











Millimeter Interferometry and ALMA

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Eleventh Synthesis Imaging Workshop Socorro, June 10-17, 2008



Outline





- The ALMA project and status
- Unique science at mm & sub-mm wavelengths
- Problems unique to mm/sub-mm observations
 - Atmospheric opacity
 - Absolute gain calibration
 - Tracking atmospheric phase fluctuations
 - Antenna and instrument constraints
- Summary







Practical aspects of observing at high frequency with the VLA

What is ALMA?

- A global partnership to deliver a transformational millimeter/submillimeter instrument North America (US, Canada) Europe (ESO) East Asia (Japan,Taiwan)
- 5000m (16,500 Ft) site in Chilean Atacama desert
- Main Array: 50 x 12m antennas (up to 64 antennas)
 - + 4 x 12m (total power) + ACA: compact array of 12 x 7m antennas
- Total cost ~1.3 Billion (\$US)





ALMA

- Baselines up to 15 km (0.015" at 300 GHz) in "zoom lens" configurations
- Sensitive, precision imaging between 30 to 950 GHz (10 mm to 350 µm)
- Receivers: low-noise, wide-band (8 GHz)
- Flexible correlator with high spectral resolution at wide bandwidth
- Full polarization capabilities
- A resource for ALL astronomers including pipeline products and regional science centers



Summary of Existing and Future mm/sub-mm Arrays

| Telescope | altitude (feet) | diam. (m) | No. dishes | A s (m²) | [∨] max (GHz) |
|-------------------|--------------------|--------------|---------------|-------------|---------------------------|
| NMA | 2,000 | 10 | 6 | 470 | 250 |
| EVLA | 7,050 | 25 | 27 | 13250 | 43 |
| CARMA | 7,300 | 3.5/6/10 | 23 | 800 | 250 |
| IRAM PdB | 8,000 | 15 | 6 | 1060 | 250 |
| SMA | 13,600 | 6 | 8 | 230 | 650 |
| eSMA | 13,600 | 6/10/15 | 10 | 490 | 345 |
| ALMA ¹ | 16,400 | 12 | 50 | 5700 | 950 |
| ACA | 16,400 | 7 | 12 | 490 | 950 |

¹ First call for early science proposals expected in Q2 2010

ALMA will be 10-100 times more sensitive and have 10-100 times better angular resolution compared to current millimeter interferometers



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AOS (High Site) Completed



Houses the ALMA and ACA correlators



ACA correlator being installed at AOS

OSF (mid-level) Construction Completed



Hardware arriving in Chile



1st quadrant of ALMA correlator



- Surfaces better than 15 µm!
- Pointing accuracy 2" absolute, 0.6" offset
- Fast switching (1.5 deg in 1.5 sec)
- Currently 4 Vertex and all 4 Melco 12m (total power)



An Important ALMA Milestone: Spectrum from ALMA Test Facility

- "Real" ALMA scheduling blocks are being run routinely at the ATF
- ALMA data format ASDM ⇒ CASA filler completed
- CASA routinely being used to reduce data at the ALMA Test Facility at VLA





ATF Orion spectrum (four datasets) edited and calibrated in CASA

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Current Projected Timeline

- Mid 2008 Testing at ATF continues
- Fall 2008 Commissioning Begins at OSF
- Mid 2009 Commissioning Begins with 3-element array at AOS
- Mid 2010 Call for Early Science Proposals
 - * 24+ antennas, 2+ bands, continuum & spectral line, 1km baselines
- Early 2011 Start Early Science
 - * Off line data reduction
- Mid 2012 Pipeline images for standard modes
- Early 2013 Baseline ALMA Construction Complete



Highest Level-1 Science Drivers

Bilateral Agreement Annex B:

- The ability to image the gas kinematics in a solar-mass protostellar/ protoplanetary disk at a distance of 150 pc (roughly, the distance of the starforming clouds in Ophiuchus), enabling one to study the physical, chemical, and magnetic field structure of the disk and to detect the tidal gaps created by planets undergoing formation.
- The ability to detect spectral line emission from CO or CII in a normal galaxy like the Milky Way at a redshift of z = 3, in less than 24 hours of observation.
- The ability to provide precise images at an angular resolution of 0.1". Here the term precise image means accurately representing the sky brightness at all points where the brightness is greater than 0.1% of the peak image brightness.

