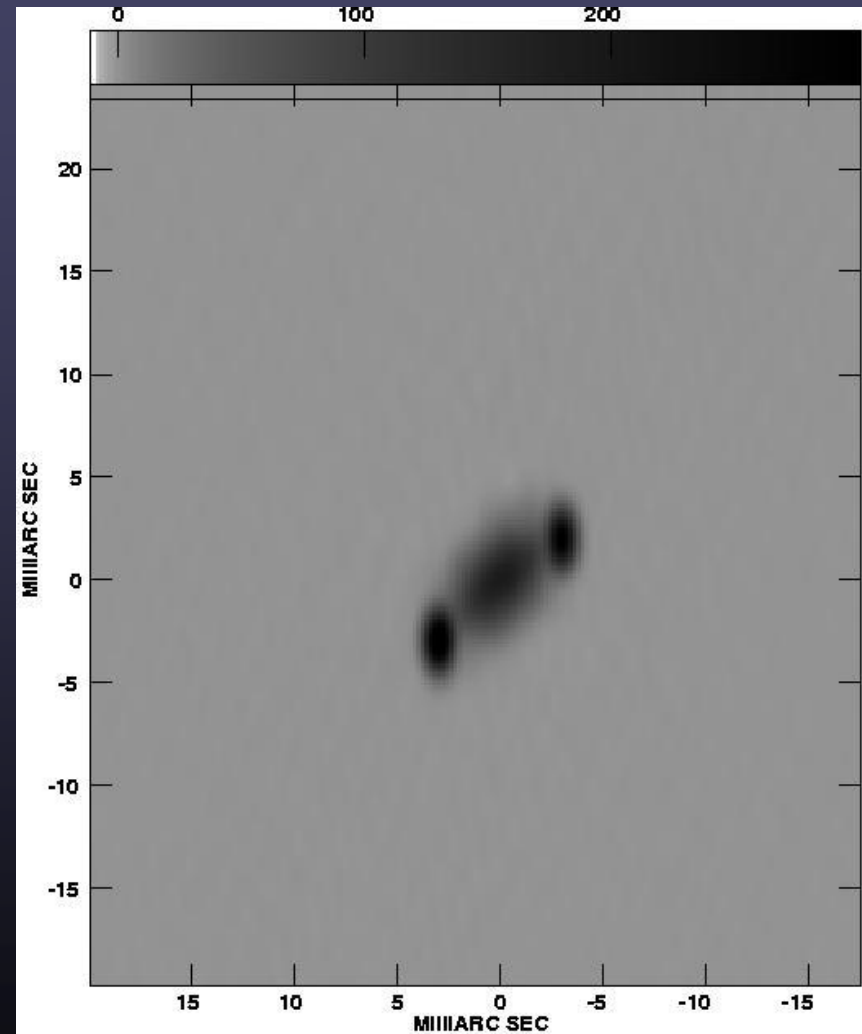
After lots of work, I can finally analyze this image and get some interesting scientific results.

**What were defects?**

Two antennas had 10% calibration errors, and one with a 5 deg error, plus a few outlier points.

**This part of the lecture.**

How to find the errors and remove



milliarcsec

## GENERAL PROCEDURE

Assuming that the data have been edited and calibrated reasonably successfully (earlier lectures). Self-calibration is usually necessary.

So, the first serious display of an image leads one--

to inspect again and clean-up the data with repetition of some or all of the previous reduction steps.

to image analysis and obtaining scientific results from the image.

But, first a digression on data and image display.

# IMAGE DISPLAYS (1)

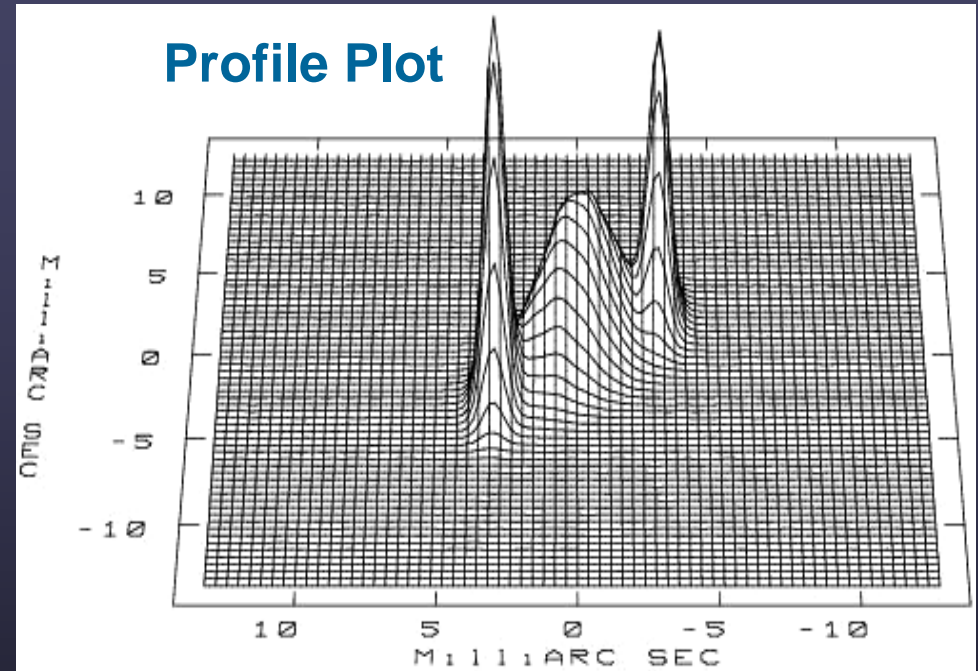
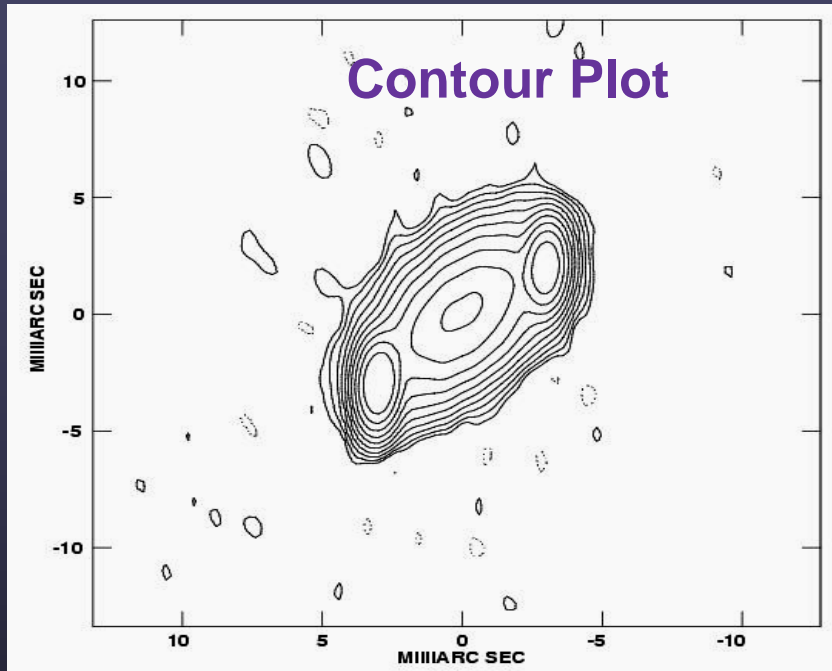
	Pixel values																													
	235						245						255						265						275					
287	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
285	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0				
283	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	0	0	0				
281	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	2	3	3	3	4	3	1	0	0				
279	0	0	0	0	0	0	0	0	0	0	0	0	1	1	2	3	4	4	5	5	8	12	8	3	1	0				
277	0	0	0	0	0	0	0	0	0	0	0	1	2	3	5	7	7	8	9	9	19	32	22	8	1	0				
275	0	0	0	0	0	0	0	0	0	0	1	2	4	6	9	13	14	15	14	16	40	72	47	12	2	0				
273	0	0	0	0	0	0	0	1	1	1	2	4	8	12	17	22	23	24	22	27	77	136	87	19	2	0				
271	0	0	0	0	0	0	0	1	1	2	4	8	15	21	28	35	36	37	33	43	126	217	132	28	3	0				
269	0	0	0	0	0	0	0	1	3	4	8	15	25	34	44	54	54	53	48	61	173	288	168	34	3	0				
267	0	0	0	0	0	0	1	2	4	8	14	25	40	52	67	79	77	74	63	75	199	316	177	34	3	0				
265	0	0	0	0	0	0	1	3	7	14	24	40	60	77	97	109	102	93	74	79	191	289	155	29	3	0				
263	0	0	0	0	0	1	2	5	11	22	37	59	86	108	130	137	123	105	79	73	154	220	113	20	2	0				
261	0	0	0	0	1	1	3	8	17	33	54	81	118	139	156	156	133	107	75	61	106	140	69	12	2	0				
259	0	0	0	0	1	2	5	12	24	45	72	105	143	182	170	161	131	99	66	47	64	75	36	6	1	0				
257	0	0	0	0	2	4	8	18	32	58	88	124	160	171	169	152	118	86	55	36	36	36	16	3	1	0				
255	0	0	0	1	2	7	16	27	42	70	101	135	182	184	158	134	100	71	44	27	20	16	7	1	0					
253	0	0	0	1	4	15	34	43	51	77	105	133	150	146	135	112	81	56	34	19	11	7	3	1	0					
251	0	0	0	1	8	34	73	70	59	79	100	120	130	122	110	88	61	41	24	12	6	3	1	0	0					
249	0	0	1	2	14	69	141	112	65	73	87	100	106	96	83	64	43	27	14	7	3	1	1	0	0					
247	0	0	1	3	23	121	238	167	69	62	69	77	81	70	59	42	26	16	8	3	1	0	0	0	0					
245	0	0	1	3	34	180	338	217	69	48	52	56	57	47	36	25	15	8	3	1	0	0	0	0	0					
243	0	0	1	4	42	222	402	242	65	36	37	39	37	29	21	14	7	4	1	0	0	0	0	0	0					
241	0	0	1	4	44	229	398	228	56	26	25	25	22	16	11	7	3	1	0	0	0	0	0	0	0					
239	0	0	1	3	39	196	327	179	41	18	18	15	12	8	5	3	1	1	0	0	0	0	0	0	0					
237	0	0	1	3	28	139	223	118	26	11	9	8	6	4	2	1	1	0	0	0	0	0	0	0	0					
235	0	0	0	2	18	82	127	64	14	6	5	4	3	1	1	1	0	0	0	0	0	0	0	0	0					
233	0	0	0	1	9	40	60	29	7	3	2	1	1	0	0	0	0	0	0	0	0	0	0	0	0					
231	0	0	0	0	4	17	23	11	3	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
229	0	0	0	0	2	6	7	3	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
227	0	0	0	0	1	2	2	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
225	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
223	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					

Digital image

Numbers are proportional to the intensity

Good for slow links, ie. For the Gobi device to Socorro

## IMAGE DISPLAYS (2)



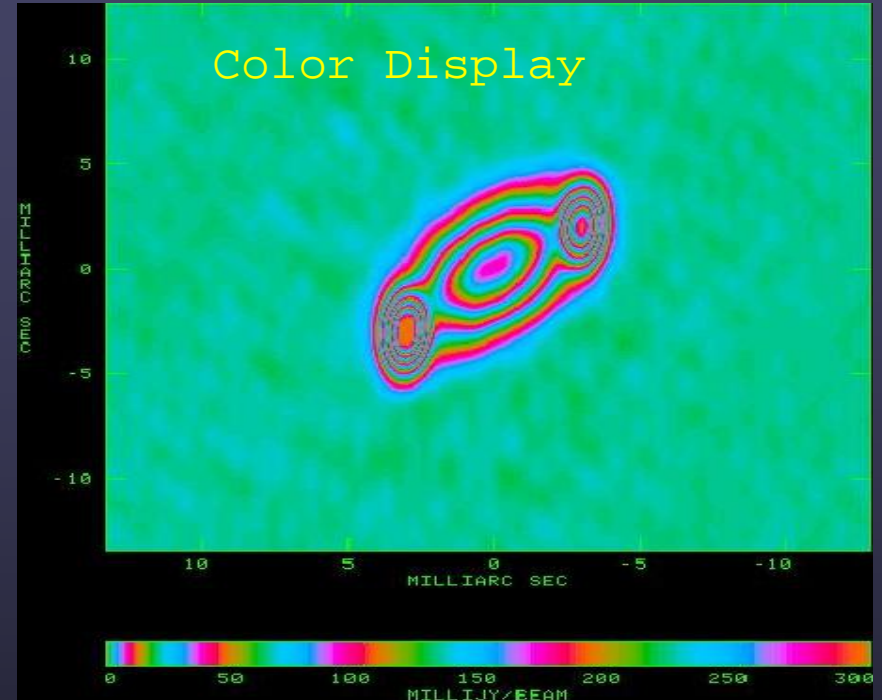
**These plots are easy to reproduce and printed**

Contour plots give good representation of faint emission.

Profile plots give a good representation of the 'mosque-like'



## IMAGE DISPLAYS (3)



**TV-based displays are most useful and interactive:**

Grey-scale shows faint structure, but not good for high dynamic range and somewhat unbiased view of source



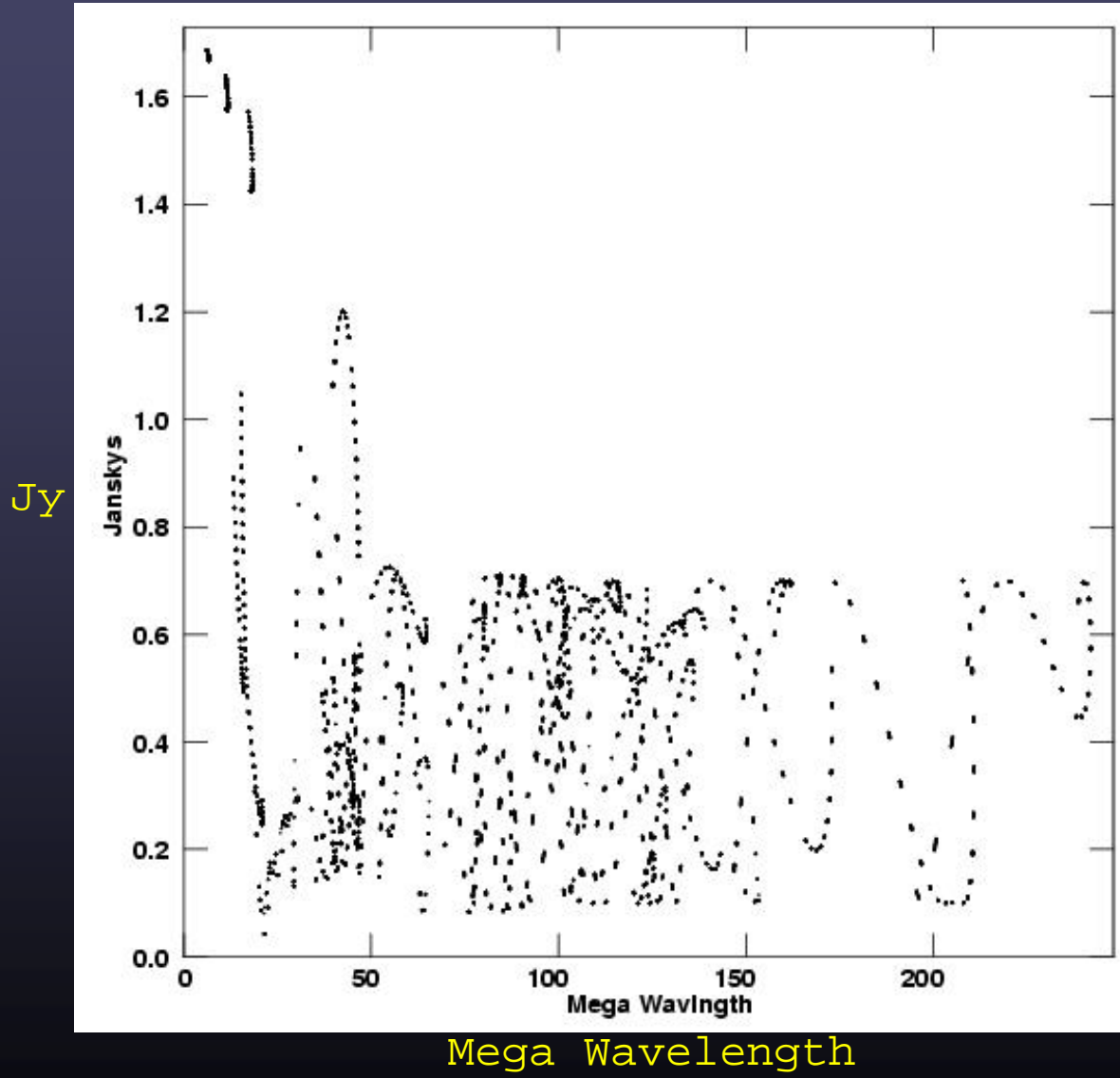
## DATA DISPLAYS (1)

### List of u-v Data

Source=	J0121+11	Freq=	8.434858511	Sort=	TB	1	RR			
Vis #	IAT	Ant	Su Fq	U(klam)	V(klam)	W(klam)	Amp	Phas	Wt	
2191	0/22:35:08.22	5- 6	1 0	94220	23776	100371	0.614	-16	1.0000	
3971	0/22:43:43.34	5- 6	1 0	97659	24517	96844	0.508	-13	1.0000	
6431	0/23:07:05.15	5- 6	1 0	106307	26661	86632	0.154	17	1.0000	
6611	0/23:07:14.98	5- 6	1 0	106364	26677	86557	0.152	17	1.0000	
6791	0/23:07:24.81	5- 6	1 0	106421	26692	86483	0.150	18	1.0000	
6971	0/23:07:34.64	5- 6	1 0	106477	26708	86408	0.148	19	1.0000	
7151	0/23:07:44.47	5- 6	1 0	106534	26724	86333	0.146	19	1.0000	
7331	0/23:07:54.30	5- 6	1 0	106591	26739	86259	0.144	20	1.0000	
7511	0/23:15:06.84	5- 6	1 0	109027	27438	82930	0.101	74	1.0000	
7691	0/23:15:16.67	5- 6	1 0	109081	27454	82854	0.101	75	1.0000	
7871	0/23:15:26.50	5- 6	1 0	109135	27470	82777	0.102	77	1.0000	
8051	0/23:15:36.33	5- 6	1 0	109189	27486	82701	0.102	78	1.0000	
8231	0/23:15:46.16	5- 6	1 0	109243	27502	82624	0.103	79	1.0000	
8411	0/23:15:55.99	5- 6	1 0	109297	27518	82547	0.104	81	1.0000	
9701	0/23:31:02.36	5- 6	1 0	114020	29035	75322	0.260	134	1.0000	
9791	0/23:31:06.29	5- 6	1 0	114040	29042	75290	0.261	134	1.0000	
10301	0/23:31:29.88	5- 6	1 0	114156	29082	75098	0.266	134	1.0000	
10861	0/23:39:02.08	5- 6	1 0	116320	29863	71379	0.348	139	1.0000	
10951	0/23:39:06.01	5- 6	1 0	116339	29870	71346	0.348	139	1.0000	
11171	0/23:39:15.84	5- 6	1 0	116384	29887	71264	0.350	139	1.0000	

Very primitive display, but sometimes worth-while: egs,  
can search on  
Amp > 1.0, for example, or large Wt. Often need precise  
times in order to  
flag the data appropriately.

