



## Mm-Wave Interferometry

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- Why a special lecture on mm interferometry?
  - everything about interferometry is more difficult at high frequencies
  - some of the problems are unique to the mm/submm, and affect the way observations are carried out

## Why do we care about mm/submm?

- unique science can be done at mm/submm wavelengths, because of the sensitivity to thermal emission from dust and molecular lines
- e.g.: @  $\lambda = 1 \text{ mm}$  ( $\nu = 300 \text{ GHz}$ )  $h\nu/k \sim 14 \text{ K}$ 
  - ⇒ probe of cool gas and dust in:
    - molecular clouds
    - dust in dense regions
    - star formation in our Galaxy and in the high-redshift universe
    - protoplanetary disks
    - etc...

## Science at mm/submm wavelengths: dust emission

In the Rayleigh-Jeans regime,  $h\nu \ll kT$ ,

$$S_\nu = \frac{2kT\nu^2 \tau_\nu \Omega}{c^2} \quad \text{W m}^{-2} \text{Hz}^{-1}$$

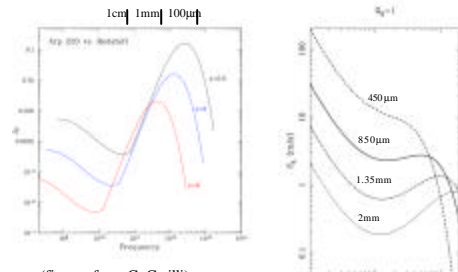
dust opacity  $\propto \nu^2$

so for optically-thin emission, flux density

$$S_\nu \propto \nu^4; \quad T_B \propto \nu^2$$

⇒ emission is brighter at higher frequencies

## Star-forming galaxies in the early universe



(figures from C. Carilli)

## Science at mm/submm wavelengths: molecular line emission

- most of the dense ISM is  $\text{H}_2$ , but  $\text{H}_2$  has no permanent dipole moment ⇒ use trace molecules
- lines from heavy molecules → mm
- lighter molecules (e.g. hydrides) → submm

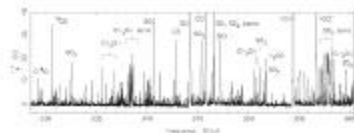
Table 28-6. Low Order Rotational Transitions of Simple Diatomic Molecules\*

Molecule	J=1-0	J=2-1	J=3-2	$\nu_{rot}$ (cm <sup>-1</sup> )
	GHz	GHz	GHz	cm <sup>-1</sup>
CO	115.273	230.539	345.790	$10^2 - 10^3$
CS	65.806	131.611	197.416	$10^2 - 10^3$
HCN	89.433	178.866	268.299	$10^2$
HCO <sup>+</sup>	89.388	178.773	268.151	$10^2$
SiO	43.122	86.243	129.364	$10^2 - 10^3$

+ many more complex molecules ( $\text{CH}_3\text{CH}_2\text{CN}$ ,  $\text{CH}_2\text{OHCHO}$ ,  $\text{CH}_3\text{COOH}$ , etc.)

- probe kinematics, density, temperature
- abundances, interstellar chemistry, etc...
- for an optically-thin line it turns out that

$$S_\nu \propto \nu^4; \quad T_B \propto \nu^2 \quad (\text{cf. dust})$$



Spectrum of molecular emission from Orion at 345 GHz

## Problems unique to the mm/submm

- atmospheric opacity: raises  $T_{sys}$ , attenuates source
  - opacity vs frequency and altitude, typical values
  - calibration techniques, rapid calibration
- atmospheric phase fluctuations
  - cause of the fluctuations: variable  $H_2O$
  - current and planned calibration schemes
- antennas
  - pointing accuracy, surface accuracy
  - baseline determination
- instrument stability

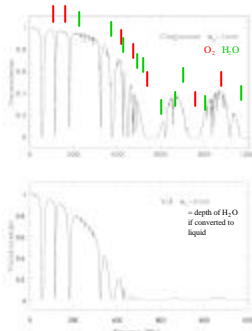
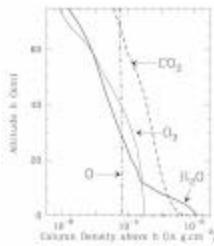
## Problems, continued...