These goals drive the technical specifications of ALMA.

Why Do We Care About mm/submm?

- After the 3K cosmic background radiation, mm/submm photons carry most of the radiative energy in the Universe:
 - 40% of Milky Way photons are in mm/submm
- Unique science because of the sensitivity to thermal emission from dust and molecular lines:

In Rayleigh-Jeans regime, $hv \ll kT$,

 $S_{v} = \frac{2kTv^{2}\tau_{v}\Omega}{c^{2}} \qquad Wm^{-2} Hz^{-1}$

for optically-thin emission $\underline{\tau}_\nu \propto \nu^2$, flux density: $S_\nu \propto \nu^4$



Exploration of the Solar System

- 'Weather' on Venus, Mars, Jovian planets
- Comets
- Volcanism on lo
- Search for Molecules from the "Fountains of Enceladus"
- Better understand Minor Planets. For examle: 'Eris' with its moon 'Dysnomia' easily resolved, Eris could be imaged.





Searching for "dust gaps" in Nearby Low Mass Protoplanetary Disks¹⁵



Simulation of the 950 GHz dust emission from a 1 Jupiter Mass planet around a 0.5 Solar mass star (orbital radius 5 AU)

- The disk mass was set to that of the Butterfly star in Taurus
- Integration time 8 hours; 10 km baselines; 30 degrees phase noise

Wolf & D'Angelo (2005)

Understanding how Massive Stars form though Hot Core Line Emission₁₆



ALMA will improve resolution and spectral line sensitivity by more than a factor of 25!

Brogan, Hunter et al. in prep

ALMA Simulation: Rotating m = 1 Spiral



Galaxy Structure and Evolution



CO(1-0) BIMA-SONG



Helfer et al. (2003)

M82 starburst Red: optical emission Blue: x-ray emission Green: OVRO ¹²CO(J=1-0) (Walter, Weiss, Scoville 2003) Ability to trace chemical composition of galaxies to z=3 in less than 24 hours





Study of 'first light' During Cosmic Reionization



Current State-of-art: Tens of hours to detect rare, systems (FIR $\sim 1 \times 10^{13} \text{ L}_{\odot}$)

- Brightest submm galaxies detect dust emission in 1sec (5σ)
- Detect multiple lines in 24 hours => detailed astrochemistry
- Image dust and gas at sub-kpc resolution – gas dynamics!



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ALMA Science Support

- Three regional ALMA science centers: ARCs
- The North American ARC is a partnership between the US and Canada (7.25%)
- One international proposal review committee is envisioned. Details TBD





NAASC: North America ALMA Science Center, Charlottesville, VA

One-stop shopping for:

- Proposals
- Observing scripts
- Data archive and reduction
- Astronomer outreach (summer schools, tutorials, workshops)

Problems unique to the mm/submm

Constituents of Atmospheric Opacity

- Due to the troposphere (lowest layer of atmosphere): h < 10 km
- Temperature ↓ with ↑ altitude: clouds & convection can be significant
- Dry Constituents of the troposphere:, O₂, O₃, CO₂, Ne, He, Ar, Kr, CH₄, N₂, H₂
- H₂O: abundance is highly variable but is < 1% in mass, mostly in the form of water vapor
- "Hydrosols" (i.e. water droplets in the form of clouds and fog) also add a considerable contribution when present



Optical Depth as a Function of Frequency



• At 1.3cm most opacity comes from H₂O vapor

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- At 7mm biggest contribution from dry constituents
- At 3mm both components are significant
- "hydrosols" i.e. water droplets (not shown) can also add significantly to the opacity

Troposphere opacity increases with frequency:



Models of atmospheric transmission from 0 to 1000 GHz for the ALMA site in Chile, and for the VLA site in New Mexico

 \Rightarrow Atmosphere transmission not a problem for λ > cm (most VLA bands)

Mean Effect of Atmosphere on Phase ²⁶

- Since the refractive index of the atmosphere ≠1, an electromagnetic wave propagating through it will experience a phase change (i.e. Snell's law)
- The phase change is related to the refractive index of the air, *n*, and the distance traveled, *D*, by

 ϕ_{e} = (2 π/λ) × *n* × *D*



In addition to receiver noise, at millimeter wavelengths the atmosphere has a significant brightness temperature (T_{skv}) :