## DATA DISPLAYS (2)



Visibility Amplitude  
versus  
Projected uv  
spacing

General trend of  
data.

Useful for  
relatively strong  
Sources.

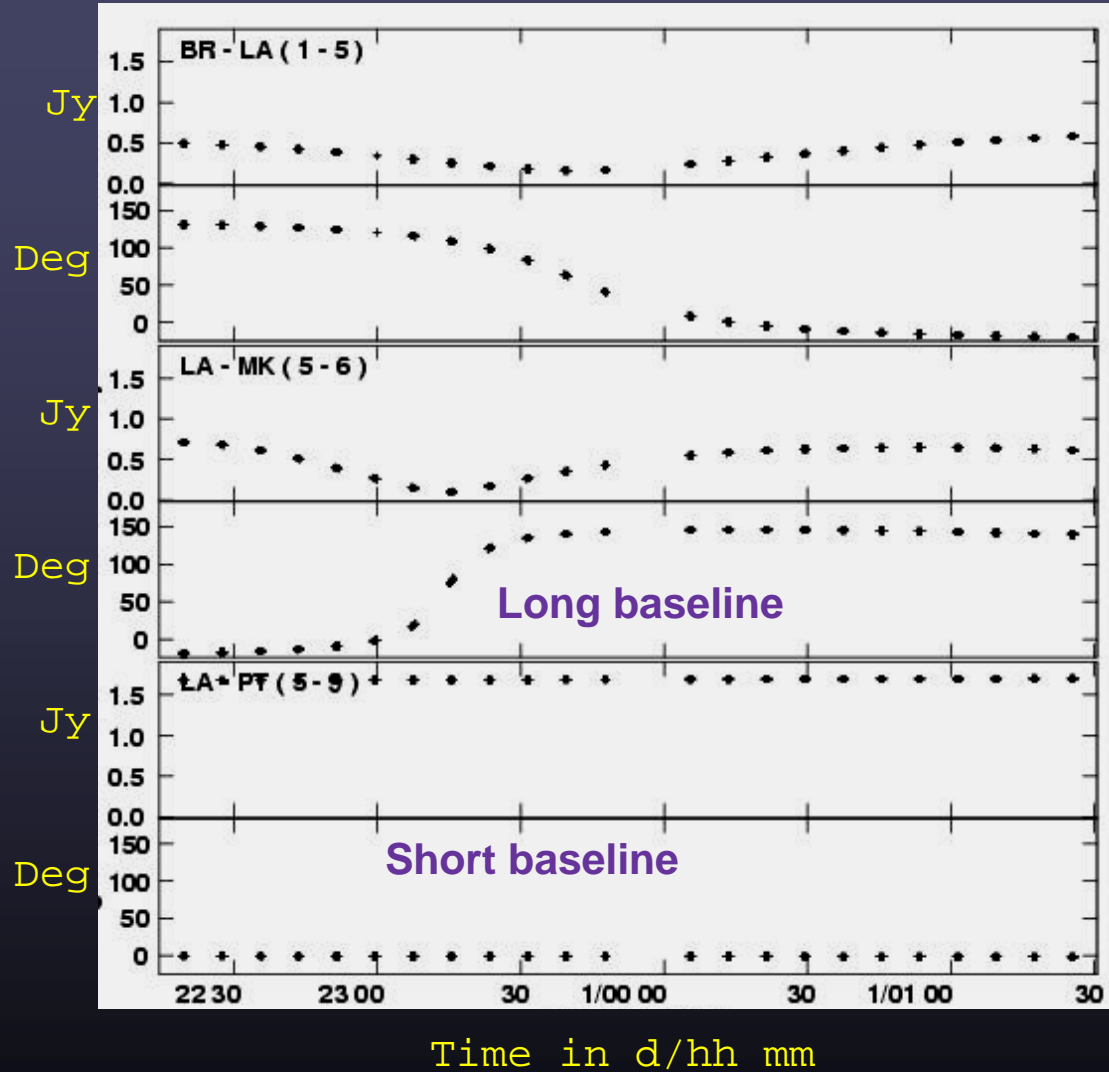
Triple source model.  
Large

component cause  
rise at

short spacings.

Oscillation at longer

# DATA DISPLAYS (3)

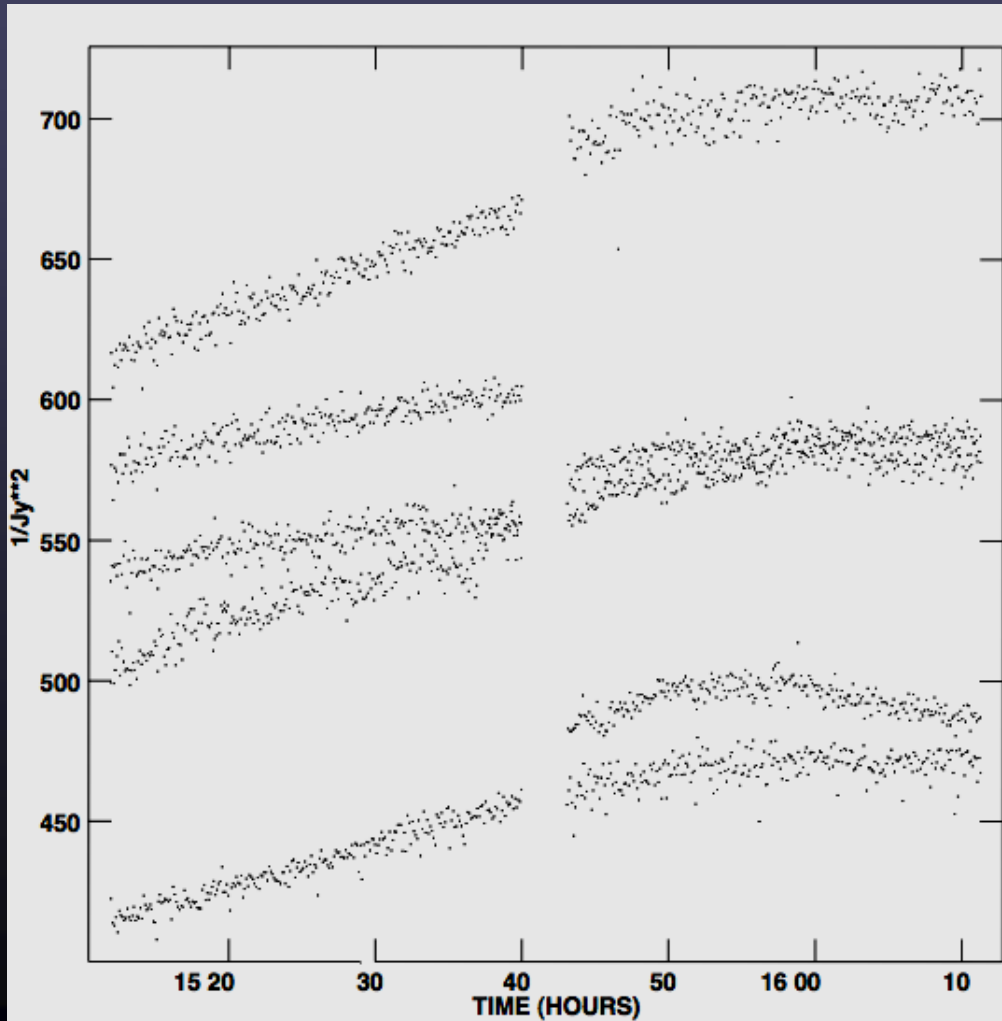


Visibility amplitude and phase versus time for various baselines

Good for determining continuity of the  
Should be relatively  
with time.  
Outliers are obvious.

## DATA DISPLAYS ( 4 )

Weights of antennas 4 with 5,6,7,8,9



All u-v data points have a weight. The weight depends on the antenna sensitivity, measured during the observations.

The amplitude calibration values also modify the weights.

Occasionally the weight of the points become very large, often caused by subtle software bugs.

A large discrepant weight causes the same image artifacts as a large discrepant visibility value.

Please check weights to make sure they are reasonable.

# IMAGE PLANE OR DATA (U-V) PLANE INSPECTION?

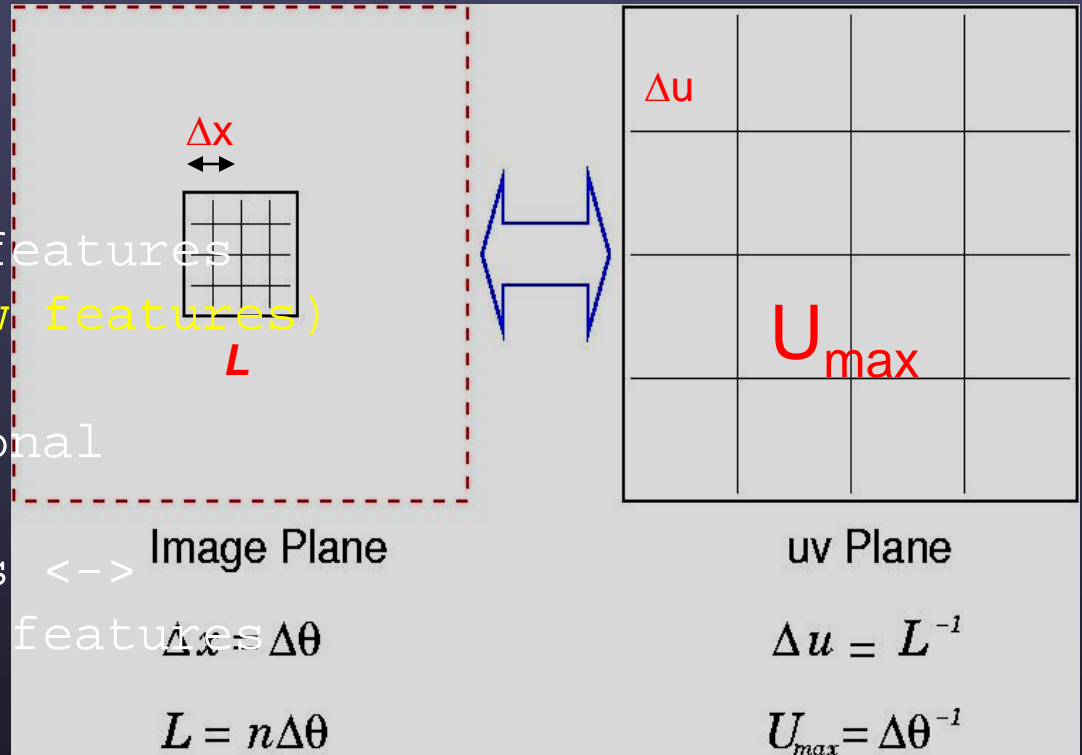
## Errors obey Fourier relationship

Narrow features  $\leftrightarrow$  Wide features  
(easier to find narrow features)

Orientations are orthogonal

Data uv amplitude errors  $\leftrightarrow$  symmetric image features

Data uv phase errors  $\leftrightarrow$  asymmetric image features



## GOLDEN RULE OF FINDING ERRORS

### ---Obvious outlier data (u-v) points:

100 bad points in 100,000 data points gives an  
0.1% image error

(unless the bad data points are 1 million Jy)

LOOK at DATA to find gross problem (but  
don't go overboard)

FURTHER OPPORTUNITIES TO FIND BAD DATA!

### ---Persistent small data errors:

egs a 5% antenna gain calibration error is  
difficult to see

in (u-v) data (not an obvious outlier), but  
will produce a

1% effect in image with specific



## ERROR RECOGNITION IN THE U-V PLANE

Editing obvious errors in the u-v plane

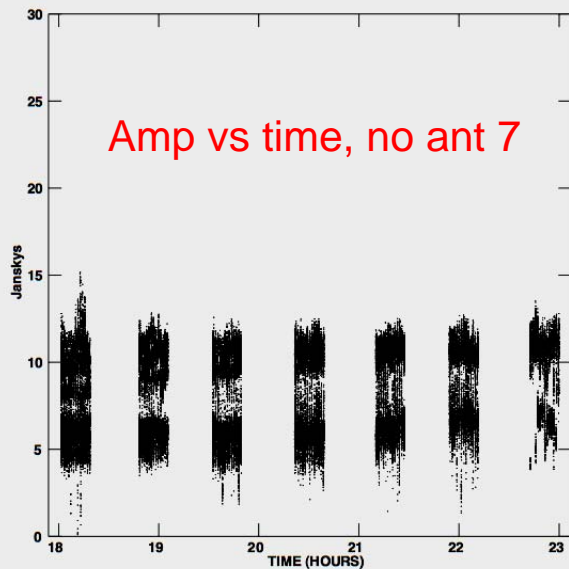
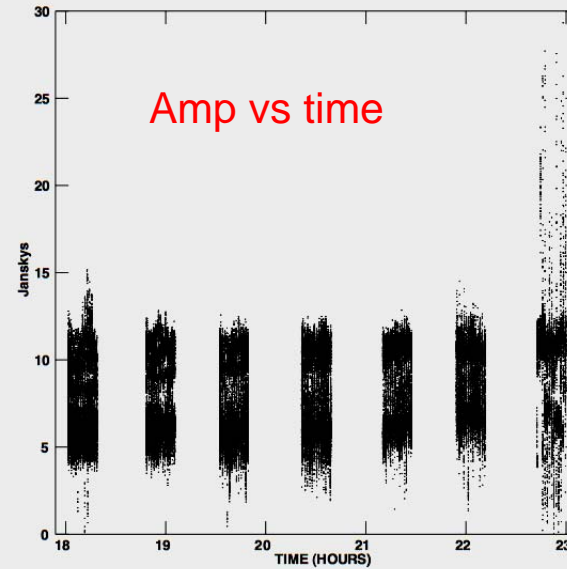
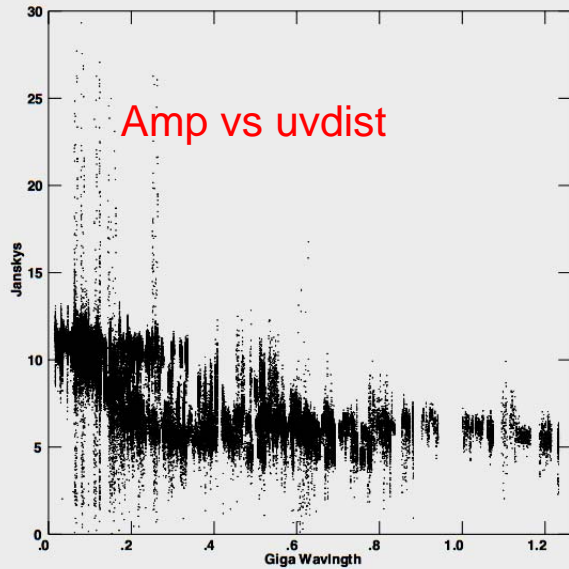
---Mostly consistency checks assume that the visibility cannot change much over a small change in u-v spacing

---Also, double check gains and phases from calibration processes. These values should be relatively stable.

See Summer school lecture notes in 2002  
by Myers

See ASP Vol 180, Ekers, Lecture 15,  
p321

# VISIBILITY AMPLITUDE PLOTS



Amp vs uvdist shows outliers

Amp vs time shows outliers in last scan

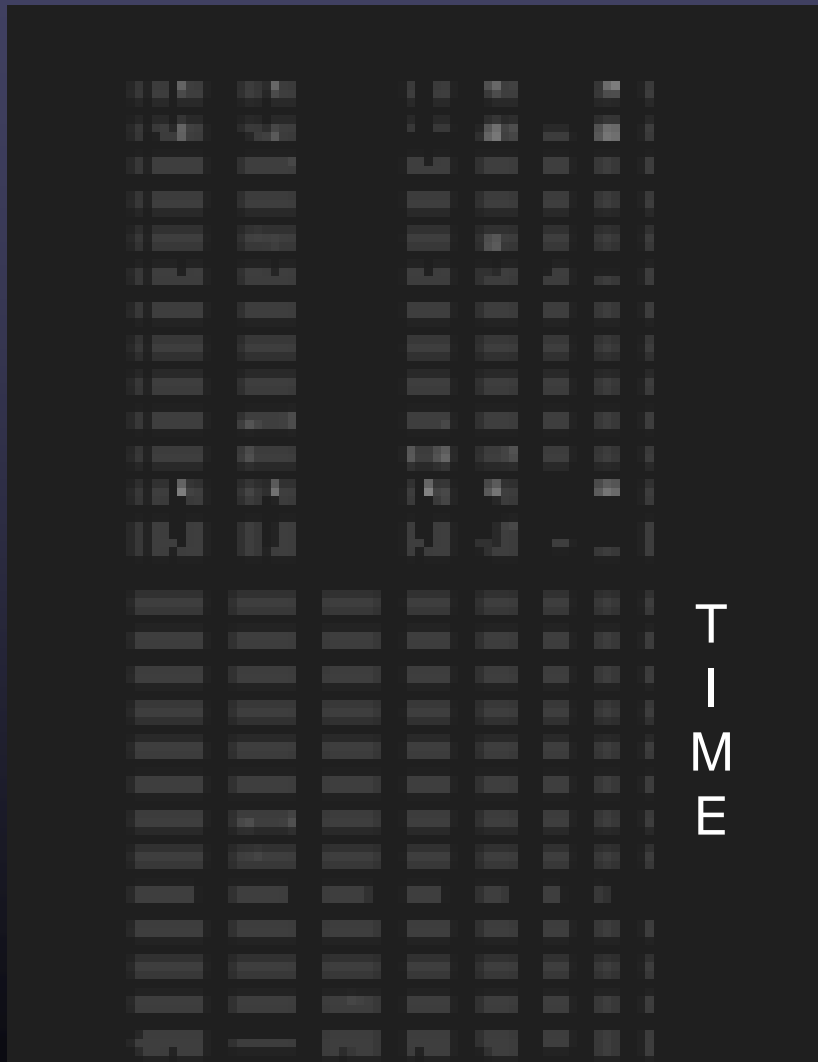
Amp vs time without ant 7 should good data

(3C279 VLBA data at 43 GHz)

# VISIBILITY AMPLITUDE RASTERS

BASELINE

Ant 1 2 3 4 5 6 7 8



(Last two scans from previous slide)