- millimeter/submm receivers (will not be discussed further)
  - SIS mixers, cryogenics
  - local oscillators
  - IF bandwidths
- correlators (will not be discussed further)
  - need high speed (high bandwidth) for spectral lines:  $\Delta V = 300 \text{ km s}^{-1}$ 
    - $\equiv 1.4 \text{ MHz @ } 1.4 \text{ GHz}, 230 \text{ MHz @ } 230 \text{ GHz}$
  - broad bandwidth also needed for sensitivity to thermal continuum and phase calibration,  $\geq \text{GHz}$
- existing and future arrays
  - small field of view, need for mosaicing: FWHM of 10 m antenna @ 230 GHz is  $\sim 30''$
  - limited  $m$ -coverage, small number of elements

## Atmospheric opacity

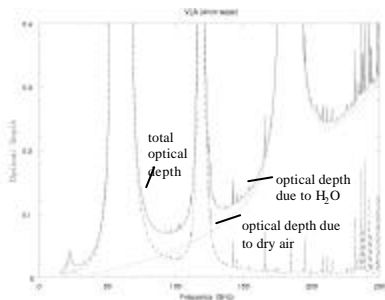
•due to the troposphere,  $h \leq 7-10 \text{ km}$

- constituents of the troposphere = dry air ( $N_2, O_2, Ar, CO_2, Ne, He, Kr, CH_4, H_2, N_2O$ )
  - + $H_2O$ : abundance is highly variable but is  $< 1\%$  in mass, mostly in the form of water vapor
  - +particulates



Transmission of the atmosphere from 0 to 1000 GHz for the ALMA site in Chile, and for the VLA site in New Mexico

$\Rightarrow$  atmosphere little problem for  $\lambda > \text{cm}$  (most VLA bands)



Optical depth of the atmosphere at the VLA site

## Effect of atmospheric noise on $T_{sys}$

- consider a simple cascaded amplifier system, with one component:

input  $S_n + N1$   $\xrightarrow{\text{gain } G}$  output =  $G(S_n + N1)$

output noise relative to  $S_n$ ,  $N_{out} = G N1 / G = N1$

- now consider two components:

input  $S_n$   $\xrightarrow{N1}$   $\xrightarrow{G1}$   $\xrightarrow{N2}$   $\xrightarrow{G2}$  output =  $G2[G1(S_n + N1) + N2]$

...divide by  $G1G2$  to find noise relative to  $S_n$ , then

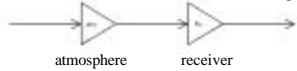
$$N_n^{eff} = N1 + \frac{N2}{G1}$$

...and in general,  $N_n^{eff} = N1 + \frac{N2}{G1} + \frac{N3}{G1G2} + \dots$

## Atmospheric opacity, continued...

Now consider the troposphere as the first element of a cascaded amplifier system:

- $G_{\text{atm}} = e^{-\tau}$
- $T_{\text{B}}^{\text{atm}} = T_{\text{atm}} \times (1 - e^{-\tau})$ , where  $T_{\text{atm}}$  = physical temperature of the atmosphere, ~ 300 K



- "effective" system noise temperature scaled to the top of the atmosphere (i.e., relative to the unattenuated celestial signal) is:

$$T_{\text{sys}}^{\text{eff}} = e^{\tau} \times [T_{\text{atm}} \times (1 - e^{-\tau}) + T_{\text{rec}}]^*$$

\*ignoring spillover terms, etc.

## Atmospheric opacity, continued...

•example: typical 1.3 mm conditions at OVRO

- $\tau_0 = 0.2$ , elevation =  $30^\circ \Rightarrow \tau = 0.4$
- $T_{\text{sys}}(\text{DSB}) = 1.5 (100 + 50) = 225 \text{ K}$
- dominated by the atmosphere
- if receiver is double side band and sideband gain ratios are unity, then

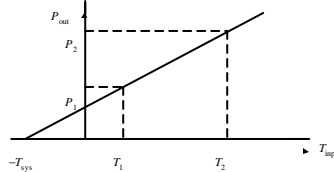
$$T_{\text{sys}}(\text{SSB}) = 2 T_{\text{sys}}(\text{DSB}) = 450 \text{ K} \quad \text{--very noisy}$$