For a perfect antenna, ignoring spillover and efficiencies

$$T_{\text{noise}} \approx T_{\text{rx}} + T_{\text{sky}}$$
where $T_{\text{sky}} = T_{\text{atm}} (1 - e^{-\tau}) + T_{\text{bg}} e^{-\tau}$
so $T_{\text{noise}} \approx T_{\text{rx}} + T_{\text{atm}} (1 - e^{-\tau})$

Receiver

temperature

Emission from

atmosphere

T_{atm} = temperature of the atmosphere ≈ 300 K

 $T_{\rm bg}$ = 3 K cosmic background

Before entering atmosphere the source signal $S = T_{source}$

After attenuation by atmosphere the signal becomes $S=T_{source} e^{-\tau}$

Consider the signal-to-noise ratio:

S / N =
$$(T_{\text{source}} e^{-\tau}) / T_{\text{noise}} = T_{\text{source}} / (T_{\text{noise}} e^{\tau})$$

$$T_{\text{sys}} = T_{\text{noise}} e^{\tau} \approx T_{\text{atm}}(e^{\tau} - 1) + T_{\text{rx}}e^{\tau}$$

⇒The system sensitivity drops rapidly (exponentially) as opacity increases

Typical optical depth for 345 GHz observing at the SMA:

at zenith $\tau_{225} = 0.08 = 1.5 \text{ mm PWV}$, at elevation = $30^{\circ} \Rightarrow \tau_{225} = 0.16$ Conversion from 225 GHz to 345 GHz $\Rightarrow \tau_{345} \approx 0.05 + (2.25 \tau_{225}) \approx 0.41$ assume $T_{atm} = 300 \text{ K}$ and $T_{rx} = 100 \text{ K}$ $T_{sys}(\text{DSB}) = T_{sys} e^{\tau} = e^{\tau} (T_{atm}(1 - e^{-\tau}) + T_{rx}) = 1.5(101 + 100) \approx 300 \text{ K}$

 \Rightarrow Atmosphere adds considerably to T_{sys} and since the opacity can change rapidly, T_{sys} must be measured often

Many MM/Submm receivers are double sideband, thus the effective T_{sys} for spectral lines (which are inherently single sideband) is doubled:

$$T_{sys}(SSB) = 2 T_{sys} (DSB) \sim 600 K$$

Sensitivity: Receiver noise temperature



Interferometric MM Measurement of T_{svs}

- How do we measure $T_{sys} = T_{atm}(e^{\tau}-1) + T_{rx}e^{\tau}$ without constantly measuring T_{rx} and the opacity?
- T_{sys} is obtained by the "chopper wheel" method i.e. putting an ambient temperature load (T_{load}) in front of the receiver and measuring the resulting power compared to power when observing sky (Penzias & Burrus 1973).

Load in
$$V_{in} = G T_{in} = [T_{rx} + T_{load}]$$

Load out $V_{out} = G T_{out} = [T_{rx} + T_{atm}(1 - e^{-\tau}) + T_{bg}e^{-\tau} + T_{source}e^{-\tau}$
assume $T_{atm} \approx T_{load}$
Comparing $\frac{V_{in} - V_{out}}{V_{out}} = \frac{T_{load}}{T_{sys}}$
 $T_{sys} = T_{load} * T_{out} / (T_{in} - T_{out})$
Power is really observed but is ∞ T in the R-J limit

 IF T_{atm} ≈ T_{load}, and T_{sys} is measured often, changes in mean atmospheric absorption are corrected. ALMA will have a two temperature load system which does not require assuming T_{atm} ≈ T_{load}



SMA calibration load swings in and out of beam

Example SMA 345 GHz T_{sys} Measurements ³¹





Absolute gain calibration

There are no non-variable quasars in the mm/sub-mm for setting the absolute flux scale

Instead, planets and moons are typically used: roughly black bodies of known size and temperature:

Uranus @ 230 GHz: $S_v \sim 37$ Jy, θ ~ 4" Callisto @ 230 GHz: $S_v \sim 7.2$ Jy, θ ~ 1.4"

- S_v is derived from models, and can be uncertain by ~ 10%
- If the planet is resolved, you need to use visibility model for each baseline
- If larger than primary beam it shouldn't be used (can be used for bandpass)



Atmospheric phase fluctuations

- Variations in the amount of precipitable water vapor (PWV) cause phase fluctuations, which are worse at shorter wavelengths, and result in
 - Low coherence (loss of sensitivity)
 - Radio "seeing", typically 1"- 3" at 1 mm
 - Anomalous pointing offsets
 - Anomalous delay offsets

Simplifying assumption:

The timescale for changes in the water vapor distribution is long compared to time for wind to carry features over the array

 V_w ~10 m/s



Patches of air with different water vapor content (and hence index of refraction) affect the incoming wave front differently.