Use AIPS task TVFLG, CASA viewer

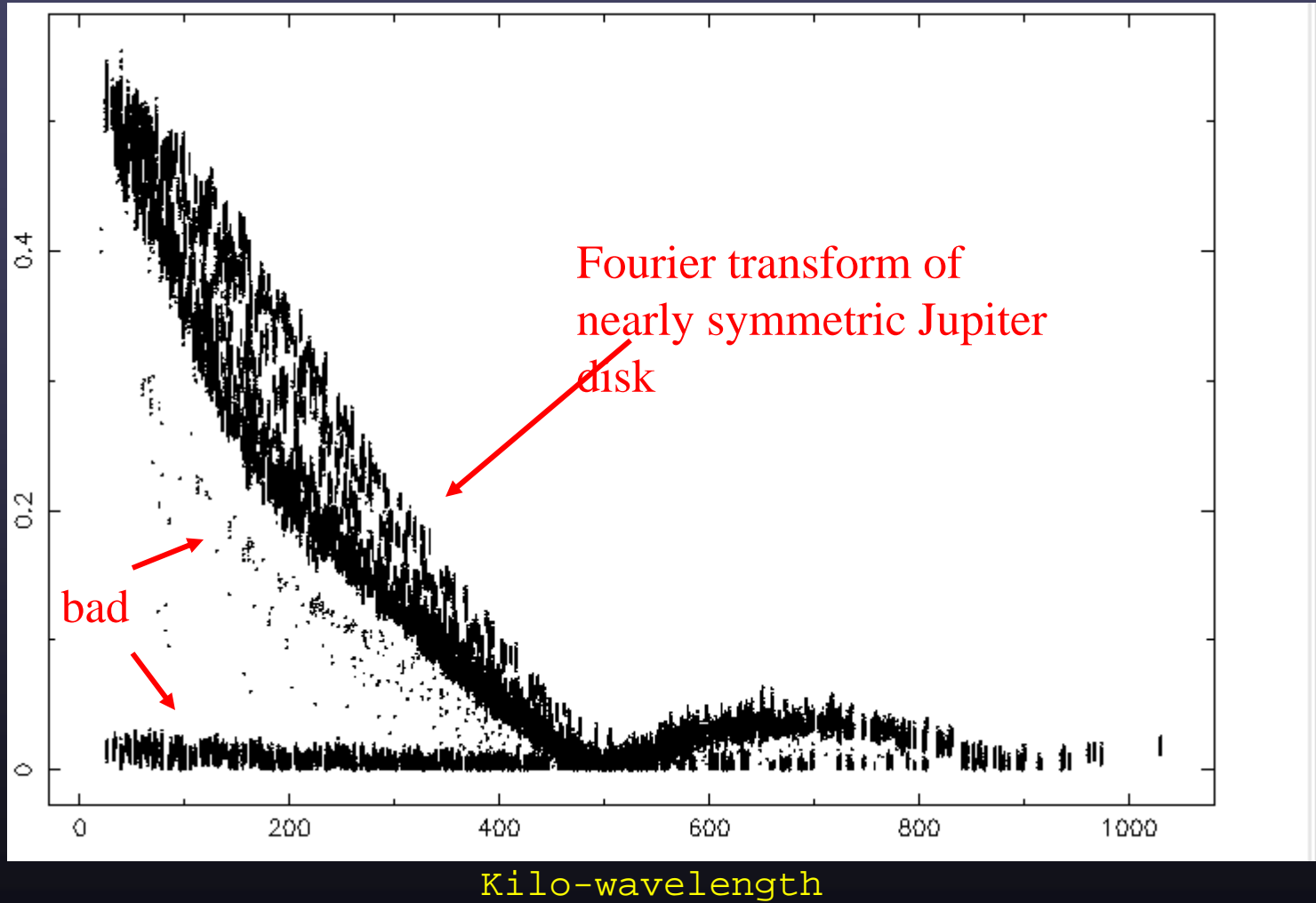
Raster scan of baseline versus time immediately shows where the bad data are

Pixel range is 5 to 20 Jy

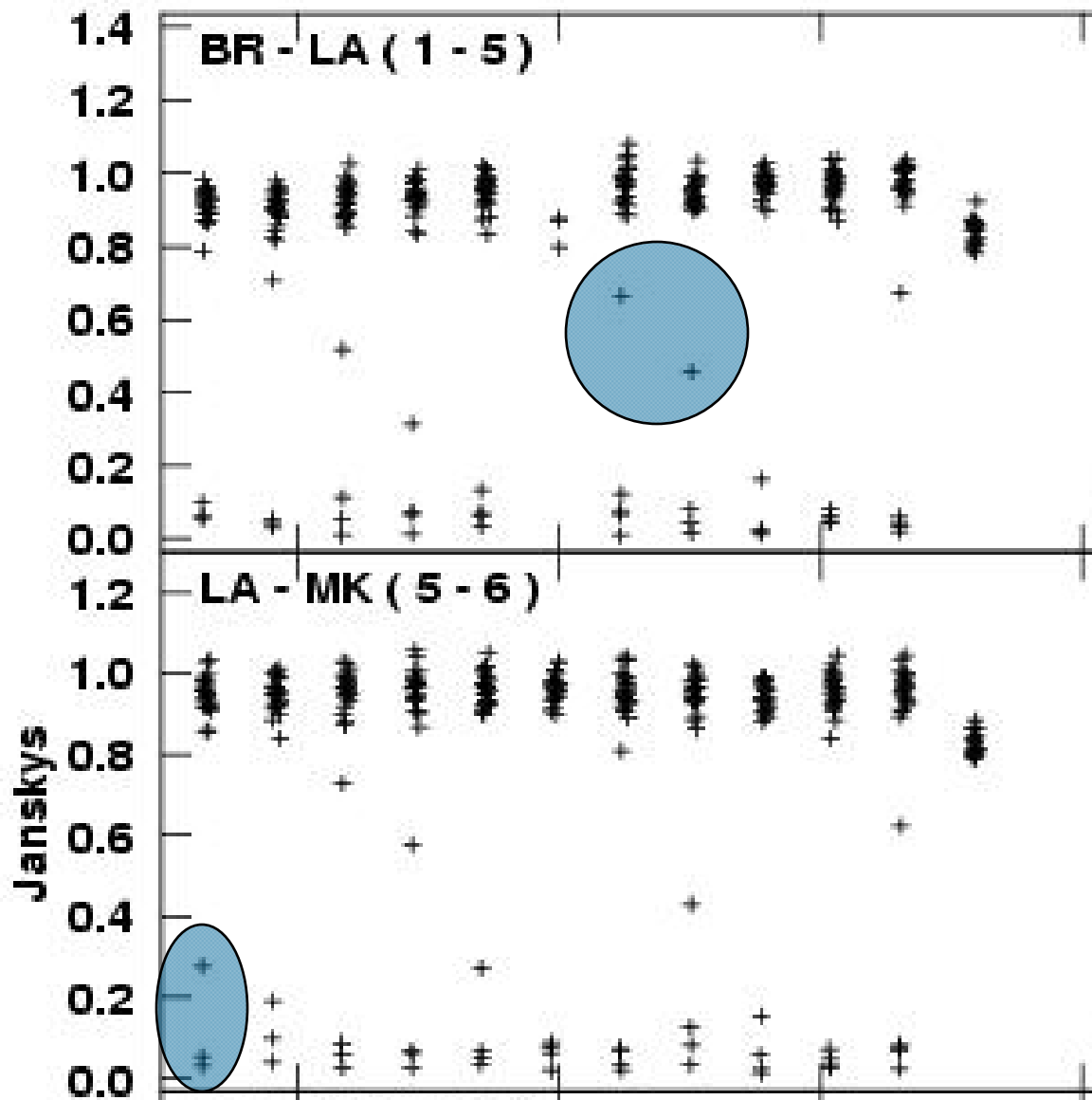
Bad data can be flagged with an interactive clipping control

Example Edit - msplot  
(2)

Jansky



# Drop-outs at Scan Beginnings



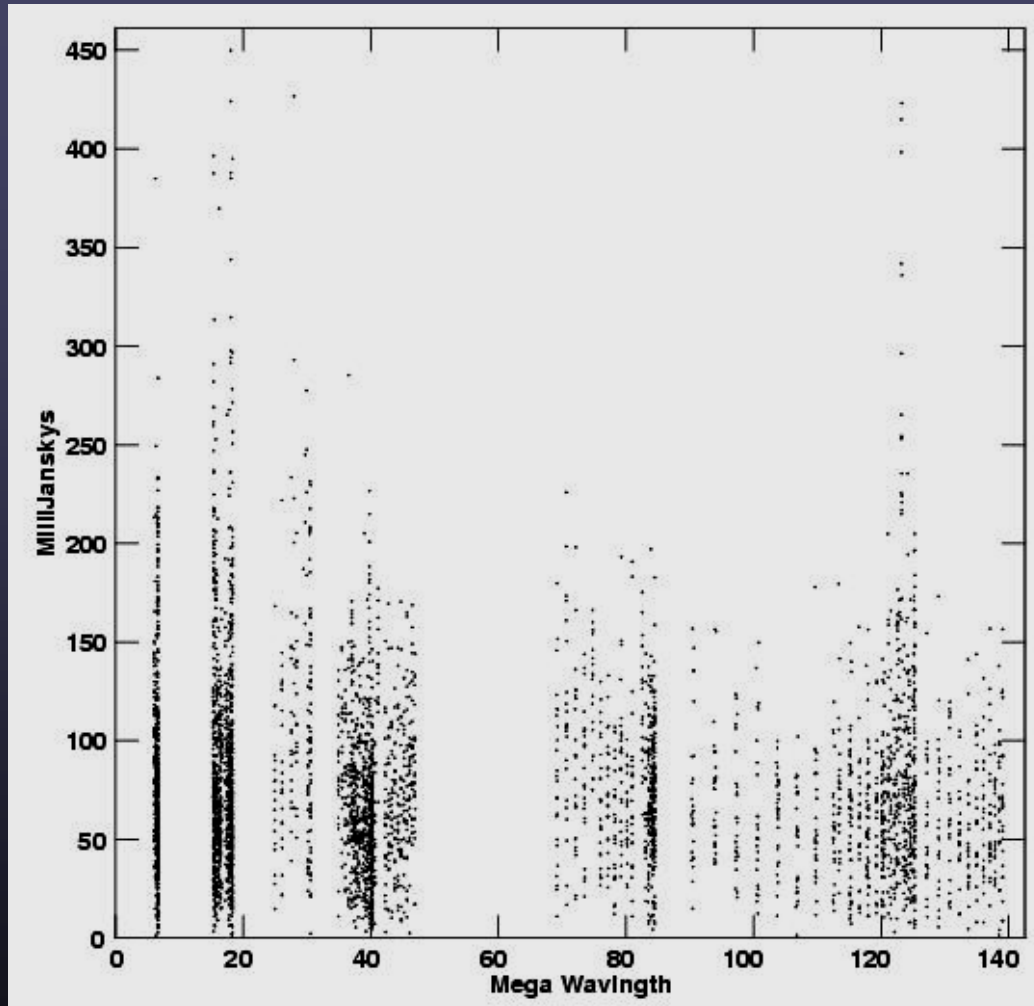
Often the first few points of a scan are low. Egs. antenna not on source.

Software can remove these points (aips,casa 'quack')

## Flag extension:

Should flag all sources in the same manner even though you cannot see dropout for weak sources

# Editing Noise-dominated Sources



No source structure  
information is  
detected.

Noise dominated.

All you can do is  
remove

outlier points  
above

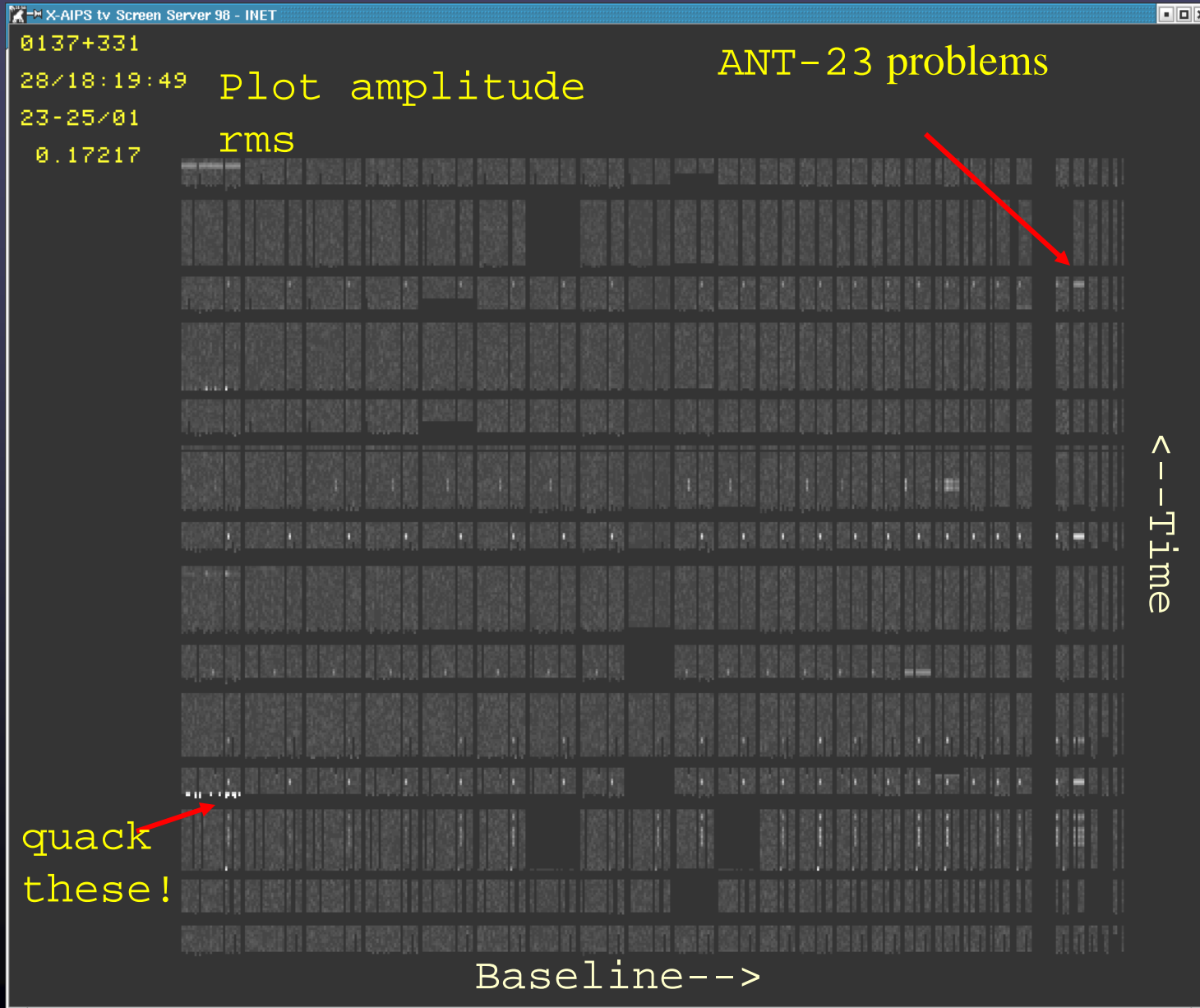
0.3 Jy. Precise  
level

not important as  
long

as large outliers  
removed.

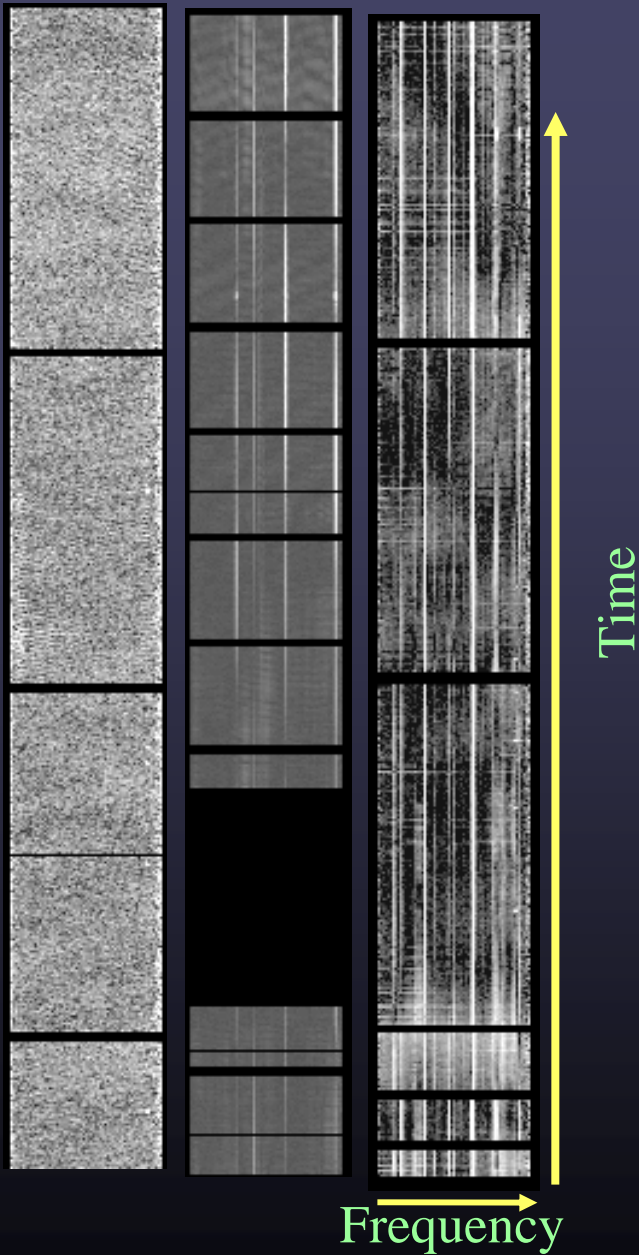


# USING TVFLG (VIEWER) DISPLAY on a source



35 km 12 km 3 km baseline

# RFI Excision



AIPS: SPFLG

before after



RFI environment worse on short baselines

Several 'types': narrow band, wandering, wideband, ...

Wideband interference hard for automated routines

Example using AIPS tasks FLGIT, FLAGR

Unfortunately, still best done by hand!

# ERROR RECOGNITION IN THE IMAGE PLANE

Some Questions to ask?

Noise properties of image:

Is the rms noise about that expected from integration?  
Is the rms noise much larger near bright sources?  
Are there non-random noise components (faint wave

Funny looking Structure:

Non-physical features; stripes, rings, symmetric  
Negative features well-below 4xrms noise  
Does the image have characteristics in the dirty

Image-making parameters:

Is the image big enough to cover all significant  
Is cell size too large or too small? ~4 points p  
Is the resolution too high to detect most of the

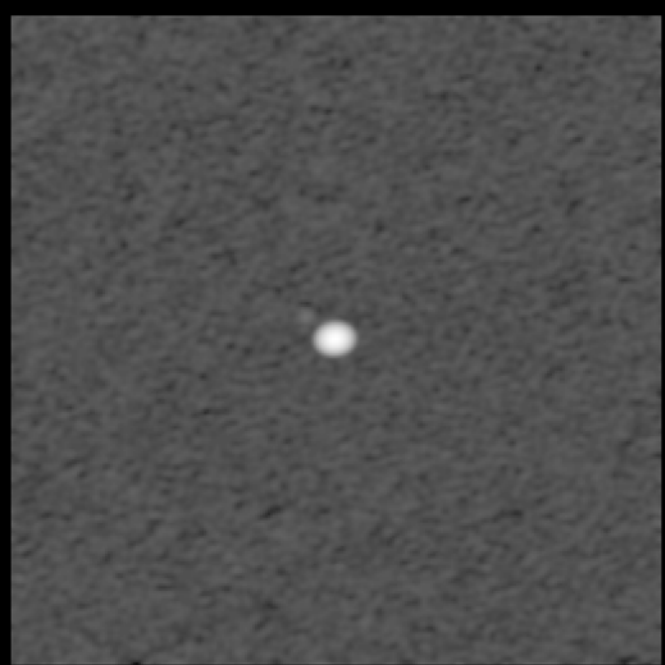
## Data bad over a short period of time

Results for a point source using VLA. 13-5min  
observation over 10 hr.