•so: atmosphere is noisy and is often the dominant contribution to  $T_{\text{sys}}$ ; it is a function of airmass and changes rapidly, so need to calibrate often

## Calibration of $T_{\text{sys}}$

•systems are linear  $\Rightarrow P_{\text{out}} = m \times (T_{\text{in}} + T_{\text{sys}})$

•if  $P_{\text{out}} = 0$  then  $T_{\text{in}} = -T_{\text{sys}}$ :



$$T_{\text{sys}} = \frac{(T_2 - T_1) P_1 - T_1 (P_2 - P_1)}{(P_2 - P_1)}$$

## Calibration of $T_{\text{sys}}$ , continued...

•at cm wavelengths loads  $T_1$  and  $T_2$  are the 3 K cosmic background radiation and a noise source with known noise temperature switched into the signal path

•at mm wavelengths we need two known loads above the atmosphere!

- (1) 3 K cosmic background radiation
- (2)  $T_{\text{atm}}$  obtained from a load placed in front of the feed at  $T_{\text{ambient}} \sim T_{\text{atm}}$

$$\text{load at } T_{\text{atm}} \rightarrow \left\{ \begin{array}{l} \text{atmosphere} \\ \text{loss + emission} \end{array} \right\} \rightarrow T_{\text{atm}} e^{-\tau} + T_{\text{atm}} (1 - e^{-\tau}) = T_{\text{atm}}$$

cancel for  $T_{\text{load}} = T_{\text{atm}}$

## Absolute gain calibration

•there are no non-variable quasars in the mm/submm for setting the absolute flux scale; instead, have to use:

•planets: roughly black bodies of known size and temperature, e.g., Uranus @ 230 GHz has  $S_{\nu} \sim 37 \text{ Jy}$ , diameter  $\sim 4''$

- problem: if the planet is resolved by the array, have to use single-dish (total power) calibration
- if the planet is resolved by the primary beam, have to know its sidelobe pattern
- $S_{\nu}$  is derived from models, can be uncertain by ~ 10%

•stars: black bodies of known size

-e.g., the Sun at 10 pc:  $S_{\nu} \sim 1.3 \text{ mJy}$  @ 230 GHz, diameter  $\sim 1 \text{ mas}$

-problem: very faint! not possible for current arrays, but will be useful for ALMA

## Atmospheric phase fluctuations

•at mm wavelengths variable atmospheric propagation delays are due to tropospheric water vapor (ionosphere is important for  $\nu < 1 \text{ GHz}$ )

•the phase change experienced by an electromagnetic wave is related to the refractive index of the air and the distance traveled by

$$\phi_c = 2\pi \times n \times D$$

or in terms of an "electrical pathlength",  $L_c = \lambda \times \phi_c = n \times D$

•for water vapor

$$n \propto \frac{pwv}{DT_{\text{atm}}}$$

so

$$L_c \approx 6.3 \times pwv$$

and

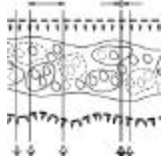
$$\phi_c \approx \frac{12.6\pi}{\lambda} \times pwv$$

## Atmospheric phase fluctuations, continued...

•variations in the amount of precipitable water vapor therefore cause

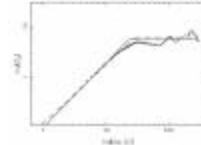
- pointing offsets, both predictable and anomalous
- delay offsets
- phase fluctuations, which are worse at shorter wavelengths, and result in
  - low coherence (loss of sensitivity)
  - radio "seeing", typically 1-3" at  $\lambda = 1$  mm

•effect of structure in the water vapor content of the atmosphere on different scales:



## Atmospheric phase fluctuations, continued...

Phase noise as function of baseline length

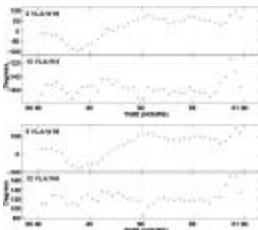


From Butler & Desai 1999

The position of the break and the maximum noise are weather dependent. Kolmogorov turbulence theory  $\rightarrow \phi_{rms} = Kb^\alpha/\lambda$ , where  $\alpha$  is a function of baseline length, and depends on the width of the turbulent layer

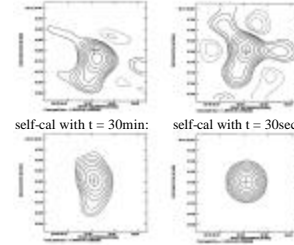
## Atmospheric phase fluctuations, continued...