Atmospheric phase fluctuations, continued...



- "Root phase structure function" (Butler & Desai 1999)
- RMS phase fluctuations grow as a function of increasing baseline length until break when baseline length ≈ thickness of turbulent layer
- The position of the break and the maximum noise are weather and wavelength dependent

RMS phase of fluctuations given by Kolmogorov turbulence theory

$$\phi_{\mathsf{rms}} = K b^{\alpha} / \lambda \text{ [deg]}$$

- *b* = baseline length (km)
- α = 1/3 to 5/6
- λ = wavelength (mm)
- K = constant (~100 for ALMA, 300 for VLA)

36 Atmospheric phase fluctuations, continued... 22 GHz VLA observations of 2 sources observed simultaneously 100 2 VLA:W16 50 0423+418 Antennas 2 & -100 5 are adjacent, 120–13 VLA:W4 phases track 9 140 -160 each other closely Antennas 12 & 01 00 00 40 45 50 55 13 are adjacent, TIME (HOURS) phases track 5 VLA:W18 100 each other 0432+416 closely -100 12 VLA:W6 160 140 Deg 120 100 01 00 00 40 45 50 55

Self-cal applied using a reference antenna within 200 m of W4 and W6, but 1000 m from W16 and W18:

TIME (HOURS)

⇒Long baselines have large amplitude, short baselines smaller amplitude

⇒ Nearby antennas show correlated fluctuations, distant ones do not

VLA observations of the calibrator 2007+404

at 22 GHz with a resolution of 0.1" (Max baseline 30 km):

one-minute snapshots at t = 0 and t = 59 min

Position offsets due to large scale structures that are correlated ⇒ phase gradient across array

Reduction in peak flux (decorrelation) and smearing due to phase fluctuations over 60 min



Sidelobe pattern shows signature of antenna based phase errors ⇒ small scale variations that are not correlated

No sign of phase fluctuations with timescale ~ 30 s

⇒ Uncorrelated phase variations degrades and decorrelates image

⇒ Correlated phase offsets = position shift

Phase fluctuations: loss of coherence



Coherence = (vector average/true visibility amplitude) = $\langle V \rangle / V_0$

Where, $V = V_0 e^{i\phi}$

The effect of phase noise, ϕ_{rms} , on the measured visibility amplitude in a given averaging time:

 $\langle V \rangle = V_0 \times \langle e^{i\phi} \rangle = V_0 \times e^{-\phi^2 rms/2}$ (Gaussian phase fluctuations)

 $V_{\mathbf{0}}$

Example: if $\phi_{\text{rms}} = 1$ radian (~60 deg), coherence = $\langle V \rangle = 0.60$

Phase fluctuations: radio "seeing"



Phase variations lead to decorrelation that worsens as a function of baseline length

Point-source response function for various power-law models of the rms phase fluctuations (Thompson, Moran, & Swenson 1986)

 $\langle V \rangle / V_0 = \exp(-\phi^2_{rms}/2) = \exp(-[K' b^{\alpha} / \lambda]^2/2)$ [Kolmogorov with K'=K *pi/180]

- Measured visibility decreases with baseline length, b, (until break in root phase structure function)
- Source appears resolved, convolved with "seeing" function

⇒ Without corrections diffraction limited seeing is precluded for baselines longer than 1 km at ALMA site!