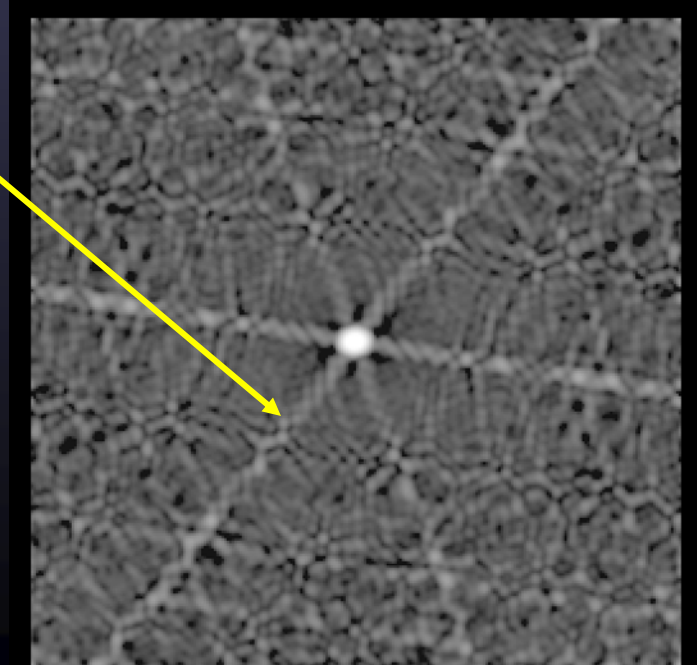
Images shown after editing, calibration and  
deconvolution.

no errors:  
max 3.24 Jy  
rms 0.11 mJy

10% amp error for  
all antennas for 1  
time period  
rms 2.0 mJy



6-fold  
symmetric  
pattern due  
to VLA "Y".  
Image has  
properties of  
dirty beam.

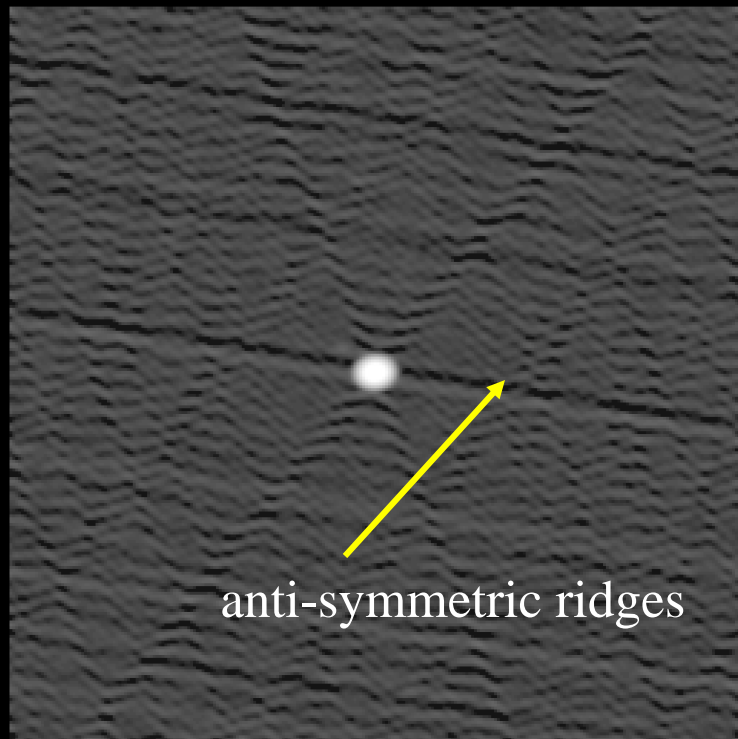


## EXAMPLE 2

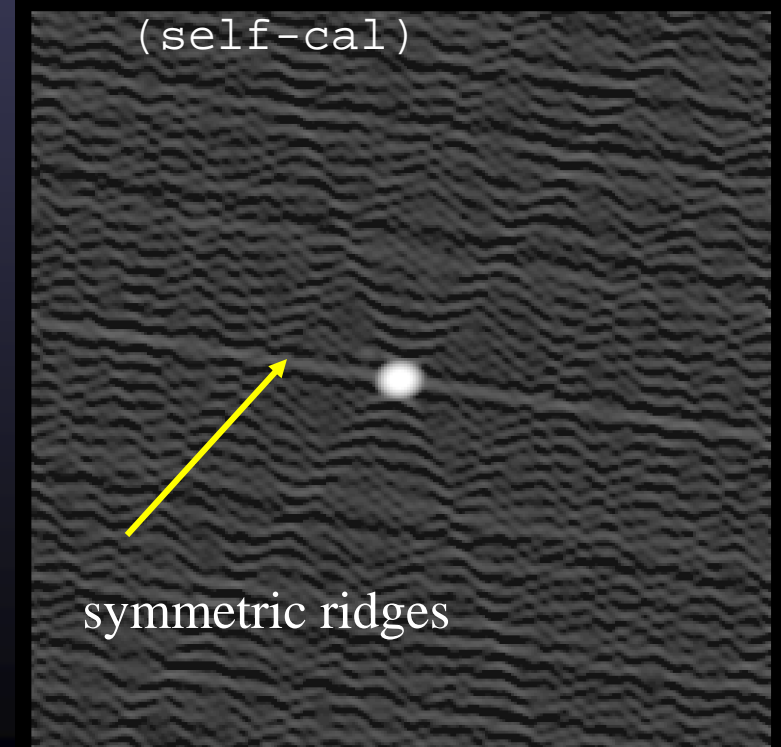
### Short burst of bad data

Typical effect from one bad u-v point:  
Data or weight

10 deg phase error  
for one antenna at  
one time  
rms 0.49 mJy



20% amplitude error  
for one antenna at  
1 time  
rms 0.56 mJy  
(self-cal)



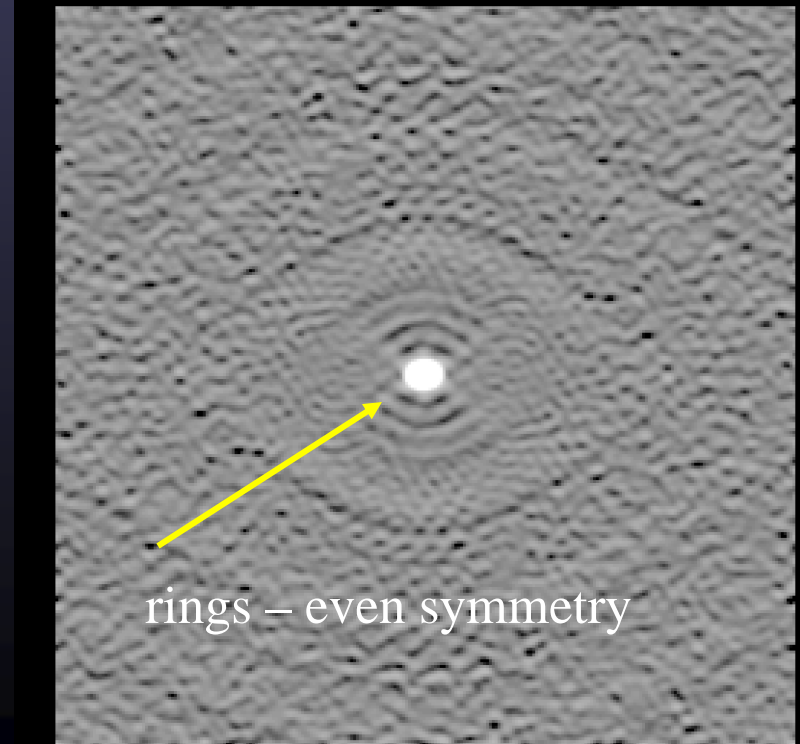
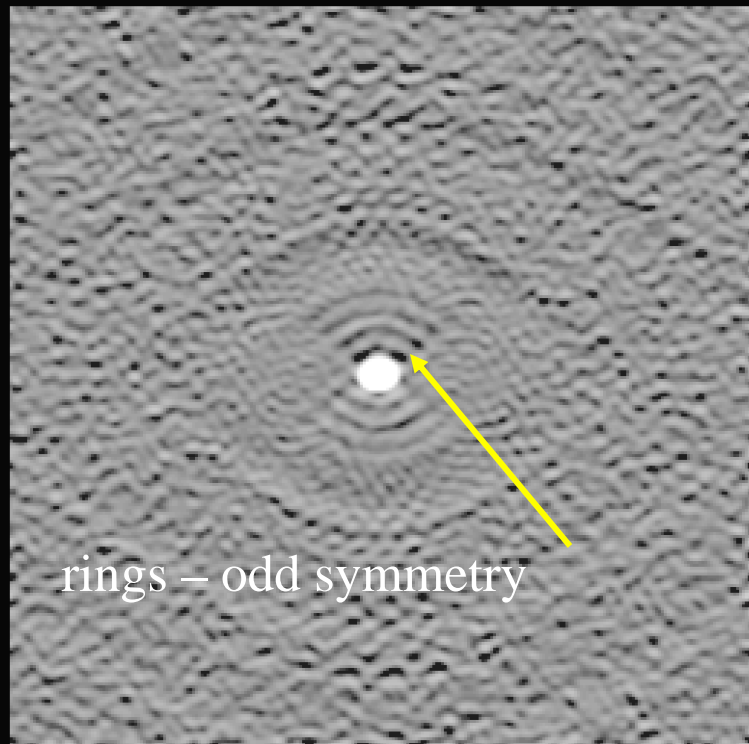
## EXAMPLE 3

### Persistent errors over most of observations

NOTE: 10 deg phase error to 20% amplitude error  
cause similar sized artifacts

10 deg phase error  
for one antenna  
all times  
rms 2.0 mJy

20% amp error for  
one antenna all  
times  
rms 2.3 mJy





## EXAMPLE 4

### Spurious Correlator Offset Signals

Occasionally correlators produce ghost signals or cross talk signals  
Occurred last year during change over from VLA to EVLA system

Symptom: Garbage near phase center, dribbling out into image

Image with correlator offsets

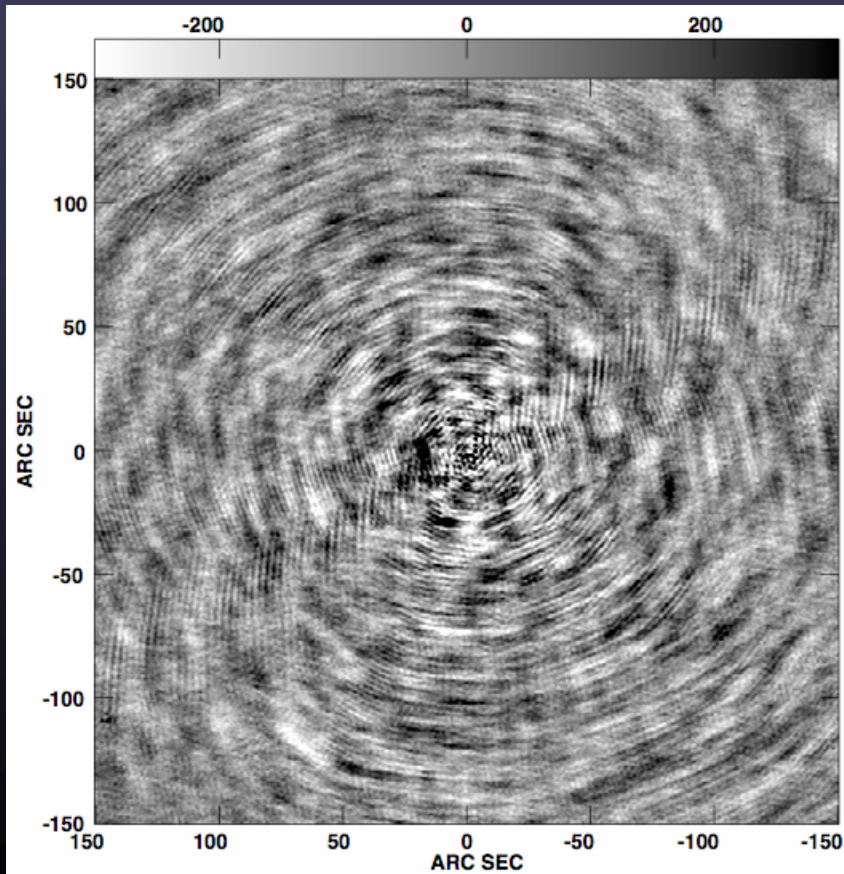
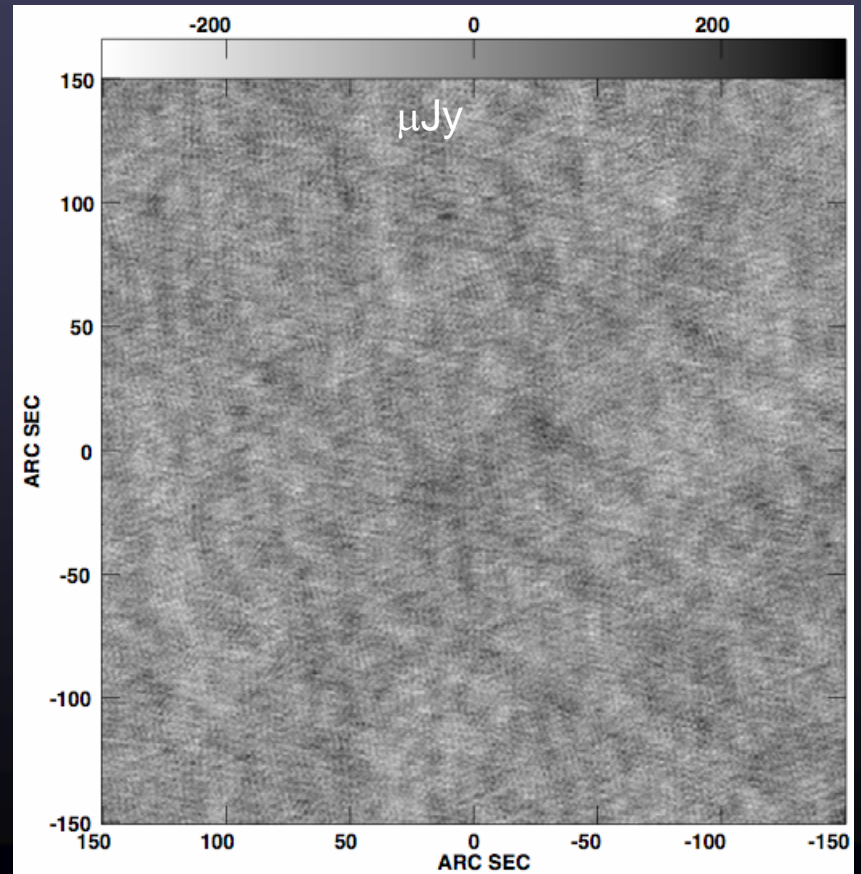
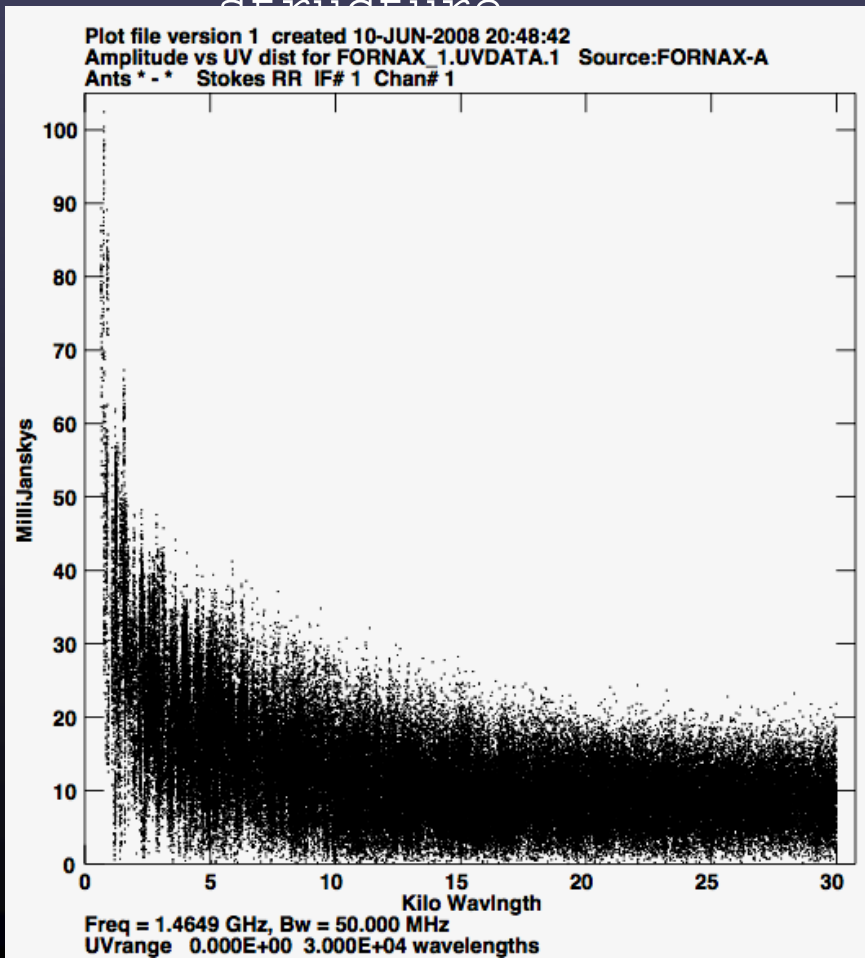


Image after correlation of offsets



## DECONVOLUTION ERRORS

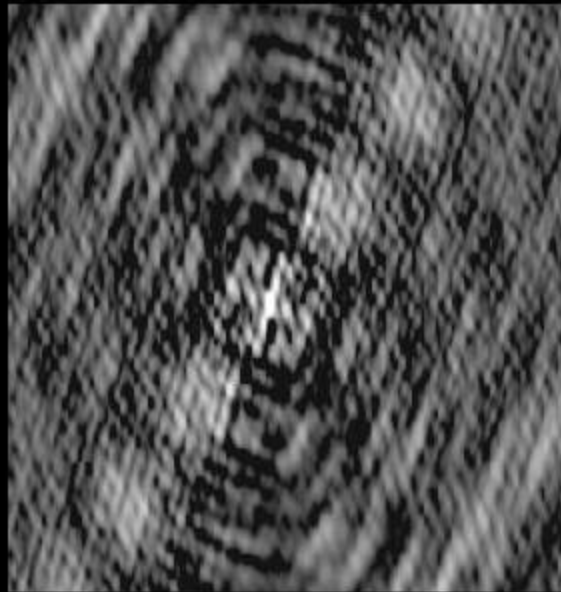
Even if the data are perfect, image errors and uncertainties will occur because the (u-v) coverage is not adequate to map the source structure



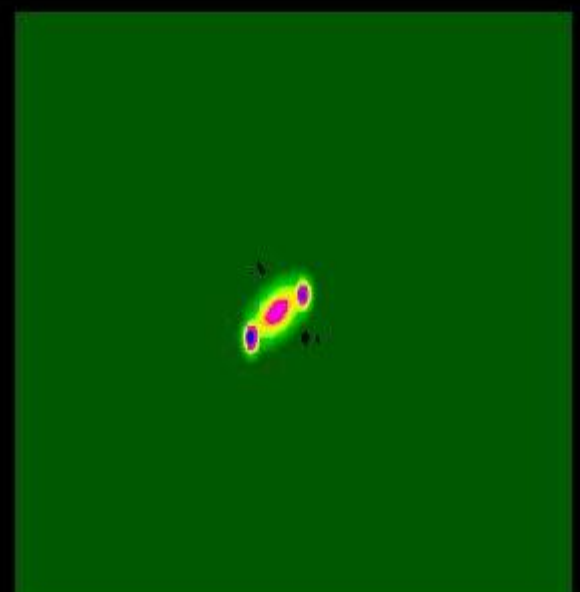
The extreme rise of visibility at the short spacings makes it impossible to image the extended structure. You are better of imaging the source with a cutoff below about 2 kilo-wavelengths

Get shorter spacing or single-dish data

# DIRTY IMAGE and BEAM (point spread function)



Dirty Beam



Dirty Image

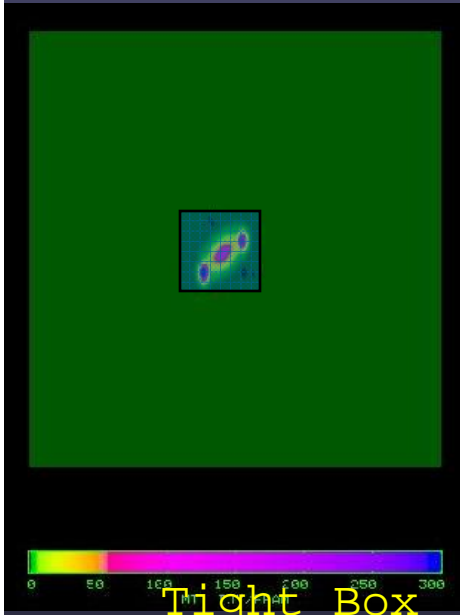


The dirty beam has large, complicated side-lobe structure.