Antenna-based phase solutions using a reference antenna within 200 m of W4 and W6, but 1000 m from W16 and W18:



VLA observations of the calibrator 2007+404 at 22 GHz with a resolution of 0.1":

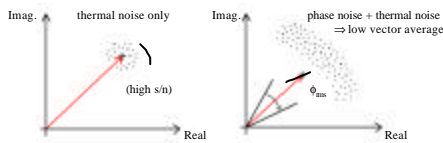
one-minute snapshots:



self-cal with t = 30min:

self-cal with t = 30sec:

## Phase fluctuations: loss of coherence



coherence = vector average  
true visibility

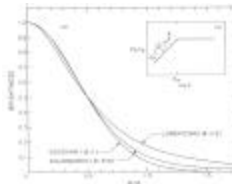
measured visibility  $V = V_0 e^{\phi}$

$\langle V \rangle = V_0 \times \langle e^{\phi} \rangle = V_0 \times e^{-\phi_{rms}^2/2}$  (assumes Gaussian phase fluctuations)

if  $\phi_{rms} = 1$  radian, coherence =  $\langle V \rangle = 0.60$

$V_0$

## Phase fluctuations: radio "seeing"



Point-source response function for various power-law models of the rms phase fluctuations, from Thompson, Moran, & Swenson

$$\langle V \rangle = V_0 \times \exp(-\phi_{rms}^2/2) = V_0 \times \exp(-[Kb^\alpha/\lambda]^2/2)$$

- measured visibility decreases with  $b$

- source appears resolved, convolved with "seeing" function

## Dependence of radio seeing on $\lambda$

•Consider observations at two frequencies, but the same resolution:

$$\lambda_1, b_1$$

$$\lambda_2, b_2 = b_1(\lambda_2/\lambda_1) \text{ for the same resolution}$$

then

$$\left( \frac{\phi_{\text{rms}}}{\lambda} \right)_1 = \left( \frac{\phi_{\text{rms}}}{\lambda} \right)_2 = \left( \frac{b_2}{b_1} \right)^{1-\alpha}$$

for example,  $\alpha = 0.5$ ,  $\lambda_1 = 1 \text{ mm}$ ,  $\lambda_2 = 6 \text{ cm}$ :

$$\left( \frac{\phi_{\text{rms}}}{\lambda} \right)_{1\text{mm}} \sim 8$$

$$\left( \frac{\phi_{\text{rms}}}{\lambda} \right)_{6\text{cm}}$$

$\Rightarrow$  phase fluctuations are severe at mm/submm wavelengths, correction methods are needed

•Self-calibration: OK for bright sources that can be detected in a few seconds

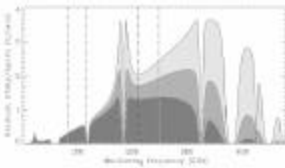
•Fast switching: used at the VLA for high frequencies. Calibrate in the normal way using a calibration cycle time,  $t_{\text{cyc}}$ , short enough to reduce  $\phi_{\text{rms}}$  to an acceptable level. Effective for  $t_{\text{cyc}} < b/v_w$ .

•Paired array calibration: divide array into two separate arrays, one for observing the source, and another for observing a nearby calibrator. Note:

–this method will not remove fluctuations caused by electronic phase noise

–only works for arrays with large numbers of antennas (e.g., VLA)

•Radiometry: measure fluctuations in  $T_B^{\text{atm}}$  with a radiometer, use these to derive the fluctuations in  $\rho w v$ , and convert this into a phase correction using  $\phi_c \approx \frac{12.6\pi}{\lambda} \times \rho w v$



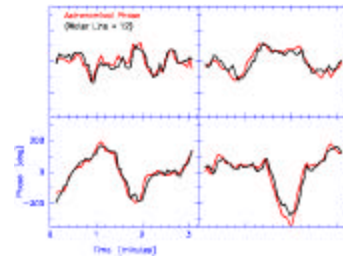
(from Bremer)