⇒ Phase fluctuations severe at mm/submm wavelengths, correction methods are needed

- Self-calibration: OK for bright sources that can be detected in a few seconds.
- Fast switching: used at the VLA for high frequencies and will be used at CARMA and ALMA. Choose fast switching cycle time, t_{cyc}, short enough to reduce φ_{rms} to an acceptable level. Calibrate in the normal way.
- Phase transfer: simultaneously observe low and high frequencies, and transfer scaled phase solutions from low to high frequency
- Paired array calibration: divide array into two separate arrays, one for observing the source, and another for observing a nearby calibrator.
 - Will not remove fluctuations caused by electronic phase noise
 - Only works for arrays with large numbers of antennas (e.g., VLA, ALMA)

Phase correction methods (continued):

 Radiometry: measure fluctuations in T_B^{atm} with a radiometer, use these to derive changes in water vapor column (w) and convert this into a phase correction using



total power (IRAM, BIMA)

ALMA: Radiometer Phase Correction

183 GHz Water Vapor Radiometers, tested at SMA





Mike Reid et al, 2006

Antenna requirements

 Pointing: for a 10 m antenna operating at 350 GHz the primary beam is ~ 20"

a 3" error $\Rightarrow \Delta(Gain)$ at pointing center = 5%

 Δ (Gain) at half power point = 22%

 \Rightarrow need pointing accurate to ~1"

 \Rightarrow ALMA pointing accuracy goal 0.6"

- Aperture efficiency, η: Ruze formula gives
 - $η = \exp(-[4\pi\sigma_{rms}/\lambda]^2)$
 - \Rightarrow for η = 80% at 350 GHz, need a surface accuracy, σ_{rms} , of 30 μm
 - \Rightarrow ALMA surface accuracy goal of 15 μ m

Antenna requirements, continued...

 Baseline determination: phase errors due to errors in the positions of the telescopes are given by

$$\Delta \phi = \frac{2\pi}{\lambda} \times \Delta b \times \Delta \theta$$

 $\Delta \theta$ = angular separation between source & calibrator

 Δb = baseline error

Note: $\Delta \theta$ = angular separation between source and calibrator, can be > 20° in mm/sub-mm \Rightarrow to keep $\Delta \phi < \Delta \theta$ need $\Delta b < \lambda/2\pi$ e.g., for λ = 1.3 mm need $\Delta b < 0.2$ mm

Problems, continued...

- Instrument stability
 - Must increase linearly with frequency (delay lines, oscillators, etc...)
- Millimeter/sub-mm receivers
 - SIS mixers needed to achieve low noise characteristics
 - Cryogenics cool receivers to a few K
 - IF bandwidth
- Correlators
 - − Need high speed (high bandwidth) for spectral lines: $\Delta V = 300 \text{ km s}^{-1} \rightarrow 1.4 \text{ MHz} @ 1.4 \text{ GHz}; 230 \text{ MHz} @ 230 \text{ GHz}$
 - Broad bandwidth also needed for sensitivity to thermal continuum and phase calibration
- Limitations of existing and future arrays
 - Small FoV ⇒ mosaicing: FWHM of 12 m antenna @ 230 GHz is ~ 30"
 - Limited *uv*-coverage, small number of elements (improved with CARMA, remedied with ALMA)

Summary

- ALMA construction is well underway and the science opportunities are astounding
- Atmospheric emission can dominate the system temperature
 - Calibration of T_{sys} is different from that at cm wavelengths
- Tropospheric water vapor causes significant phase fluctuations
 - Need to calibrate more often than at cm wavelengths
 - Phase correction techniques are under development at all mm/sub-mm observatories around the world
 - Observing strategies should include measurements to quantify the effect of the phase fluctuations
- Instrumentation is more difficult at mm/sub-mm wavelengths
 - Observing strategies must include pointing measurements to avoid loss of sensitivity
 - Need to calibrate instrumental effects on timescales of 10s of mins, or more often when the temperature is changing rapidly



Extra Slides

Practical aspects of observing at high frequencies 48 with the VLA

Note: details may be found at http://www.aoc.nrao.edu/vla/html/highfreg/

- Observing strategy: depends on the strength of your source
 - Strong (≥ 0.1 Jy on the longest baseline for continuum observations, stronger for spectral line): can apply self-calibration, use short integration times; no need for fast switching
 - Weak: external phase calibrator needed, use short integration times and fast switching, especially in A & B configurations
 - If strong maser in bandpass: monitor the atmospheric phase fluctuations using the maser, and apply the derived phase corrections; use short integration times, calibrate the instrumental phase offsets between IFs every 30 mins or so

Practical aspects, continued...