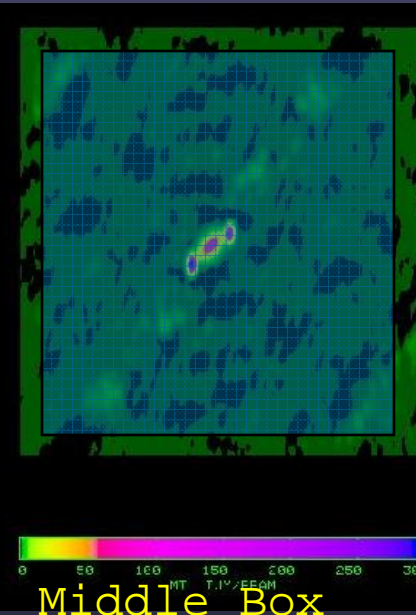
It is often difficult to recognize any details on the dirty image.

An extended source exaggerates the side-

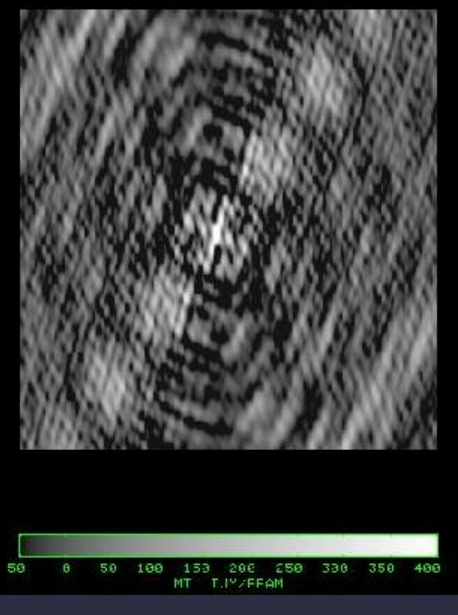
# CLEANING WINDOW SENSITIVITY



Big Box  
One small clean  
box  
(interactive clean  
shown next)



Dirty Beam  
One clean box  
around all emission



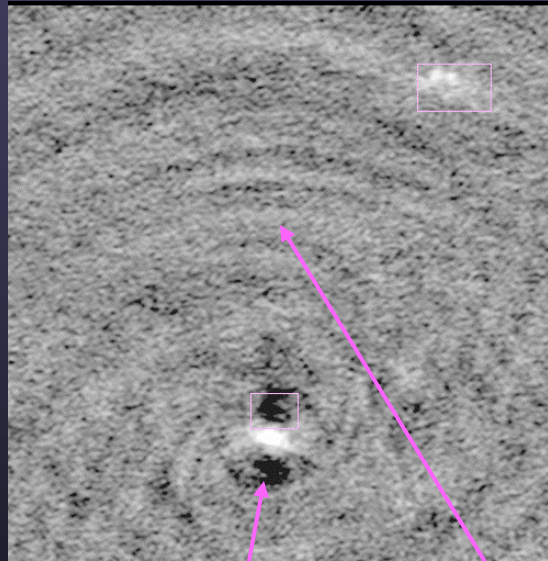
Clean entire  
inner map

*Spurious emission is always  
associated with higher  
sidelobes in dirty-beam.*



# How Deep to Clean?

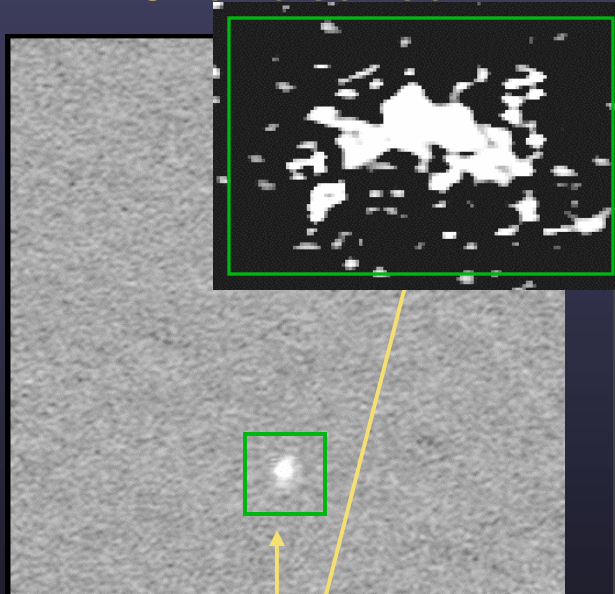
Under-cleaned



Emission from second source sits atop a negative "bowl"

Residual sidelobes dominate the noise

Over-cleaned



Regions within clean boxes appear "mottled"

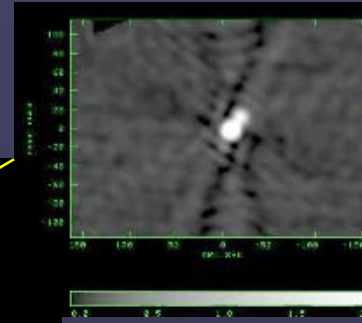
Properly cleaned



Background is thermal noise-dominated; no "bowls" around sources.

# FINDING HIDDEN BAD DATA

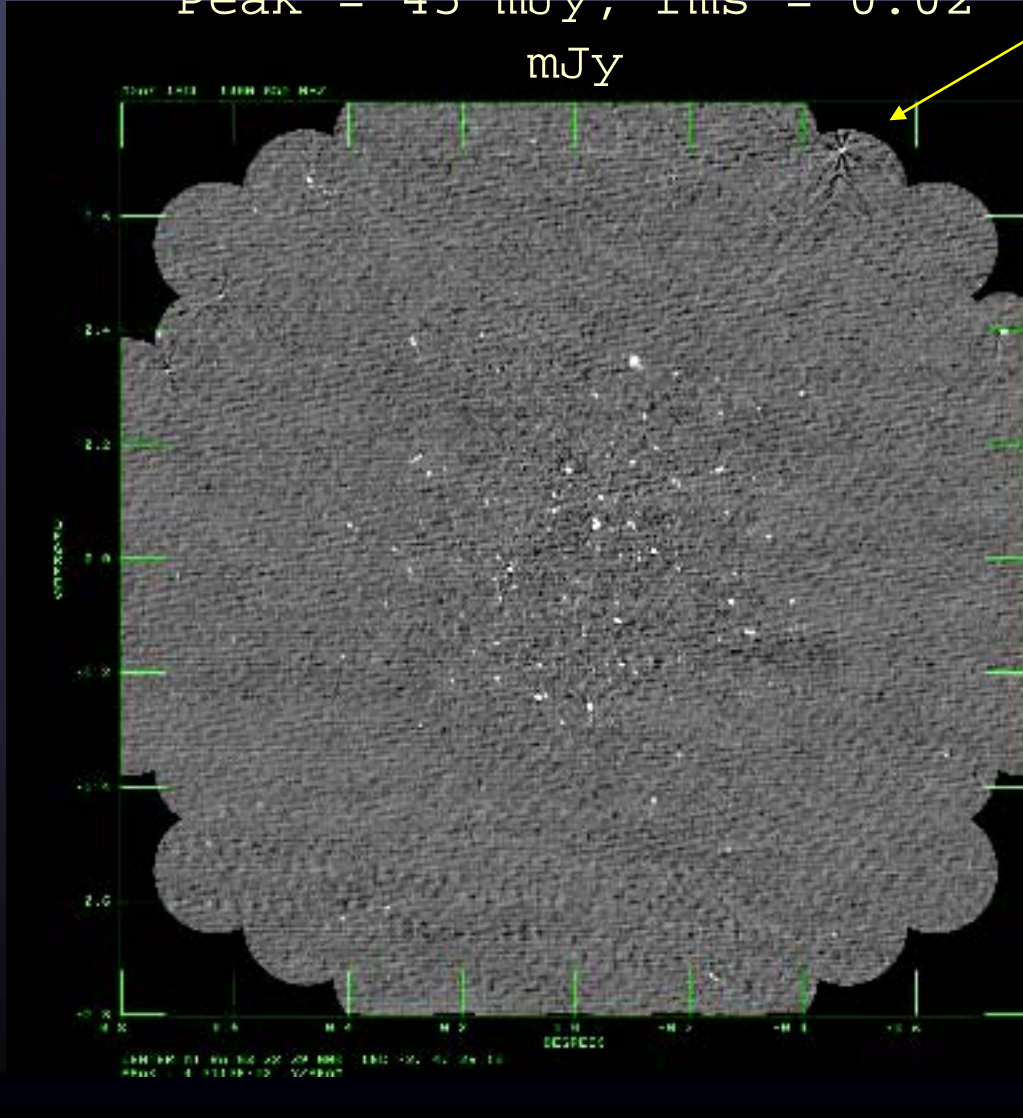
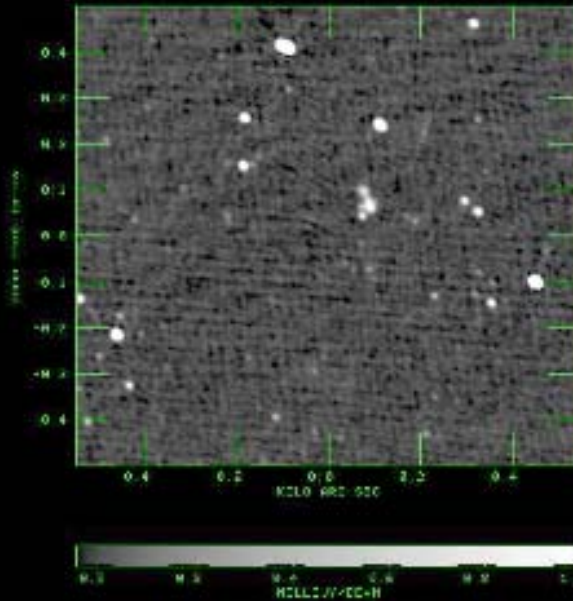
Chandra Deep Field South  
Peak = 45 mJy, rms = 0.02  
mJy



Source to NE in  
first  
Primary beam  
sidelobe

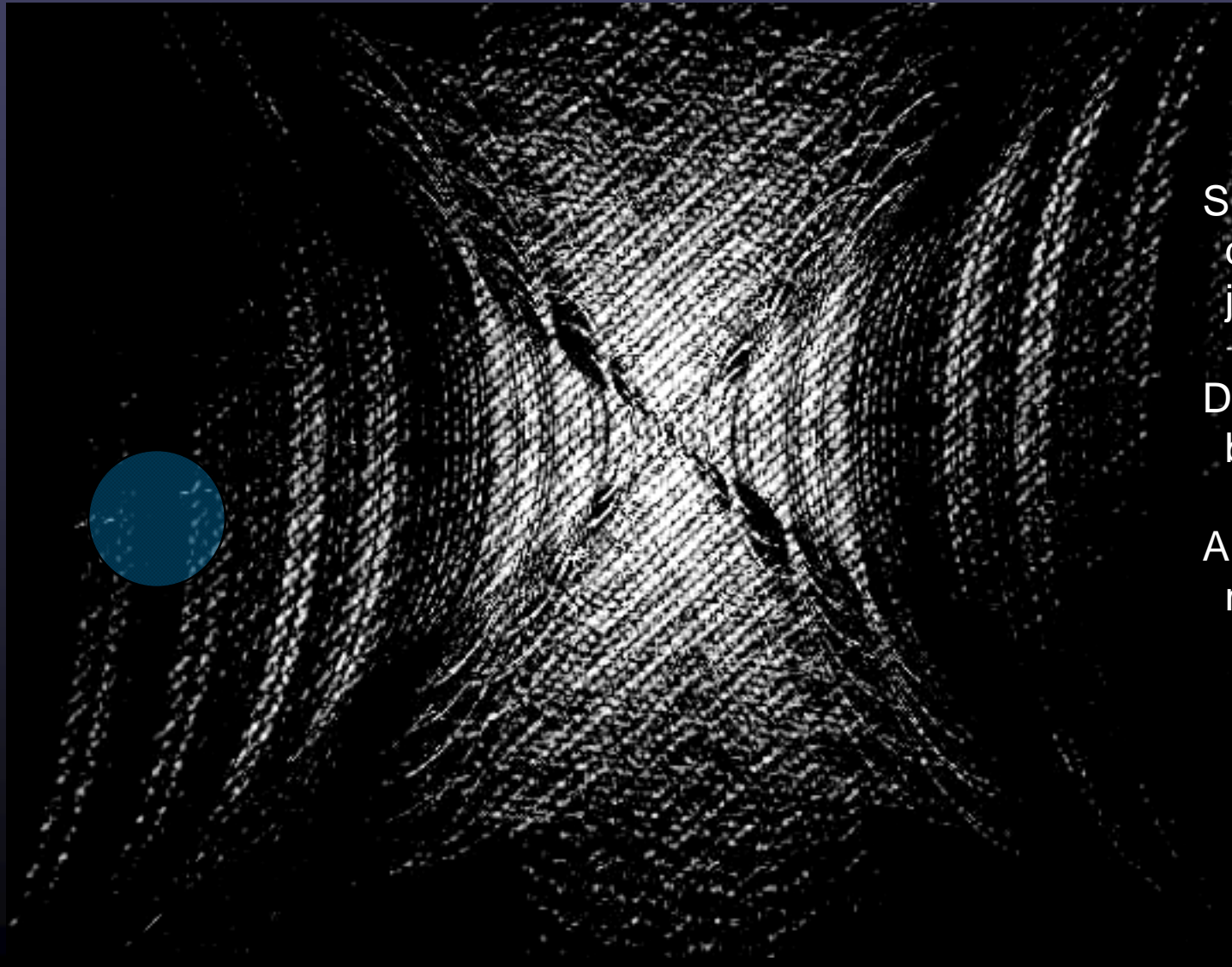
See Lectures  
Perley on  
Wide-field  
Imaging, and  
Uson on High  
dynamic Range  
Imaging