Monitor: 22 GHz H<sub>2</sub>O line (OVRO, BIMA, VLA)

183 GHz H<sub>2</sub>O line (CSO-JCMT, SMA, ALMA)

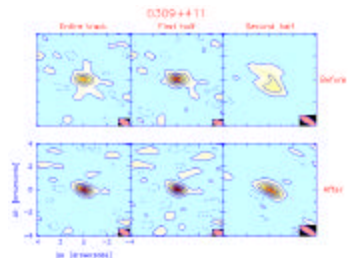
total power (IRAM, BIMA)

## Examples of phase correction: 22 GHz Water Line Monitor at OVRO



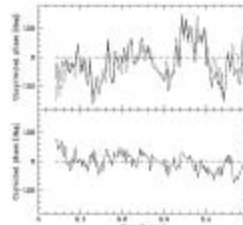
From Carpenter, Woody, & Scoville 1999

## Examples of phase correction: 22 GHz Water Line Monitor at OVRO, continued...



"Before" and "after" images from Woody, Carpenter, & Scoville 2000

## Examples of phase correction: 183 GHz Water Vapor Monitor at the CSO-JCMT



Phase fluctuations are reduced from 60° to 26° ms (from Wiedner et al. 2001).

## Antenna requirements

•Pointing: for a 10 m antenna operating at 350 GHz the primary beam is  $\sim 18''$

a  $3''$  error  $\Rightarrow \Delta(\text{Gain})$  at pointing center = 5%  
 $\Delta(\text{Gain})$  at half power point = 22%  
 $\Rightarrow$  need pointing accurate to  $\sim 1''$

•Aperture efficiency: Ruze formula gives

$$\eta = \exp(-[4\pi\sigma/\lambda]^2)$$

$\Rightarrow$  for  $\eta = 50\%$  at 350 GHz, need a surface accuracy of  $55\mu\text{m}$

•Baseline determination: phase errors due to errors in the positions of the telescopes are

$$\Delta\phi = \frac{2\pi}{\lambda} \times \Delta b \times \Delta\theta$$

$\lambda$

## Antenna requirements, continued...

where  $\Delta\theta$  = angular separation between source and calibrator, and can be  $> 20^\circ$  in mm/submm

$\Rightarrow$  to keep  $\Delta\phi < \Delta\theta$  need  $\Delta b < \lambda/2\pi$

e.g., for  $\lambda = 1.3$  mm need  $\Delta b < 0.2$  mm

## Instrument stability

•Everything is more critical at shorter wavelengths.

–transmission line for the local oscillator should be stable to  $\ll \lambda$

–needs to be temperature controlled

–round-trip path measurements can be  $\sim 1$  turn/day, but quicker at sunrise/sunset

$\Rightarrow$  calibrate instrumental phase every 20 to 30 mins

## Summary of existing and future mm/submm arrays

Telescope	altitude (feet)	diam. (m)	No. dishes	A (m <sup>2</sup> )	$\nu_{\text{max}}$ (GHz)
BIMA <sup>1</sup>	3,500	6	10	280	250
OVRO <sup>1</sup>	4,000	10	6	470	250
CARMA <sup>1</sup>	7,300	3.5/6/10	23	800	250
NMA	2,000	10	6	470	250
IRAM PdB	8,000	15	6	1060	250
JCMT-CSO <sup>2</sup>	14,000	10/15	2	260	650
SMA <sup>3</sup>	14,000	6	8	230	850
ALMA <sup>4</sup>	16,400	12	64	7200	850

<sup>1</sup>BIMA and OVRO will be combined and moved to a higher site to become CARMA

<sup>2</sup>First instrument to obtain submm fringes; will probably be used with the SMA

<sup>3</sup>Currently has 5 antennas, first fringes obtained in September 1999 at 230 GHz

<sup>4</sup>Currently under development, planned for full operation by 2010

Note:

•Existing millimeter instruments are on sites at 1,000 to 2,400 m altitude, with typically a few millimeters of precipitable H<sub>2</sub>O