- Referenced pointing: pointing errors can be a significant fraction of a beam at 43 GHz
 - Point on a nearby source at 8 GHz every 45-60 mins, more often when the az/el is changing rapidly. Pointing sources should be compact with $F_{8GHz} \ge 0.5$ Jy
- Calibrators at 22 and 43 GHz
 - Phase calibration: the spatial structure of water vapor in the troposphere requires that you find a phase calibrator < 3° from your source, if at all possible; for phase calibrators weaker than 0.5 Jy you will need a separate, stronger source to track amplitude variations
 - Absolute Flux calibrators: 3C48/3C138/3C147/3C286. All are extended, but there are good models available for 22 and 43 GHz

Practical aspects, continued...

- If you have to use fast switching
 - Quantify the effects of atmospheric phase fluctuations (both temporal and spatial) on the resolution and sensitivity of your observations by including measurements of a nearby point source with the same fast-switching settings: cycle time, distance to calibrator, strength of calibrator (weak/strong)
 - If you do not include such a "check source" the temporal (but not spatial) effects can be estimated by imaging your phase calibrator using a long averaging time in the calibration
- During the data reduction
 - Always correct bandpass before phase and amplitude calibration
 - Apply phase-only gain corrections first, to avoid de-correlation of amplitudes by the atmospheric phase fluctuations

The Atmospheric Phase Interferometer at the VLA



Accessible from http://www.vla.nrao.edu/astro/guides/api

Results from VLA 22 GHz Water Vapor Radiometry ⁵²



Transparent Site Allows Complete Spectral Coverage⁵³

* 10 Frequency bands

 Bands available from start: B3 (3mm, 100 GHz), B6 (1mm, 230 GHz), B7 (.85mm; 345 GHz) and B9 (.45mm, 650 GHz)

Some B4 (2mm, 150 GHz), B8
 (.65mm, 450 GHz) and later B10
 (.35mm, 850 GHz), built by Japan

A few B5 (1.5mm, 183 GHz) receivers built with EU funding

B1 and B2 have not yet been assigned

✤ All process 16 GHz of data

- Dual pol x 2SBs x 5.5 GHz (B6)
- Dual pol x 2SBs x 4 GHz (B3, B4, B5, B7, B8)
- Dual pol x DSB x 8 GHz (B9, B10)



Atmospheric transmission at Chajnantor, pwv = 0.5 mm

| | Francisco | Receiver noise temp | | | Dessions |
|--------------|--------------------|--|--|---------------|------------|
| ALMA Band | Frequency Range | T _{Rx} over 80% of the RF band | T _{Rx} at any RF frequency | Mixing scheme | technology |
| 1 | 31.3 – 45 GHz | 17 K | 28 K | USB | НЕМТ |
| 2 | 67 – 90 GHz | 30 K | 50 K | LSB | НЕМТ |
| 3 | 84 – 116 GHz | 37 K | 62 K | 2SB | SIS |
| 4 | 125 – 163 GHz | 51 K | 85 K | 2SB | SIS |
| 5 | 163 - 211 GHz | 65 K | 108 K | 2SB | SIS |
| 6 | 211 – 275 GHz | 83 K | 138 K | 2SB | SIS |
| 7 | 275 – 373 GHz | 147 K | 221 K | 2SB | SIS |
| 8 | 385 – 500 GHz | 98 K | 147 K | 2SB | SIS |
| 9 | 602 – 720 GHz | 175 K | 263 K | DSB | SIS |
| 10 | 787 – 950 GHz | 230 K | 345 K | DSB | SIS |

Dual, linear polarization channels: •Increased sensitivity •Measurement of 4 Stokes parameters

183 GHz water vapour radiometer: •Used for atmospheric path length correction

(1 minute; 75% Quartile opacities λ >1mm, 25% λ <1mm)

| Frequency (GHz) | Continuum (mJy) | Line 1 km s ⁻¹ (mJy) | Line 25 km s ⁻¹ (mJy) |
|-----------------|-----------------|------------------------------------|-------------------------------------|
| 35 | 0.02 | 5.1 | 1.03 |
| 110 | 0.027 | 4.4 | 0.89 |
| 140 | 0.039 | 5.1 | 1.01 |
| 230 | 0.071 | 7.2 | 1.44 |
| 345 | 0.12 | 10 | 1.99 |
| 675 | 0.85 | 51 | 10.2 |
| 950 | 1.26 | 66 | 13.3 |