Center of Field





## Fourier Transform Dirty Image

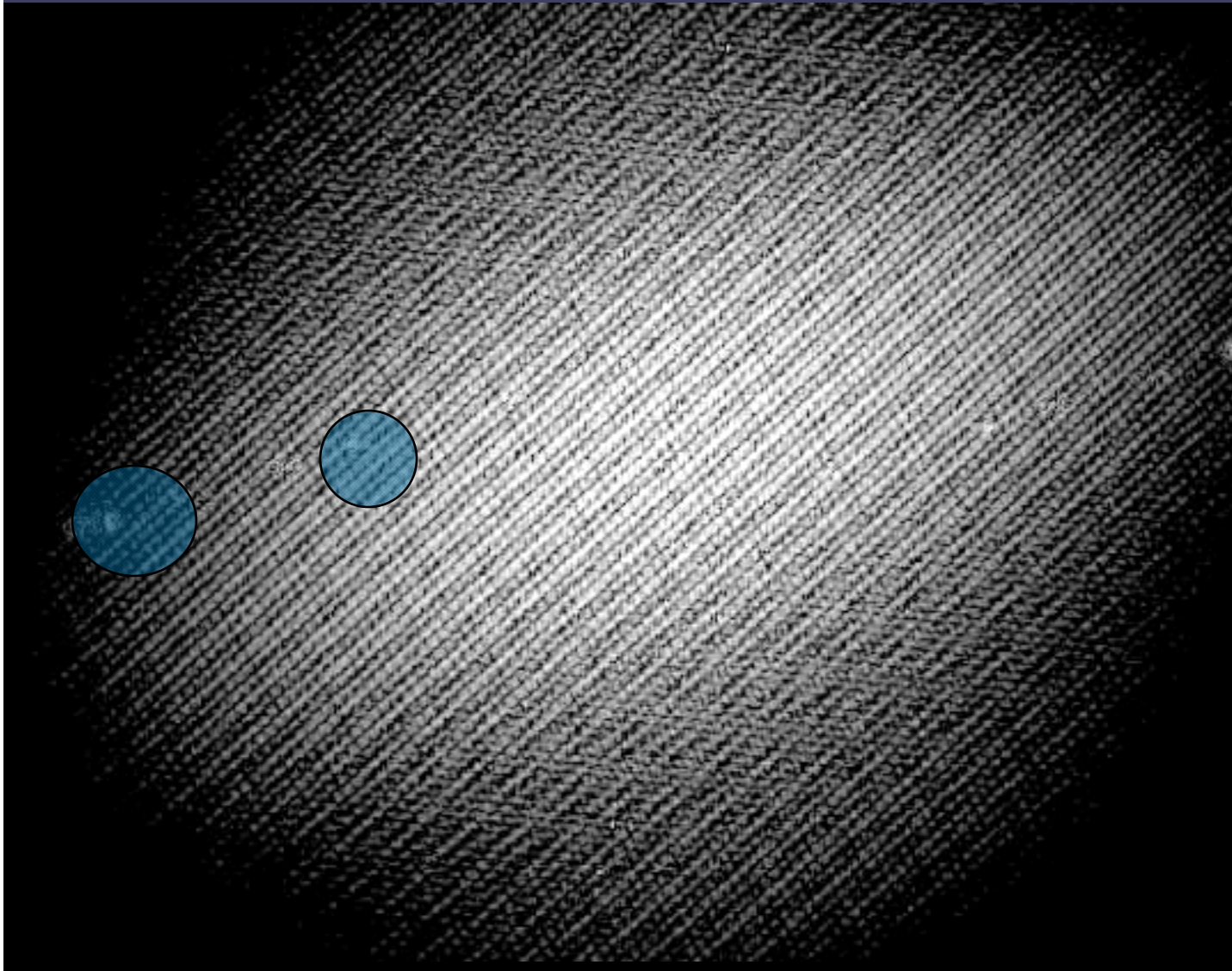


Shows the u-v  
data as gridded  
just before imaging

Diagonal lines caused  
by structure in field

A few odd points are  
not very noticeable

## Fourier Transform Clean Image

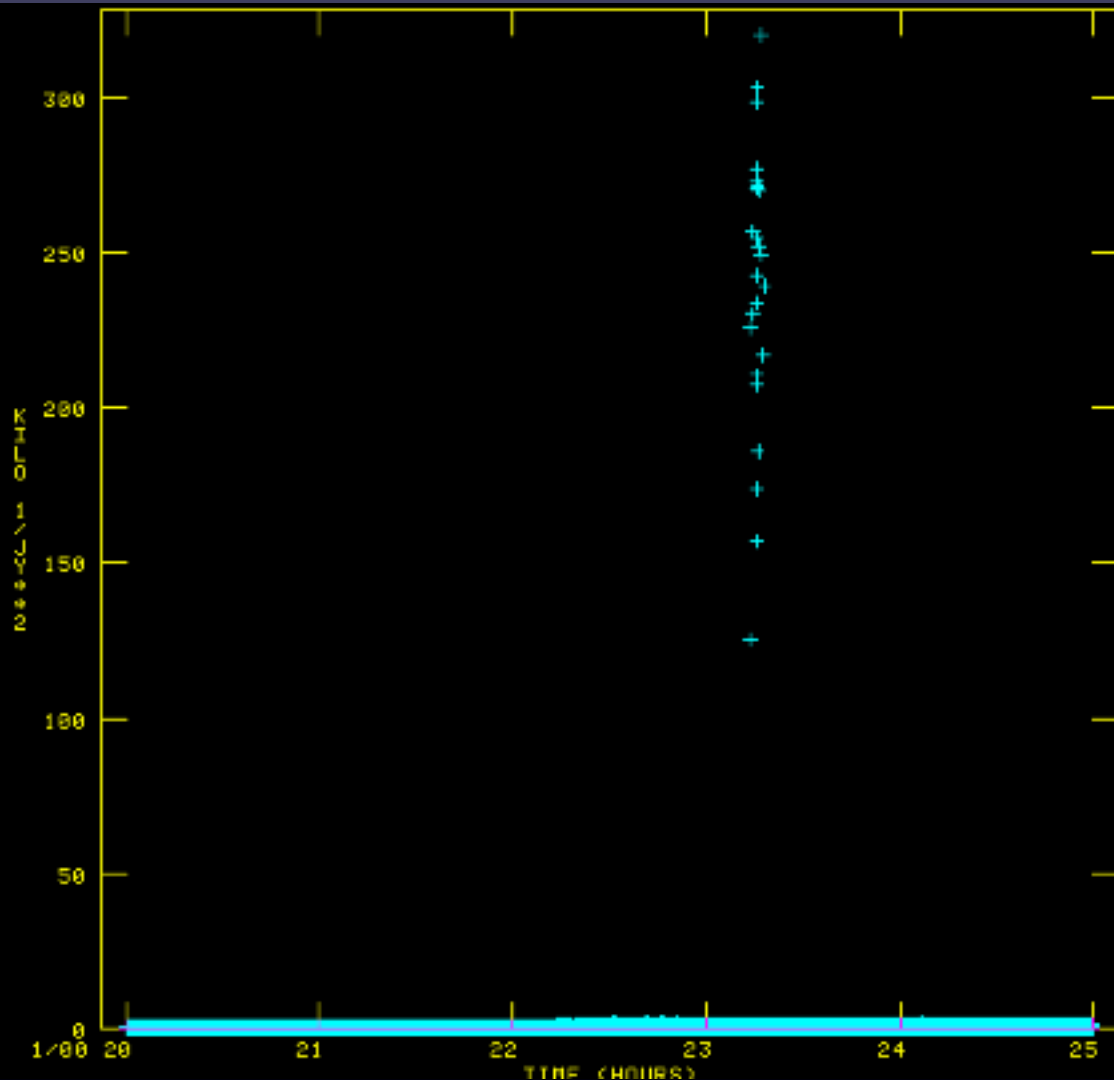


Shows the  $u$ - $v$  data from clean image.

Diagonal lines still present. Notice that clean does an interpolation in the  $u$ - $v$  plane between  $u$ - $v$  tracks.

The odd points are smeared, but still present. These produce the low level ripples.

## Bad weighting of a few u-v points



After a long search through the data, about 30 points out of 300,000 points were found to have too high of a weight by a factor of 100. Effect is <1% in image.

Cause??

Sometimes in applying calibration produced an incorrect weight in the data. Not present in the original data.

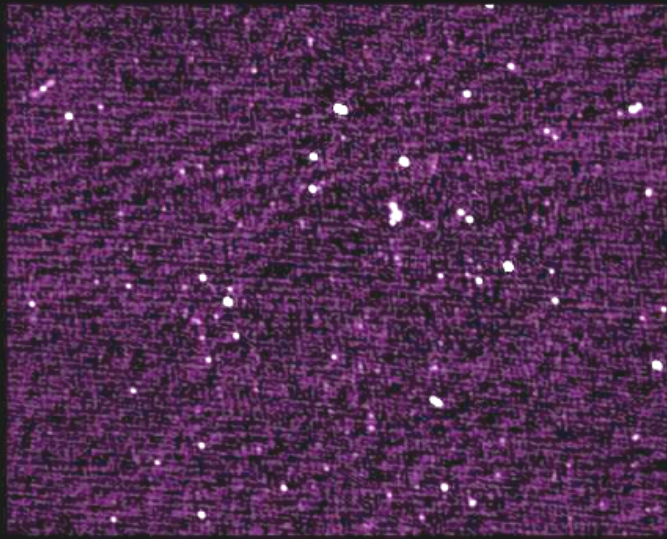
These problems can sneak up on you. Beware.



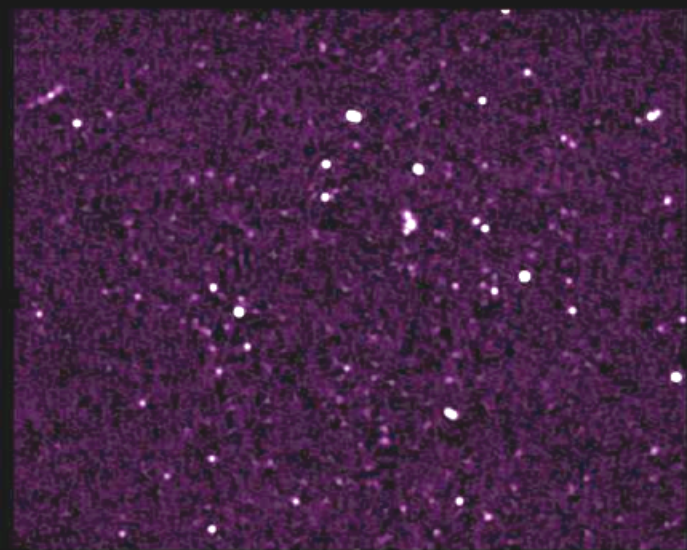
# Improvement of Image

Removal of low level ripple improves detectability of faint sources

Before editing



After editing



## SUMMARY OF ERROR RECOGNITION

Source structure should be 'reasonable', the rms im  
as expected, and the background featureless.

### UV data

Look for outliers in u-v data using several plotti

Check calibration gains and phases for instabili

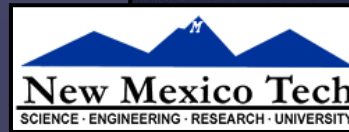
Look at residual data (uv-data - clean component

### IMAGE plane

Do defects resemble the dirty beam?

Are defect properties related to possible data e

Are defects related to possible deconvolution pr



# IMAGE ANALYSIS

**Ed Fomalont**

*Eleventh Synthesis Imaging Workshop  
Socorro, June 10-17, 2008*



# IMAGE ANALYSIS

- Input: Well-calibrated data-base producing a high quality image
- Output: Parameterization and interpretation of image or a set of images

This is very open-ended

Depends on source  
emission complexity

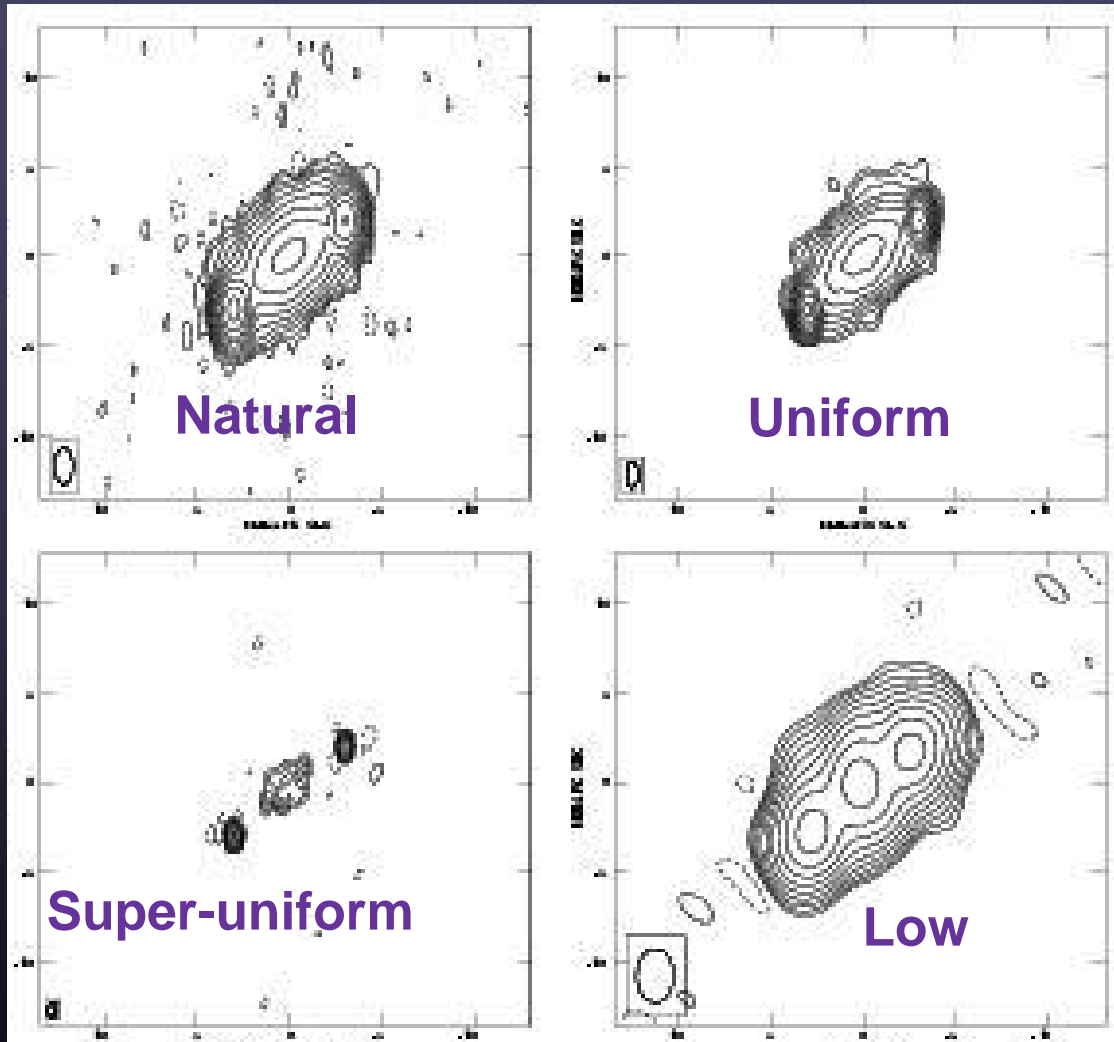
Depends on the  
scientific goals

## IMAGE ANALYSIS OUTLINE

- Multi-Resolution of radio source.
- Parameter Estimation of Discrete Components
- Polarization Data
- Image Comparisons
- Positional Registration



## IMAGE AT SEVERAL RESOLUTIONS



Different aspect of source structure can be see af various resolutions, shown by the ellipse in the lower left corner of each box.

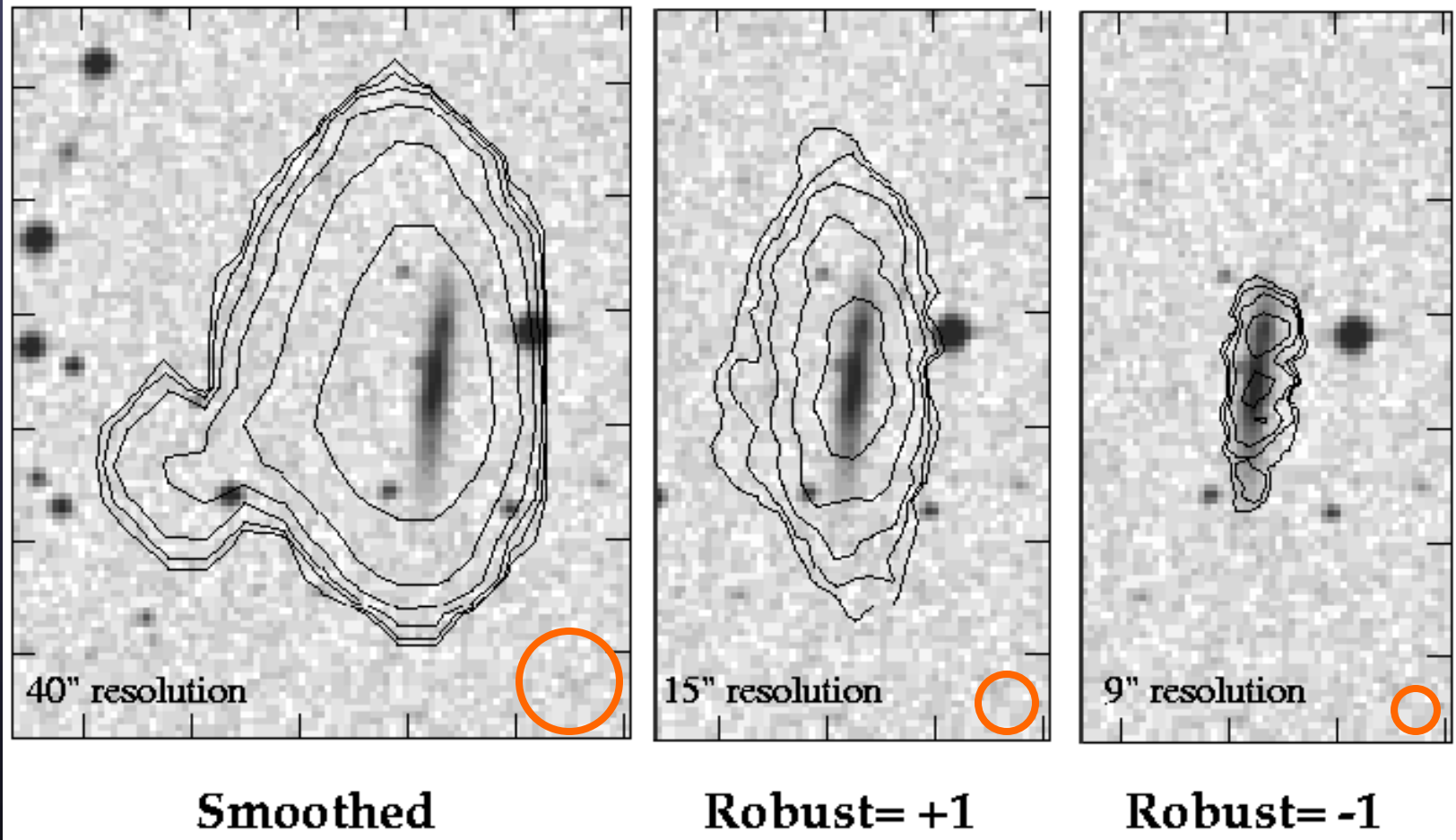
**SAME DATA USED FOR ALL IMAGES**

For example,  
Outer components are small from SU resolution  
There is no extended emission from low resolution

Milli-arcsec

# Imaging and Deconvolution of Spectral Line Data:

*Type of weighting in imaging*



HI contours overlaid on optical images of an edge-on galaxy

# PARAMETER ESTIMATION

Parameters associated with discrete components

- **Fitting in the image**
  - Assume source components are Gaussian-shaped
  - Deep cleaning restores image intensity with Gaussian-beam
  - True size \* Beam size = Image size, if Gaussian-shaped. Hence, estimate of true size is relatively simple.
- **Fitting in (u-v) plane**
  - Better estimates for small-diameter sources
  - Can fit to any source model (egs ring, disk)  
(see non-imaging analysis)
- **Error estimates of parameters**
  - Simple ad-hoc error estimates
  - Estimates from fitting programs

# IMAGE FITTING

## Component 2-Gaussian

Peak intensity = 0.104 +/- 0.005 JY/BEAM  
Integral intensity= 0.998 +/- 9.47 JANSKYS  
X-position = 255.986 +/- 0.0029 pixels  
Y-position = 257.033 +/- 0.0032 pixels  
Major ax 19.99 +/- 0.02 pixels  
Minor ax 9.98 +/- 0.03 pixels  
Pos ang 135.3 +/- 0.1 deg

## Component 1-Gaussian

Peak intensity = 0.300 +/- 0.005 JY/BEAM  
Integral intensity= 0.302 +/- 0.008 JANSKYS  
X-position = 270.991 +/- 0.001 pixels  
Y-position = 267.018 +/- 0.001 pixels  
Major ax 0.53 +/- 0.01 pixels  
Minor ax 0.00 +/- 0.05 pixels  
Pos ang 21.6 +/- 1.1 deg