•Primary beam (field of view)  $\sim 40''$  (IRAM) to  $120''$  (BIMA) at 115 GHz, resolution 1 to 2". Note:

–very small fields of view

–not sensitive to extended emission on scales  $\geq \Omega_{\text{FB}}/3$

–mosaicing necessary for imaging even moderate-sized areas

–small number of antennas make it hard to build up good  $u$ -coverage  $\Rightarrow$  not many *independent* pixels in the image plane

## Practical aspects of observing at high frequencies with the VLA

Note: details may be found at <http://www.aoc.nrao.edu/vla/html/highfreq/>

•Observing strategy: depends on the strength of your source

–Strong ( $\geq 0.1$  Jy on the longest baseline for continuum observations, stronger for spectral line): can apply self-calibration, use short integration times; no need for fast switching

–Weak: external phase calibrator needed, use short integration times and fast switching, especially in A & B configurations

–Sources with a strong maser feature within the IF bandpass: monitor the atmospheric phase fluctuations using the maser, and apply the derived phase corrections to a continuum channel or spectral line channels; use short integration times, calibrate the instrumental phase offsets between the IFs being used every 30 mins or so

## Practical aspects, continued...

•Referenced pointing: pointing errors can be a significant fraction of a beam at 43 GHz

–Point on a nearby source at 8 GHz every 45–60 mins, more often when the az/el is changing rapidly. Pointing sources should be compact with  $F_{8\text{GHz}} \geq 0.5$  Jy

•Calibrators at 22 and 43 GHz

–Phase: the spatial structure of water vapor in the troposphere requires that you find a phase calibrator  $\leq 3^\circ$  from your source, if at all possible; for phase calibrators weaker than 0.5 Jy you will need a separate, stronger source to track amplitude variations

–Flux: 3C48/3C138/3C147/3C286. All are extended, but there are good models available for 22 and 43 GHz

## Practical aspects, continued...

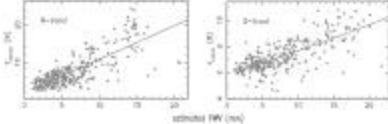
- Opacity corrections and tipping scans

- Can measure the total power detected as a function of elevation, which has contributions

$$T_{\text{sys}} = T_0 + T_{\text{atm}}(1 - e^{-\tau_0}) + T_{\text{spill}}(a)$$

- and solve for  $\tau_0$ .

- Or, make use of the fact that there is a good correlation between the surface weather and  $\tau_0$  measured at the VLA (Butler 2002):



and apply this opacity correction using FILLM in AIPS

## Practical aspects, continued...

- If you have to use fast switching

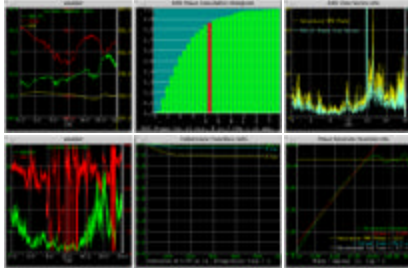
- Quantify the effects of atmospheric phase fluctuations (both temporal and spatial) on the resolution and sensitivity of your observations by including measurements of a nearby point source with the same fast-switching settings: cycle time, distance to calibrator, strength of calibrator (weak/strong)

- If you do not include such a "check source" the temporal (but not spatial) effects can be estimated by imaging your phase calibrator using a long averaging time in the calibration

- During the data reduction

- Apply phase -only gain corrections first, to avoid decorrelation of amplitudes by the atmospheric phase fluctuations

## The Atmospheric Phase Interferometer at the VLA



Accessible from <http://www.aocnrao.edu/vla/html/PhaseMonitor/phaseonhtml>

## Summary

- Atmospheric emission can dominate the system temperature

- Calibration of  $T_{\text{sys}}$  is different from that at cm wavelengths

- Tropospheric water vapor causes significant phase fluctuations

- Need to calibrate more often than at cm wavelengths

- Phase correction techniques are under development at all mm/submm observatories around the world

- Observing strategies should include measurements to quantify the effect of the phase fluctuations

- Instrumentation is harder for mm/ submm

- Observing strategies must include pointing measurements to avoid loss of sensitivity

- Need to calibrate instrumental effects on timescales of 10s of mins, or more often when the temperature is changing rapidly