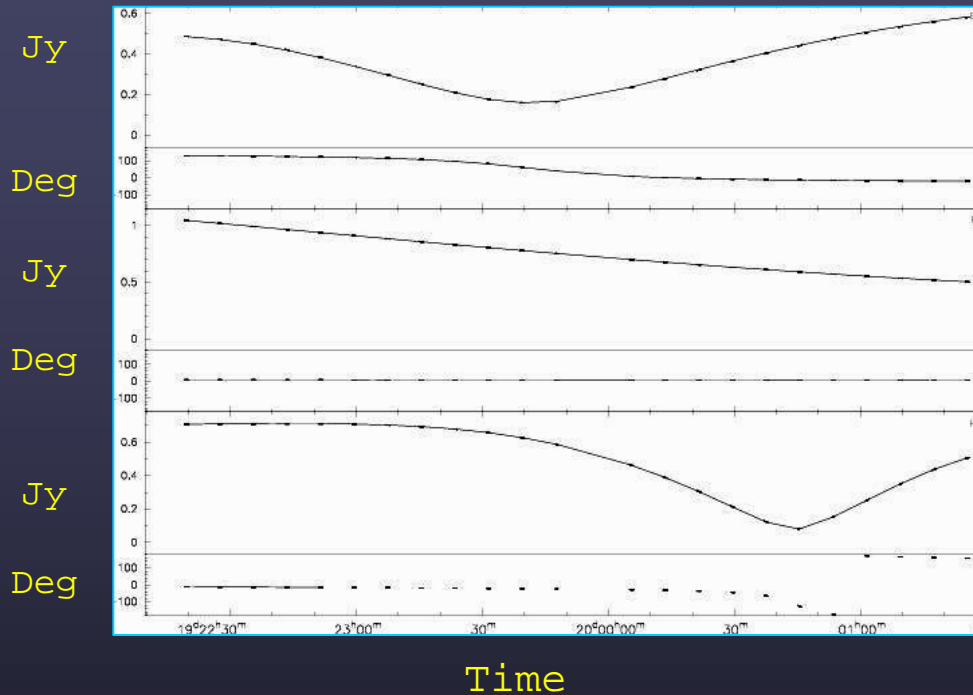
## Component 3-Gaussian

Peak intensity = 0.393 +/- 0.004 JY/BEAM  
Integral intensity= 0.403 +/- 0.008 JANSKYS  
X-position = 241.007 +/- 0.001 pixels  
Y-position = 241.988 +/- 0.001 pixels  
Major ax 1.54 +/- 0.01 pixels  
Minor ax 0.21 +/- 0.01 pixels  
Pos ang 3.6 +/- 0.2 deg

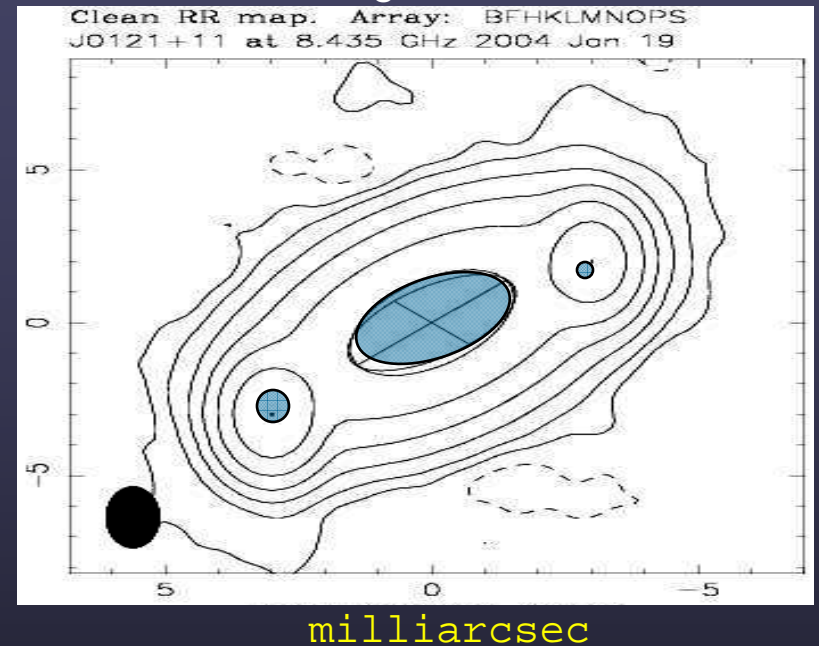
AIPS task: JMFIT  
Casa tool  
imfit

# (U-V) DATA FITTING

Amp and phase vs time for three baselines



Contour image with model fits



DIFMAP has good u-v fitting algorithm

Fit model directly to (u-v) data

Contour display of image

Compare mode to data

Ellipses show true component

Greg Taylor, Tuesday June 17, "Non-image Data Analysis"  
size. (super-resolution?)

## COMPONENT ERROR ESTIMATES

$P$  = Component Peak Flux Density

$\sigma$  = Image rms noise

$P/\sigma$  = signal/noise =  $S$

$B$  = Synthesized beam size

$\theta_i$  = Component image size

$\Delta P$  = Peak error =  $\sigma$

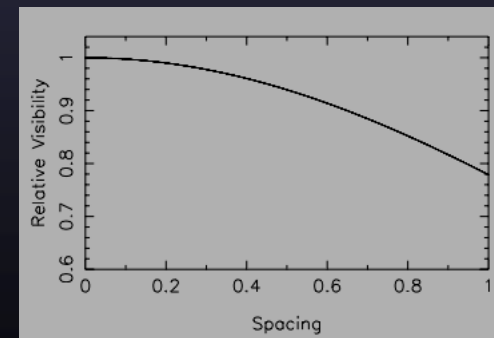
$\Delta X$  = Position error =  $B / 2S$

$\Delta \theta_i$  = Component image size error =  $B / 2S$

$\theta_t$  = True component size =  $(\theta_i^2 - B^2)^{1/2}$

$\Delta \theta_t$  = Minimum component size =  $B / S^{1/2}$

*eg.  $S=100$  means can determine size of  $B/10$*



# Comparison and Combination of Images of Many Types

## FORNAX-A Radio/Optical field

Radio is red  
Faint radio core  
in center of  
NGC1316

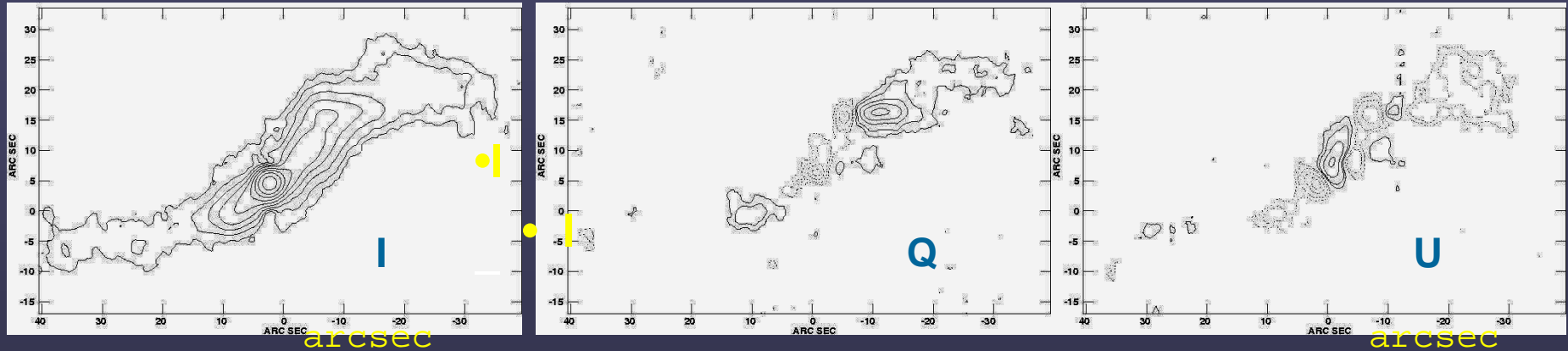
Optical in  
blue-white

Frame size is  
60' x 40'





# LINEAR POLARIZATION



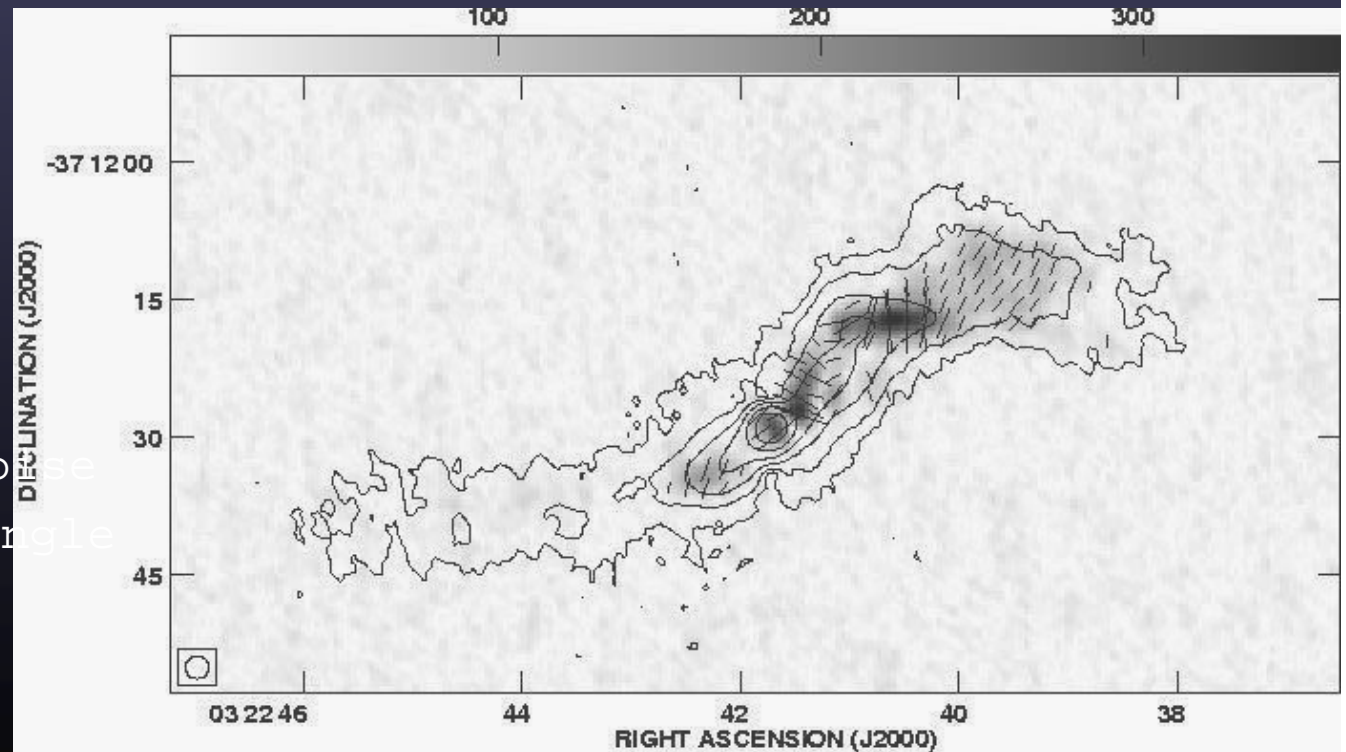
arcsec

arcsec

arcsec

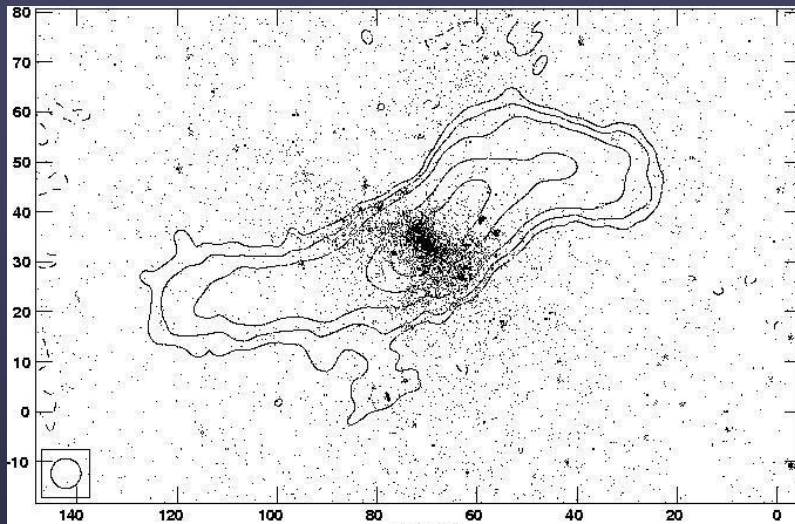
## Multi-purpose plot

Contour - I, Q, U Pol  
 Grey scale - P Pol  
 $\sqrt{Q^2+U^2}$  - noise  
 Line segments - P angle  
 $\text{atan2}(0.5*Q/U)$



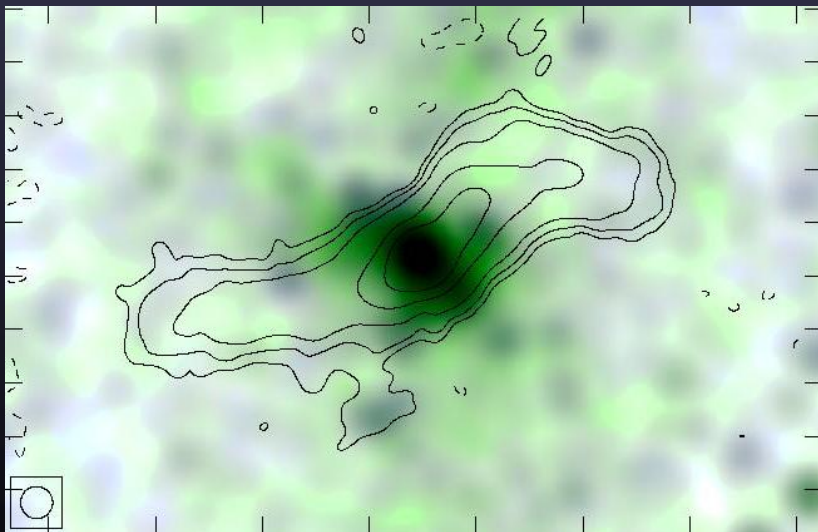


## COMPARISON OF RADIO/X-RAY IMAGES



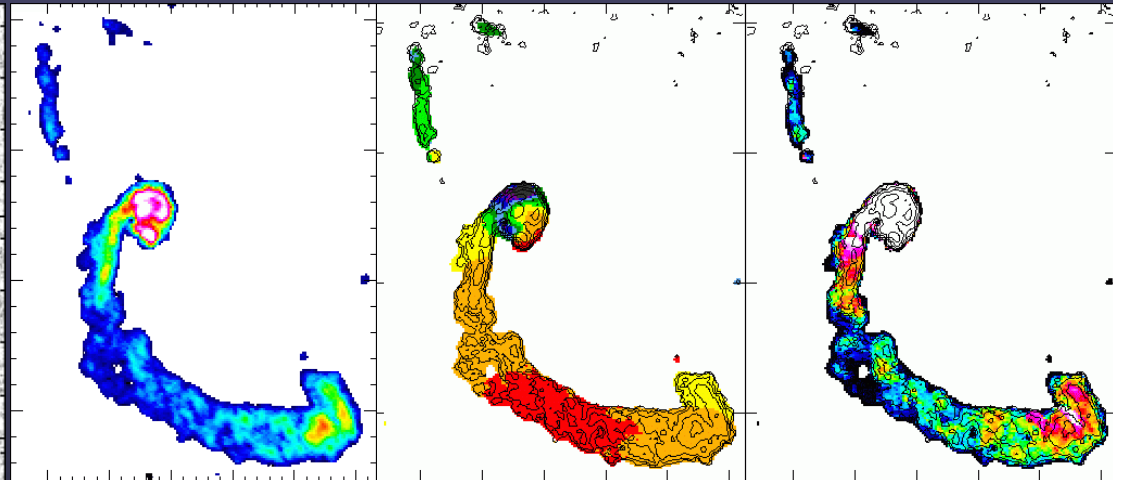
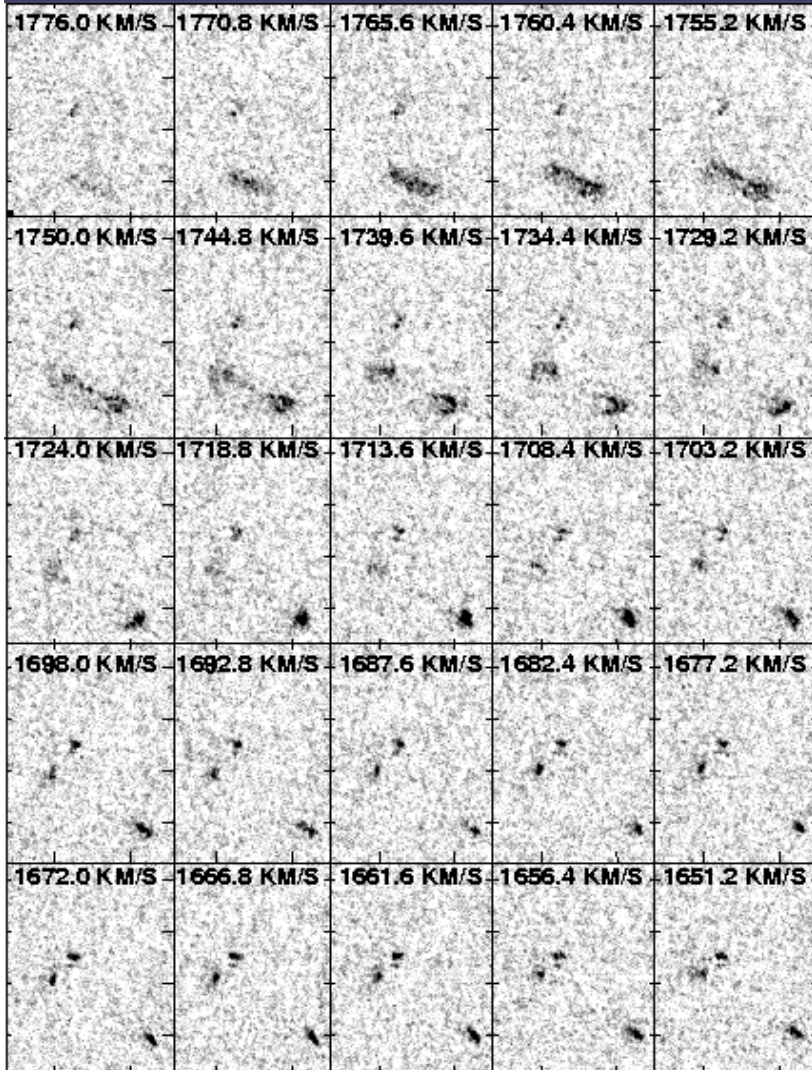
arcsec

Contours of radio  
intensity at 5 GHz  
Dots represent X-ray  
Intensity (photons)  
between 0.7 and 11.0 KeV



Contours of radio  
intensity at 5 GHz  
Color intensity represents  
X-ray intensity smooth  
to radio resolution  
Color represents hardness  
of X-ray (average  
weighted frequency)  
Blue - soft  
(thermal)

# SPECTRAL LINE REPRESENTATIONS



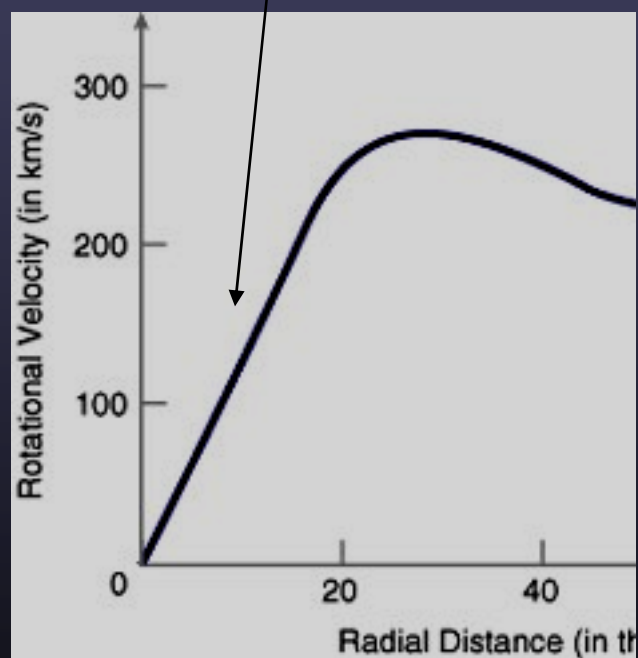
Intensity Image  
Sum of velocity  
Amount of HI  
Red high,  
Blue low

Average velocity  
Red low vel  
Blue high vel  
Rotation

Second moment  
Velocity width  
Turbulence?

# SPECTRAL LINE ROTATION MOVIES

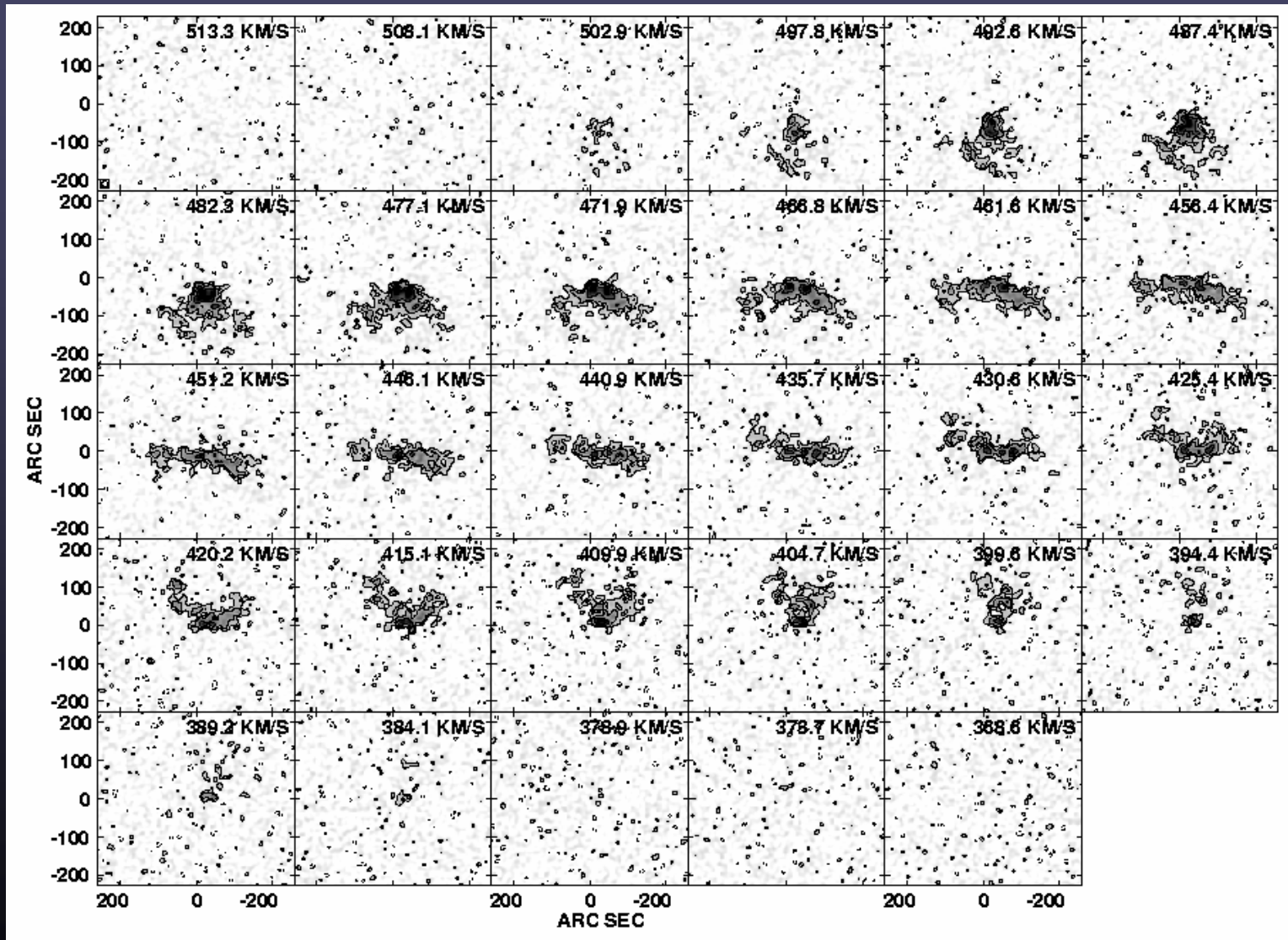
Solid-body Rotation in Inner parts of a galaxy



QuickTime™ and a YUV420 codec decompressor are needed to see this picture.

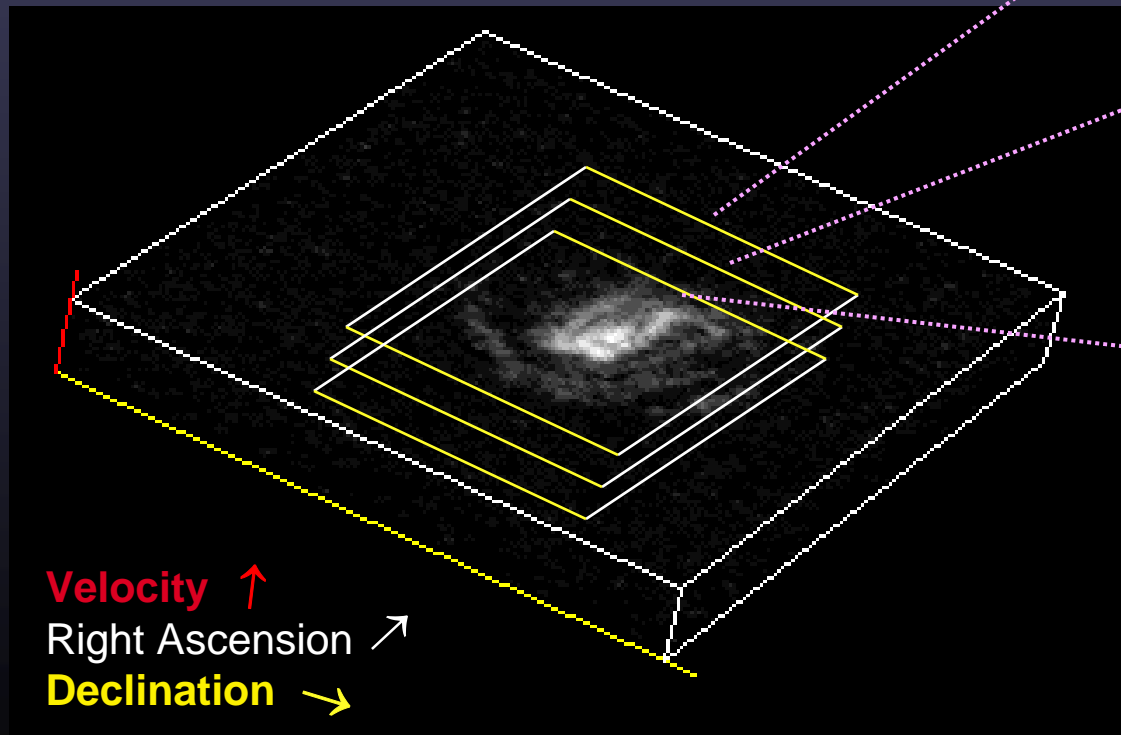
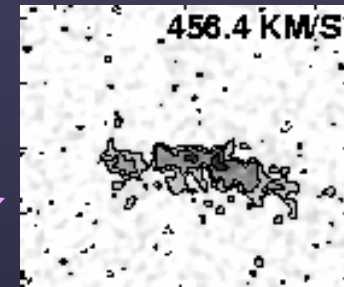


# Visualizing Spectral Line Data: Channel Images



Greyscale+contour representations of individual channel images

# Visualizing Spectral Line Data: Channel Images



# IMAGE REGISTRATION AND ACCURACY

- Separation Accuracy of Components on One Image:

Limited by signal to noise to 1% of resolution.

Position errors of 1:10000 for wide fields, i.e. 0.1" over 1.4 GHz PB

- Images at Different Frequencies:

Multi-frequency. Use same calibrator for all frequencies.

Watch out at frequencies < 2 GHz when ionosphere can

produce displacement. Minimize calibrator-target separation

- Images at Different Times (different configuration):

Use same calibrator for all observations. Daily troposphere changes

can produce position changes up to 25% of the

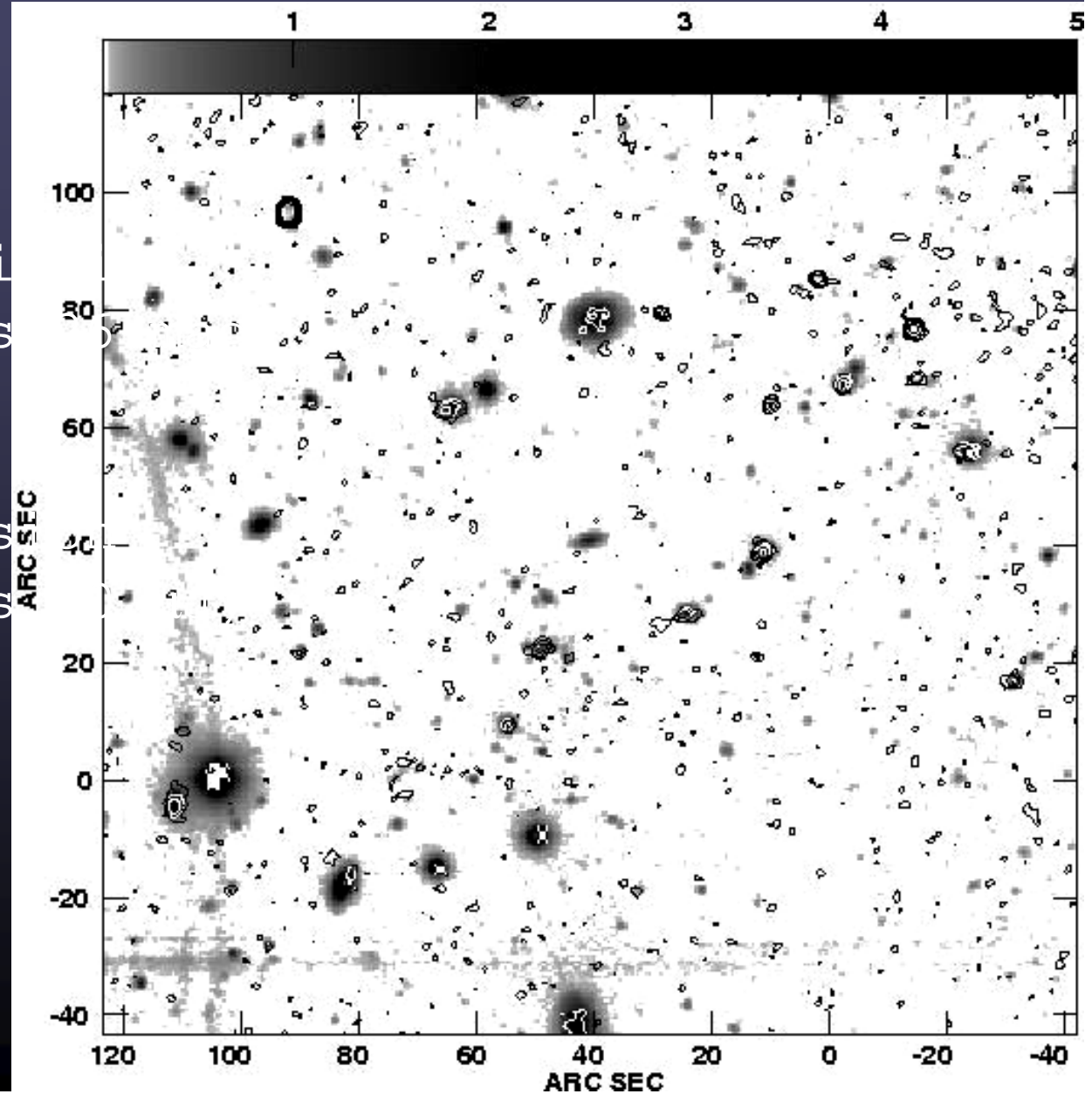
## DEEP RADIO / OPTICAL COMPARISON

Grey-Scale:

Optical emission  
faintest is

Contours:

Radio Emission  
faintest is



# Radio Source Alignment at Different Frequencies

Self-calibration at each frequency aligns maximum at (0,0) point

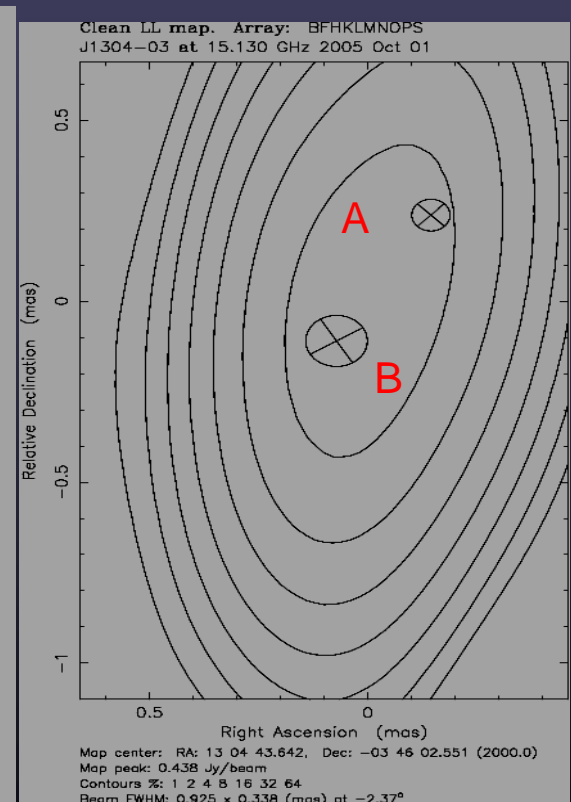
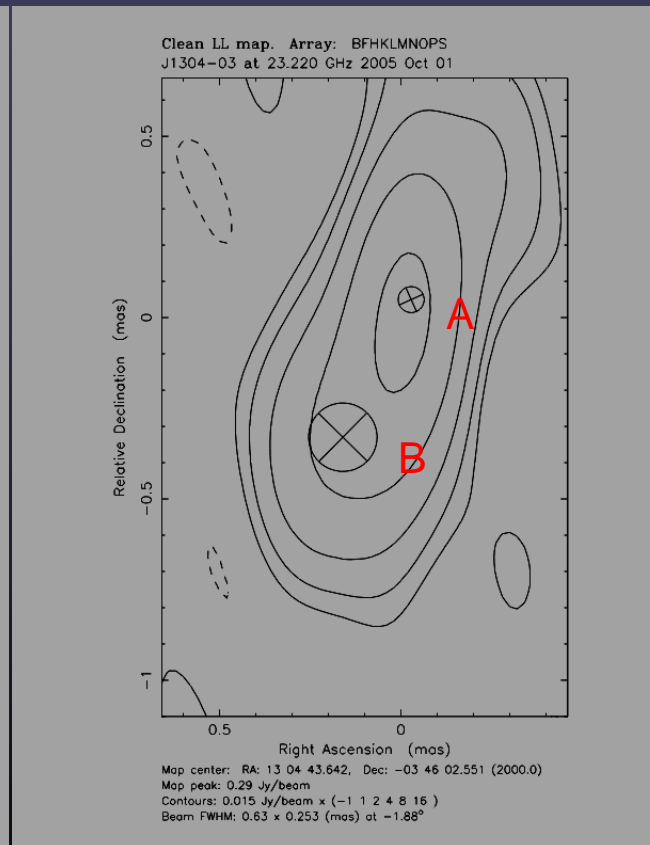
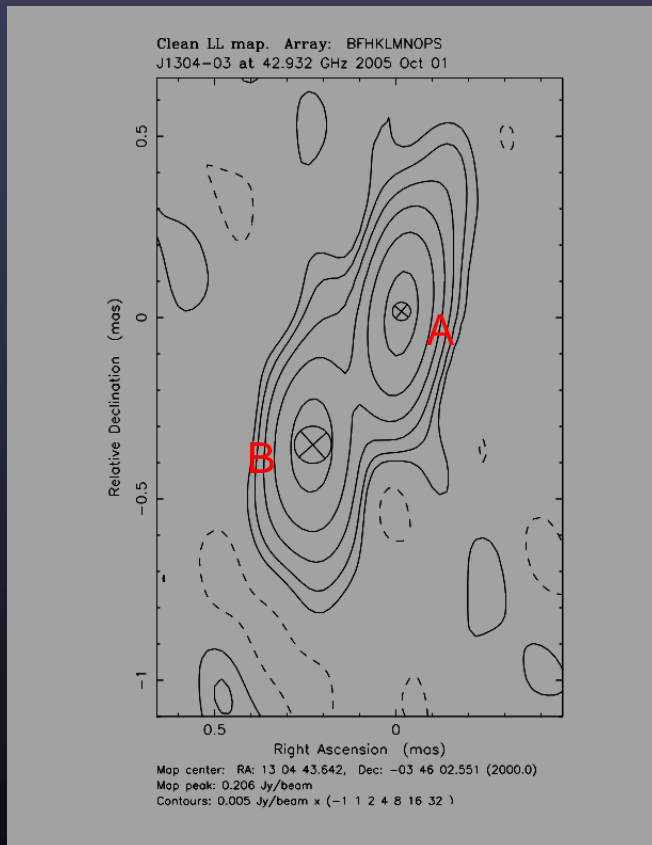
Frequency-dependent structure causes relative position of maximum to change

Fitting of image with components can often lead to proper registration

43 GHz: res = 0.3 mas

23 GHz: res = 0.6 mas

15 GHz: res = 0.8 mas



(Reid Lecture on Astrometry, Walker Lecture on VLBA Upgrade)



## IMAGE ANALYSIS: SUMMARY

- Analyze and display data in several ways  
Adjust resolution to illuminate desired interpretation, analysis
- Parameter fitting useful, but try to obtain error estimate  
Fitting in u-v plane, image plane
- Comparison of multi-plane images tricky (Polarization and Spectral Line)  
Use different graphics packages, methods, analysis tools
- Registration of a field at different frequencies or wave-bands and be subtle.  
Often use adhoc methods by aligning 'known' counterparts